

# Computer Graphics 2016

## 8. Hidden Surface Elimination

Hongxin Zhang

State Key Lab of CAD&CG, Zhejiang University

2016-11-21

# Visual Realism

---

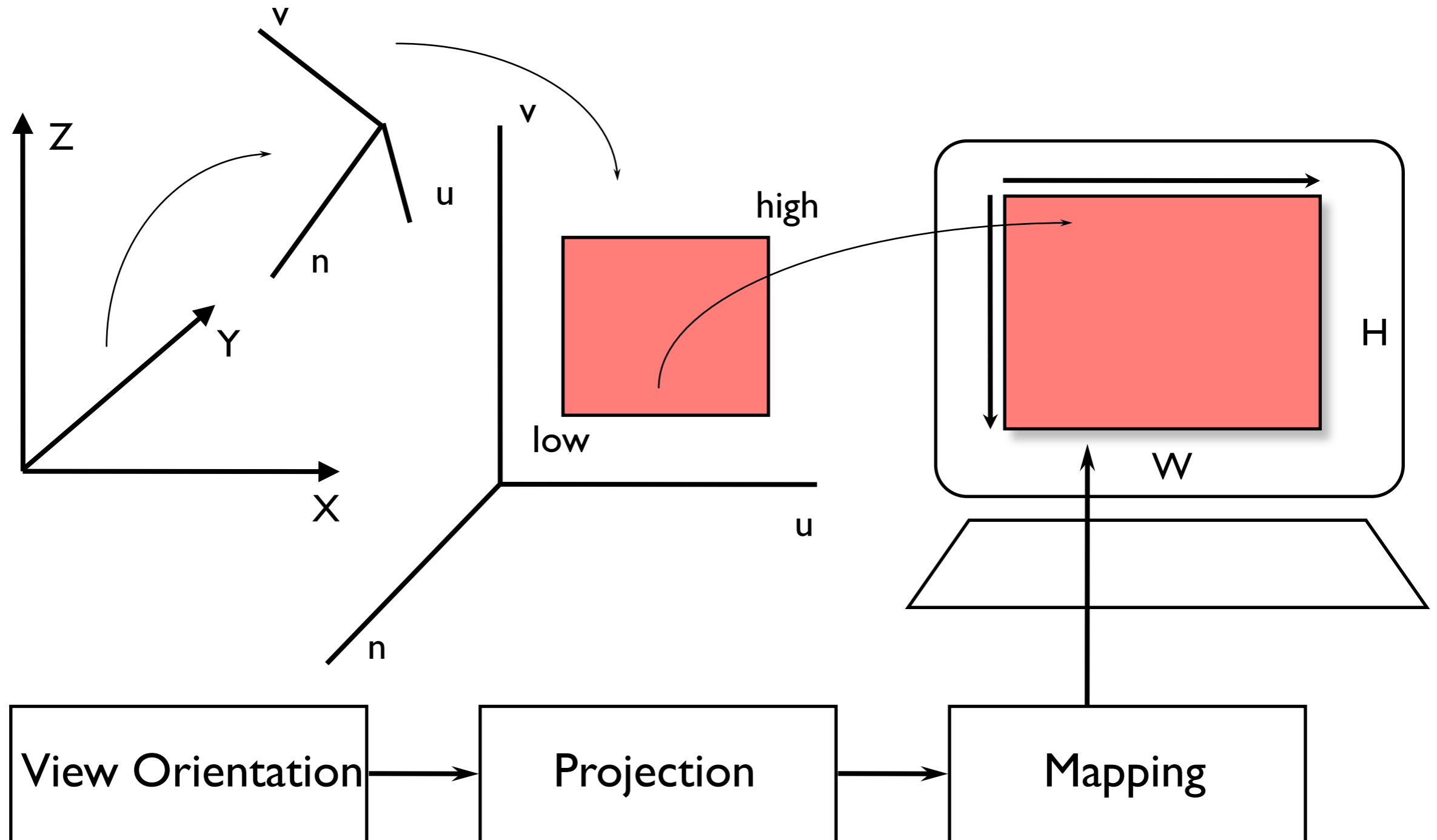
- Achieved by correct rendering of :
  - View (perspective)
  - Field of view (Clip outside the window)
  - Omit hidden parts
  - Surface details like texture
  - Light effects on surfaces like continuous shading, shadows, and caustics.
  - Volumetric effects like transparency and translucency through participating media like water, steam, smoke, ...
  - Dynamic effects like movement, elasticity, ...

