Concept Learning

Zhang Hongxin zhx@cad.zju.edu.cn

State Key Lab of CAD&CG, ZJU 2008-02-21



Overview



- Learning from examples
- General-to-specific ordering of hypotheses
- Version spaces and candidate elimination algorithm
- Inductive bias

Introduction



- What is concept learning?
 - Induce Boolean function from a sample of positive/negative training examples.
 - Infer the general definition of some concept, given examples labeled as members or nonmembers of the concept.
- Concept learning in daily life
 - 根据人证物证判断犯罪嫌疑人是否有罪
 - 根据笔试面试决定是否录用
 - And more ...

A Demo Task – Enjoy Sport

• Concept:

• days on which my friend Tom enjoys his favorite water sports

• Task:

 predict the value of "Enjoy Sport" for an arbitrary day based on the values of the other attributes

Attributes	ID	Sky	Temp	Humidi ty	Wind	Water	Foreca st	Enjoy
	1	Sunny	Warm	Normal	Strong	Warm	Same	Yes
	2	Sunny	Warm	High	Strong	Warm	Same	Yes
Example	3	Rainy	Cold	High	Strong	Warm	Change	No
	4	Sunny	Warm	High	Strong	Cool	Change	Yes

Training Data

Representing Hypothesis

- Hypothesis h is described as a conjunction of constraints on attributes
- Each constraint can be:
 - A specific value : e.g. Water=Warm
 - A don't care value : e.g. Water=?
 - No value allowed (null hypothesis): e.g. Water=Ø
- Example: hypothesis *h*
 - Sky Temp Humid Wind Water Forecast
 - < Sunny ? ? Strong ? Same >

A Demo Task – Enjoy Sport

• Given:

- Instance Space X: Possible days described by the attributes=[Sky, Temp, Humidity, Wind, Water, Forecast]
- Target function c: Enjoy Sport $X \rightarrow \{0,1\}$
- Hypotheses Space H:
 - conjunction of literals e.g. < Sunny ? ? Strong ? Same >
- Training examples **D**:
 - positive and negative examples of the target function,
 <x1,c(x1)>,..., <xn,c(xn)>

• Determine:

• A hypothesis h in H such that h(x) = c(x) for all x in X.

The Inductive Learning Hypothesis



- Any hypothesis found to approximate the target function well over a sufficiently large set of training examples will also approximate the target function well over other unobserved examples.
- Find the hypothesis that best fits the training data
- 根据已知推断未知,假定已知满足某种规律

Number of Instances, Concepts, Hypotheses

- Sky: sunny, cloudy, rainy
- Air Temp: warm, cold
- Humidity: normal, high
- Wind: strong, weak
- Water: warm, cold
- Forecast: same, change

#distinct instances : 3*2*2*2*2 = 96
#distinct concepts : 2⁹⁶
#syntactically distinct hypotheses : 5*4*4*4*4=5120
#semantically distinct hypotheses : 1+4*3*3*3*3=973



Perspective



- Concept learning can be formulated as a searching:
 - through a predefined space of potential hypotheses for the hypothesis that best fits the training examples.
- General-to-specific ordering

 $h_j \ge_g h_k \longleftrightarrow (\forall x \in X)[(h_k(x) = 1) \rightarrow (h_j(x) = 1)]$

- Example : <Sunny,?,?,?,?,>>= <Sunny,?,?,Strong,?,?>
- Introduce a hierarchy structure into hypotheses space, which leads to efficient searching strategy.

Algorithms

Algorithm	Order	Strategy	N/P	
FIND-S	Specific-to- general	Top-down	Positive	
LIST-THEN- ELIMINATE	General-to- Specific	Bottom-up	Negative	
CANDIDATE- ELIMINATION	Bi-directional	Bi-directional	Both	

FIND-S



- h0 = <0, 0,0, 0, 0. 0> h1 = <Sunny, Warm, Normal, Strong, Warm, Same> $h2 = \langle Sunny, Warm, ?,$
- $h3 = \langle Sunny, Warm, ?,$
- $h4 = \langle Sunny, Warm, ?, \rangle$

Strong, Warm, Same>

Strong, Warm, Same> Strong, ?, ?>

Training examples:

- <Sunny, Warm, Normal, Strong, Warm, Same>, Enjoy Sport = **Yes** 1.
- <Sunny, Warm, High, Strong, Warm, Same>, Enjoy Sport = **Yes** 2.
- <Rainy, Cold, High, Strong, Warm, Change>, Enjoy Sport = **No** 3.
- <Sunny, Warm, High, Strong, Cool, Change>, Enjoy Sport = **Yes** 4.