# OpenGL functions

---

- glEnable / glDisable (GL\_CULL\_FACE);
- glCullFace(mode)
  
- glutInitDisplayMode( ... | GLUT\_DEPTH )
- glEnable(GL\_DEPTH\_TEST)
- glEnable(GL\_FOG) glFog\*()

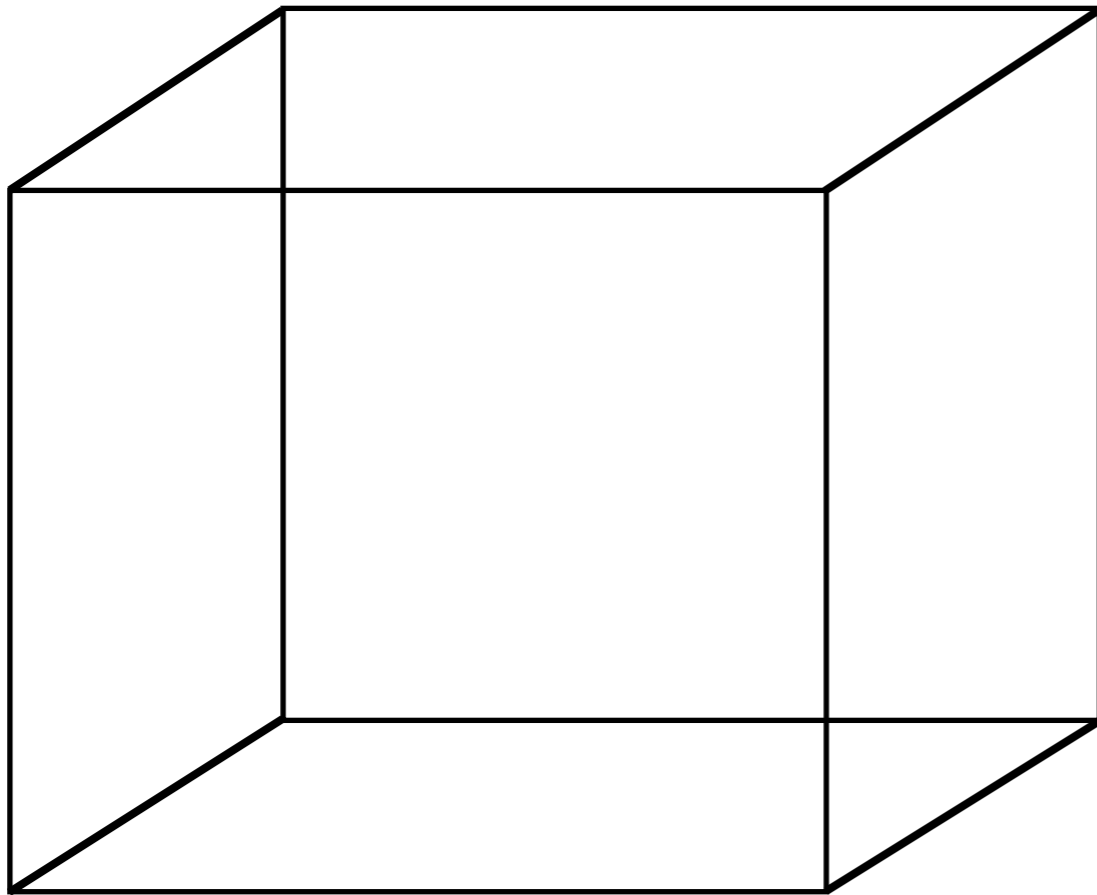
# Viewing Pipeline Review



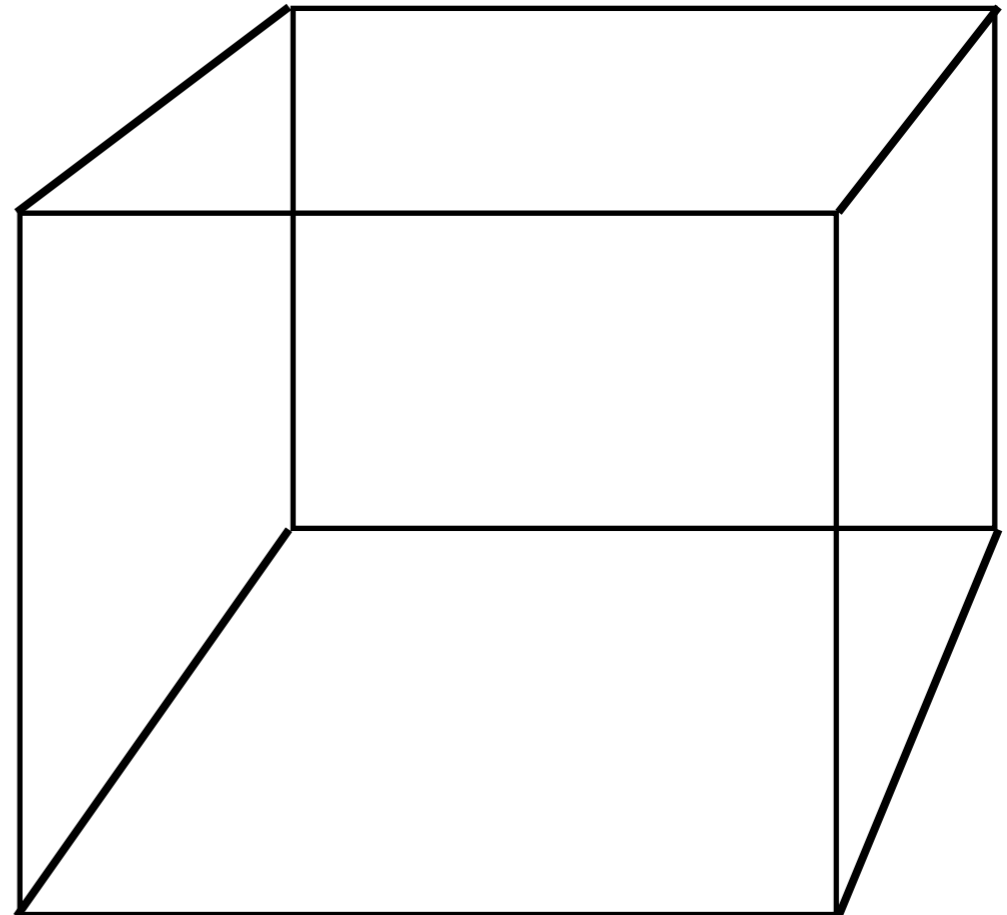
# Projection

---

Orthographic

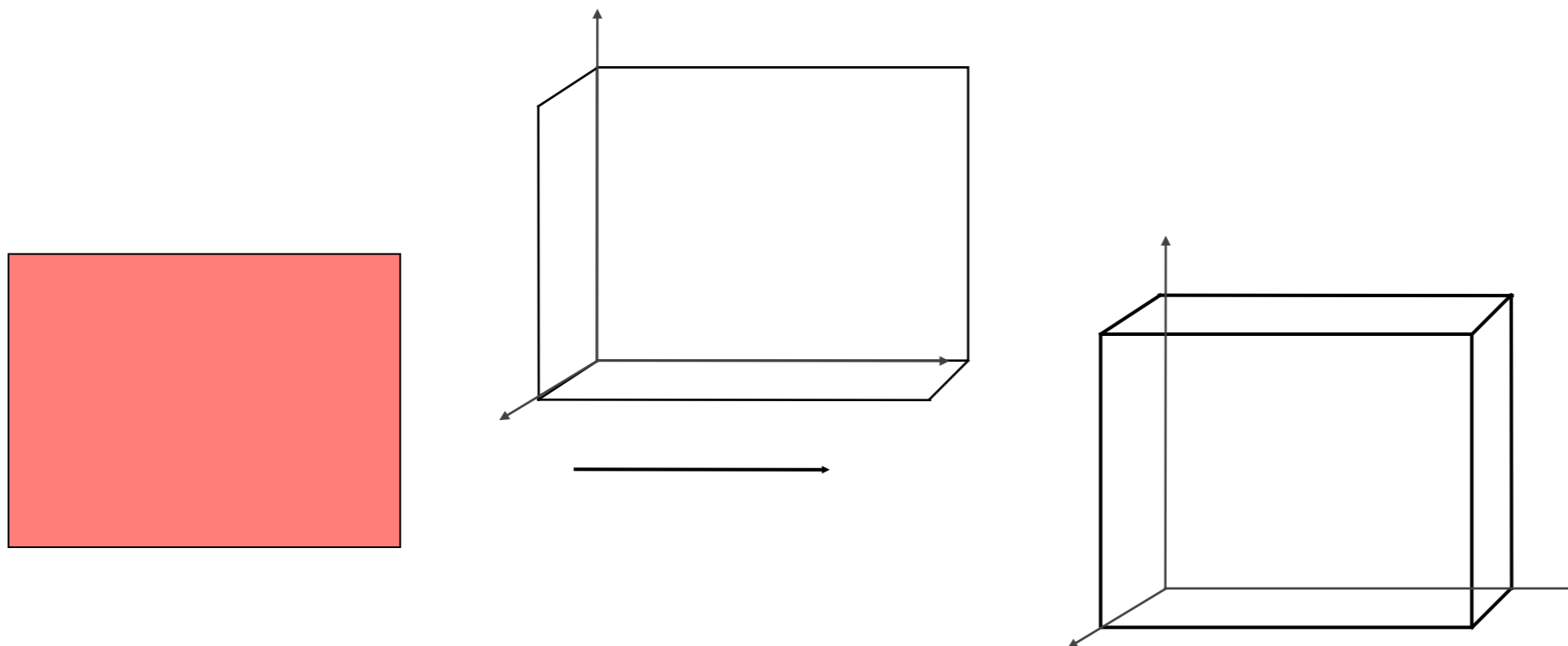


Perspective



# Visible Line Drawing

---



# Visible Surface Determination

---

- Goal
  - Given: a set of 3D objects and Viewing specification,
  - Determine: those parts of the objects that are **visible** when viewed along the direction of projection
- Or, equivalently, elimination of hidden parts (hidden lines and surfaces)
- Visible parts will be drawn/shown with proper colors and shades