Report the *most specific* hypothesis



LIST-THEN-ELIMINATE

h0 = <?, ?, ?, ?, ?, ?, ?>
h1 = <Sunny, ?, ?, ?, ?, ?> or
<?, Warm, ?, ?, ?, ?> or
<?, ?, Normal, ?, ?, ?> or
<?, ?, ?, Normal, ?, ?> or
<?, ?, ?, Weak, ?, ?> or
<?, ?, ?, ?, Cold, ?> or
<?, ?, ?, ?, ?, Same >

<Rainy, Cold, High, Strong, Warm, Change>, Enjoy Sport = **No**

Report the most general hypothesis

CANDIDATE-ELIMINATION (1)



G0, G1, G2: {<?, ?, ?, ?, ?, ?>}

Training examples:

- 1. <Sunny, Warm, Normal, Strong, Warm, Same>, Enjoy Sport = Yes
- 2. <Sunny, Warm, High, Strong, Warm, Same>, Enjoy Sport = **Yes**

遇到正例与Find-s方法类似

CANDIDATE-ELIMINATION (2)

S2,S3: {<Sunny, Warm, ?, Strong, Warm, Same>}



Training examples:

3. <Rainy, Cold, High, Strong, Warm, Change>, Enjoy Sport = *No*

遇到反例与List-then-eliminate方法类似

CANDIDATE-ELIMINATION (3)

S3: {<Sunny, Warm, ?, Strong, Warm, Same>} *S4*: {<Sunny, Warm, ?, Strong, ?, ?>}

G3:{<Sunny,?,?,?,?,> <?,Warm,?,?,?,> <?,?,?,Same>

Training examples:

4. <Sunny, Warm, High, Strong, Cool, Change>, Enjoy Sport = Yes



Report the version space - all possible hypotheses

<Sunny,Warm,Normal,Strong,Cool,Change>

<Rainy,Cold,Normal,Light,Warm,Same>

<Sunny,Warm,Normal,Light,Warm,Same>

<Sunny,Cold,Normal,strong,Warm,Same>

Remarks



- Convergence Condition
 - Noise Free (No Errors)
 - The target concept **DOES** exist in the searching hypotheses space *H*
- What Training Example Should the Learner Request Next?
 - Satisfy half the hypotheses in the current version space
 - Fastest Convergence, Least Sample Needed, Best Uncertainty Elimination
- How Can Partially Learned Concepts Be Used?
 - Absolutely Accept <Sunny,Warm,Normal,Strong,Cool,Change>
 - Absolutely Deny <Rainy,Cold,Normal,Light,Warm,Same>
 - Pending
 - <Sunny,Warm,Normal,Light,Warm,Same>
 - <Sunny,Cold,Normal,Strong,Warm,Same>



Inductive Bias (归纳的偏差)

- Bias Vs. Unbiase
- The Futility (无用性) of Bias-Free Learning
 - Too large searching space
 - The convergence is impossible
 - Rational inference is impossible
- Inductive bias of CANDIDATE-ELIMINATION algorithm
 - The target concept *c* is contained in the given hypothesis space
 H.
 - Inductive System == Deductive System + *Inductive Bias*

Summary



- Concept learning can be cast as Searching through predefined hypotheses space.
- The *general-to-specific* partial ordering of hypotheses leads to efficient searching strategy, such as CANDIDATE-ELIMINATION algorithm.
- A practical concept learning methods must employ *inductive bias*. Otherwise, they can only classify the observed training examples.
- Version spaces and the CANDIDATE-ELIMINATION algorithm provide a useful *conceptual framework* for studying concept learning. However, their correctness rely on the noise-free training examples and the ability of provided hypotheses space to express the unknown target concepts.

EnjoySport revisit



• Given:

- Instances X: Possible days, each described by the attributes
 - Sky (Sunny, Cloudy, and Rainy)
 - Temp (Warm and Cold)
 - Humidity (Normal and High)
 - Wind (Strong and Weak)
 - Water (Warm and Cool)
 - Forecast (Same and Change)
- Hypotheses *H*: Each hypothesis is described by a *conjunction* of constraints. These constraints may be "?" (any value), "0" (no value), or a specific value.

设想编程调试时候的情景

• Determine:

• A hypothesis *h* in **H** such that h(x) = c(x) for all x in **X**.



Thank you