# HLHSR Algorithms

---

- Two Fundamental Approach
  - Object space algorithm
    - a.k.a. **Object Precision** ~
    - hidden line remove
  - Image space algorithm
    - a.k.a. **Image Precision** ~
    - z-buffer



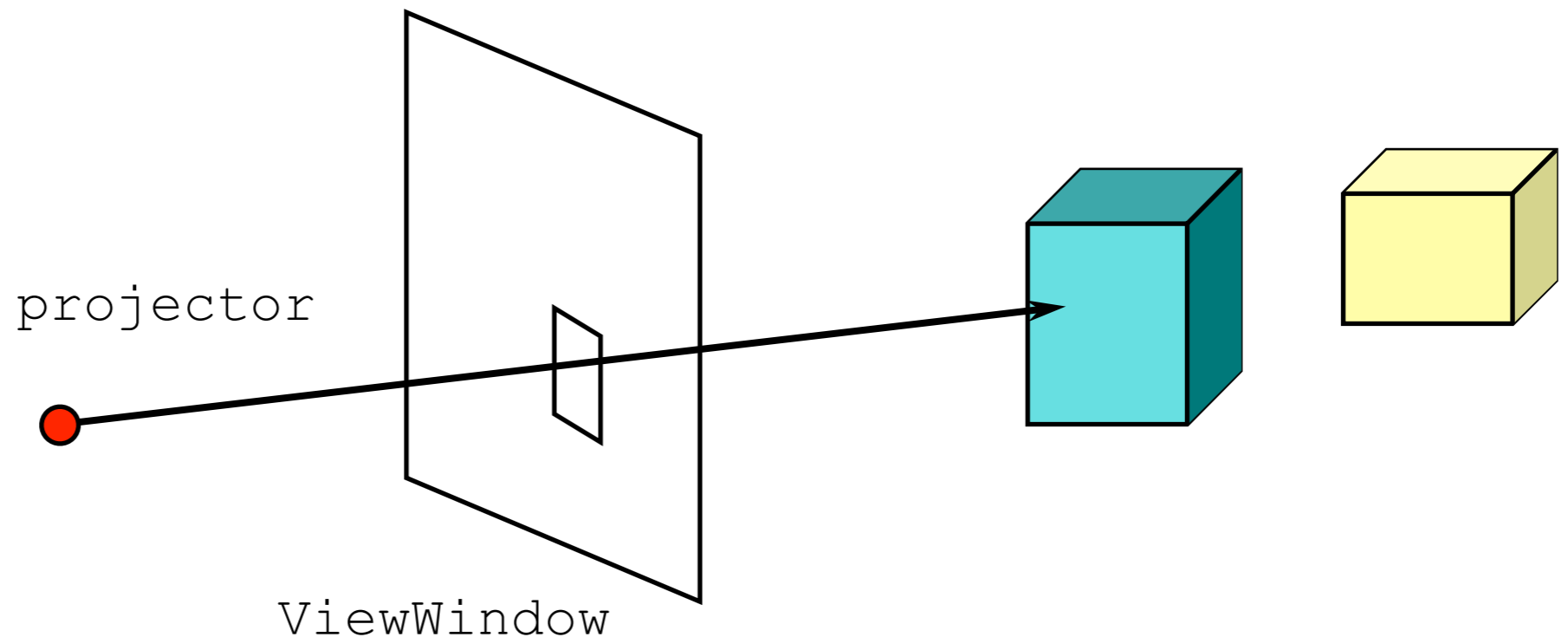
# Object Precision Algorithm

---

```
foreach (object in the world) {  
    determine those parts of the object whose view is  
        unobstructed by other parts of it or any other object;  
    draw those parts in the appropriate color;  
}
```

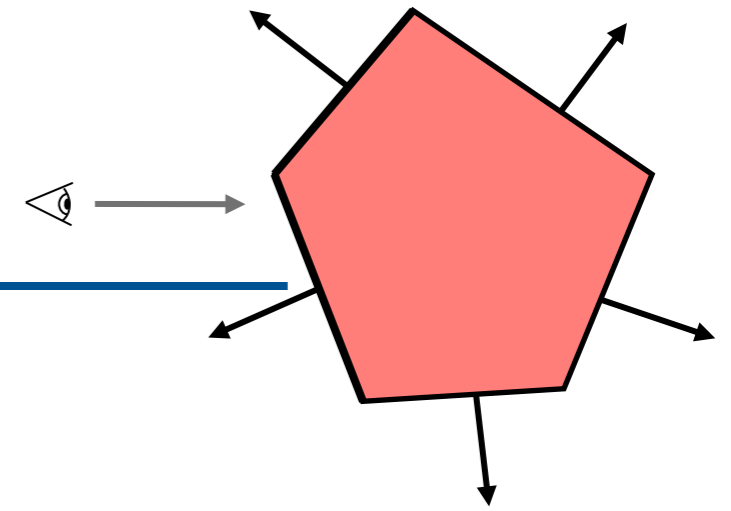
# Image Precision Algorithms

```
foreach (pixel in the image) {  
    determine the object closest to the viewer that is pierced  
    by the projector through the pixel;  
    draw the pixel in the appropriate color;  
}
```



# Back-face Culling

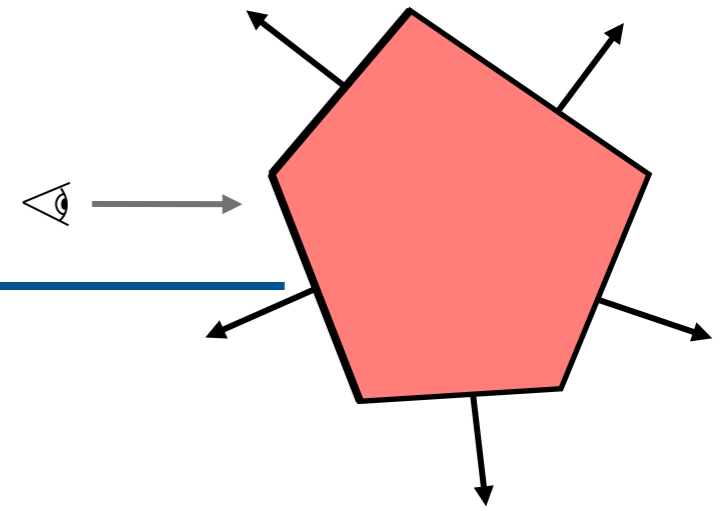
---



- In a closed polygonal surface
  - i.e. the surface of a polyhedral volume or a solid polyhedron
  - The faces whose outward normals point away from the viewer are not visible
  - Such back-facing faces can be eliminated from further processing
- Elimination of back-faces is called back-face culling

# Back-Face Culling

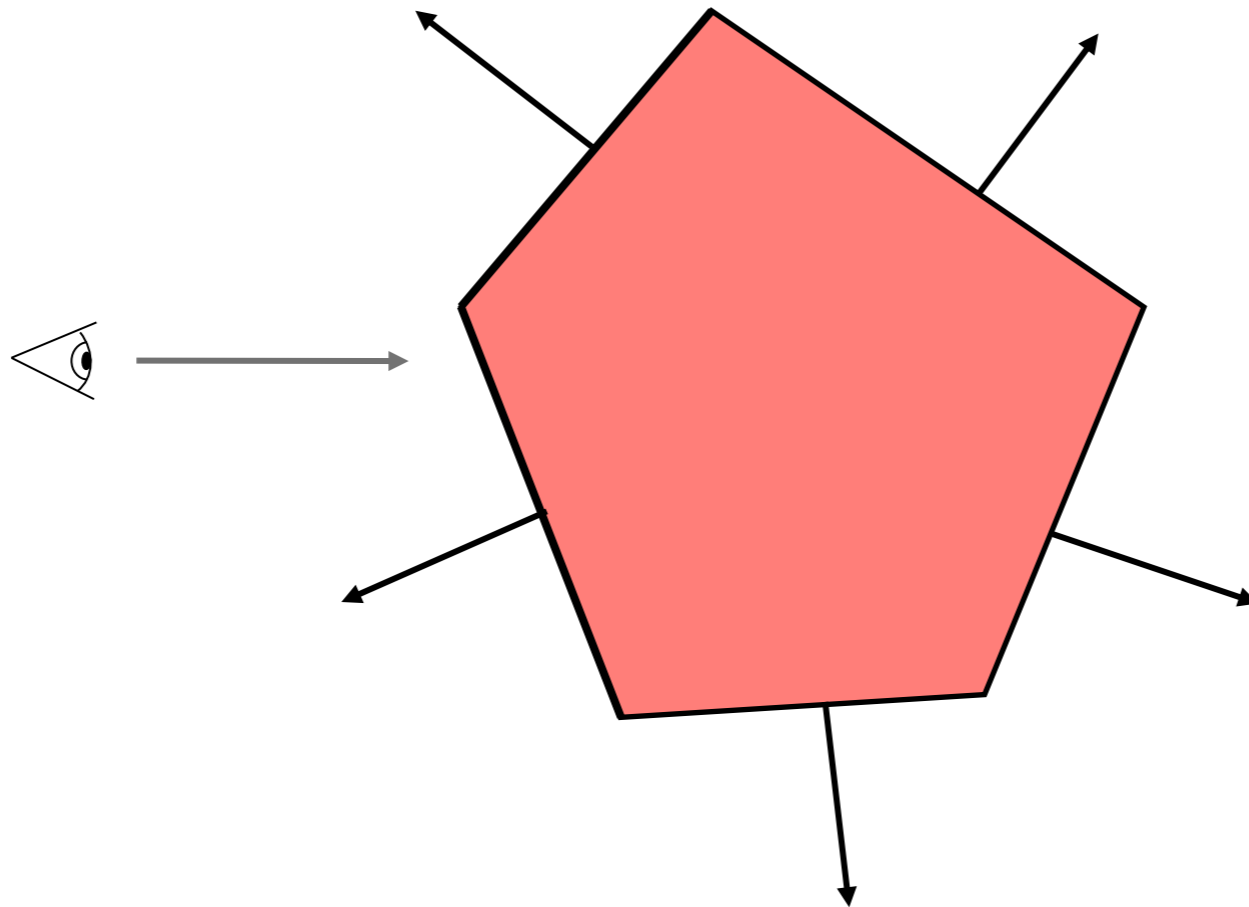
---



- Back Face:
  - Part of the object surface facing away from the eye.
  - i.e. surface whose normal points away from the eye position.

# Back-Face Culling

---



## Algorithm:

1. Find angle between the eye-vector & normal to face.
2. If between  $0$  to  $90^\circ$ , discard the face.

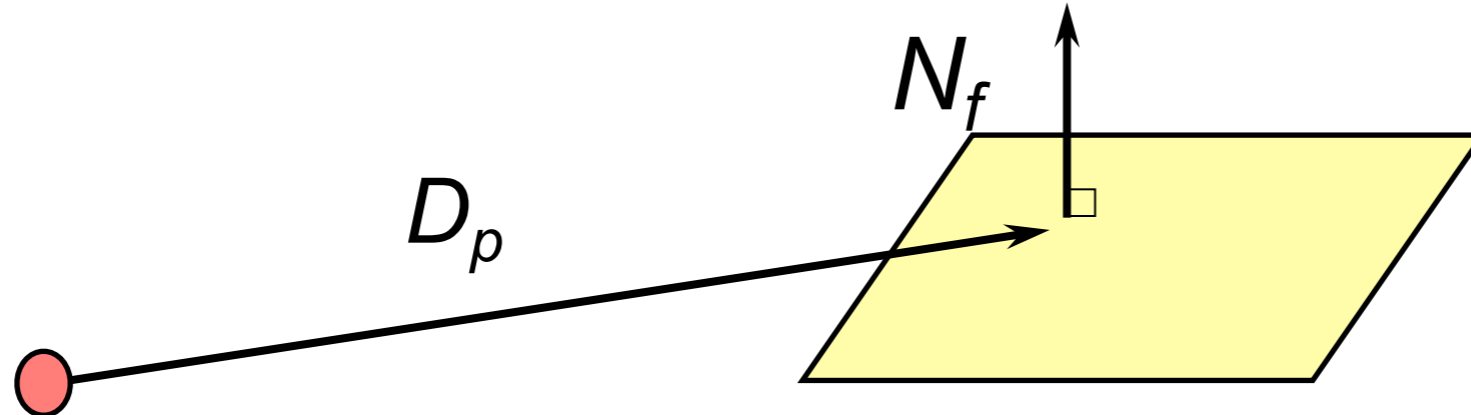
# Back-face Culling

---

- Determination of back-faces

A polygonal face with outward surface normal  $N_f$  is a back-face if  $N_f \cdot D_p > 0$

where  $D_p$  is the direction of projection



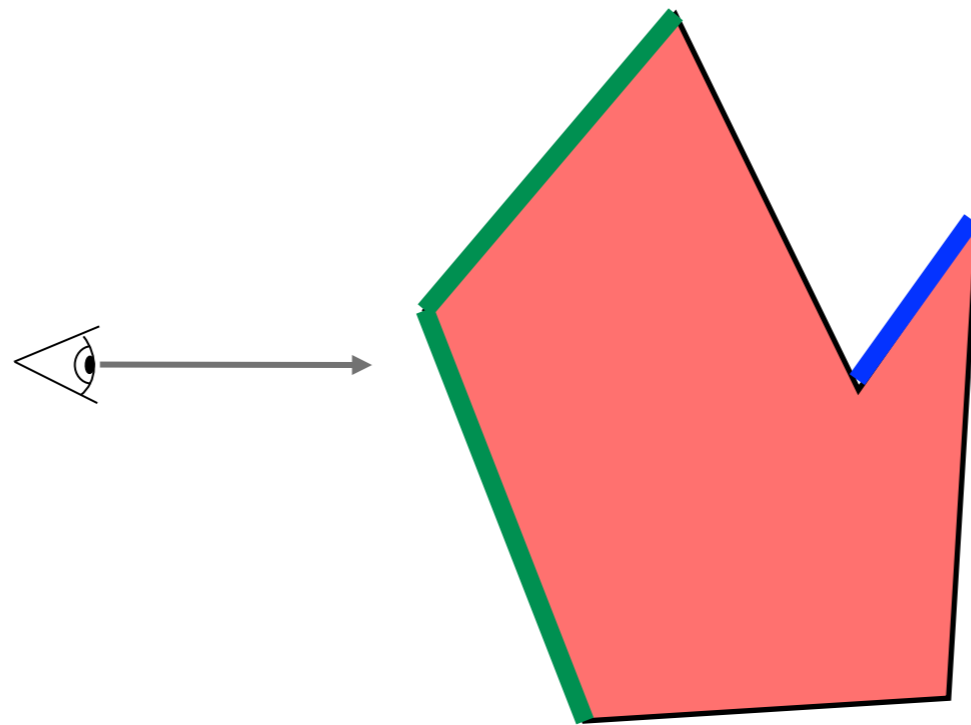
What happens when the projectors are along Z axis, i.e.,  $(0,0,1)$  is the view direction.

Let  $N_f = (n_x, n_y, n_z)$ , the dot product now equals  $n_z$ . If this is +ve, then this is a back-face!

# Back-Face Culling

---

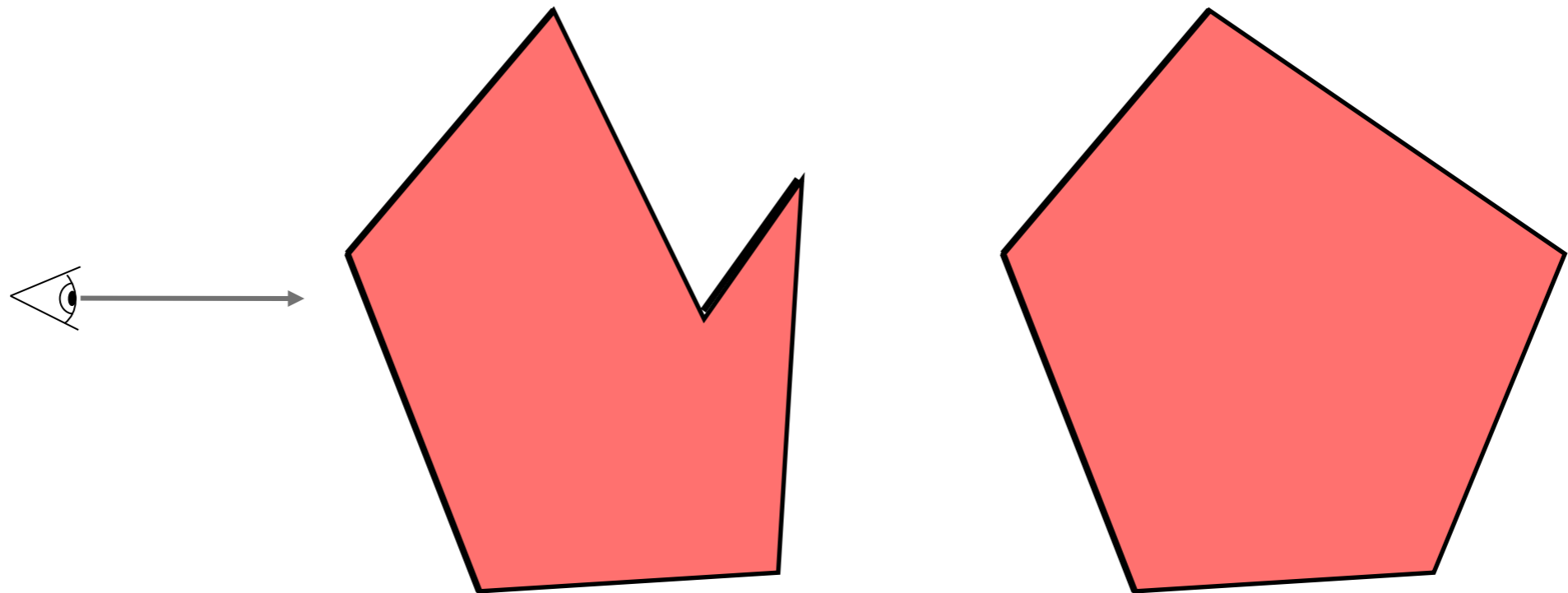
Back-face culling does not solve all visibility problems



# Back-Face Culling

---

Back-face culling does not solve all visibility problems

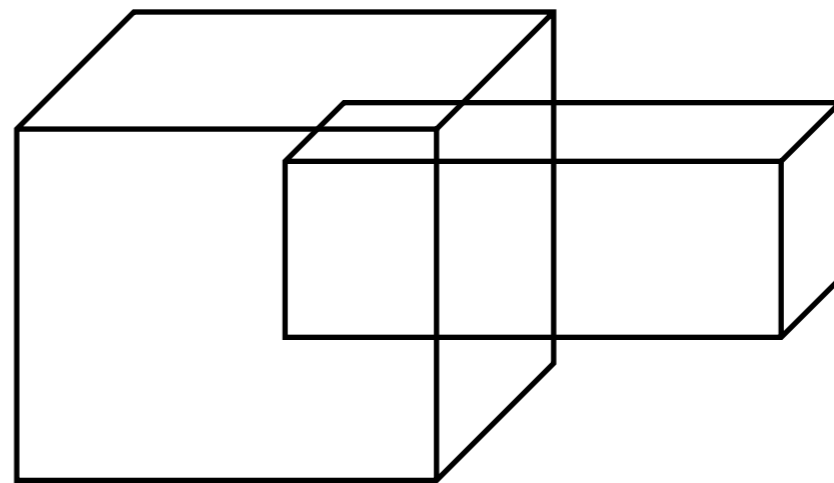
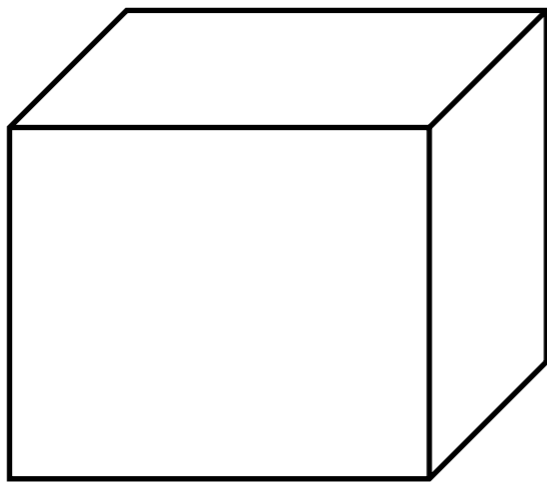




# Back-face Culling

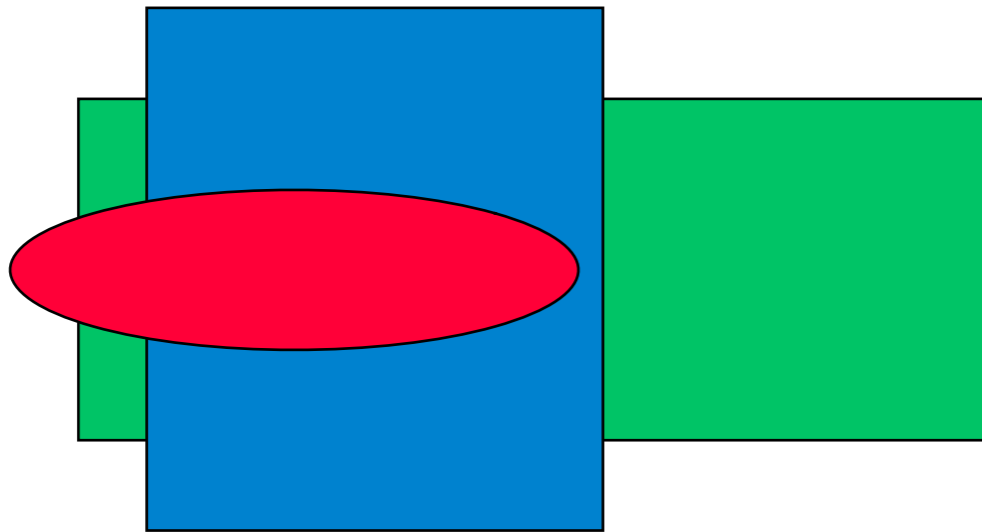
---

If the scene consists of a **single convex closed** polygonal surface then back-face culling is equivalent to HLHSR

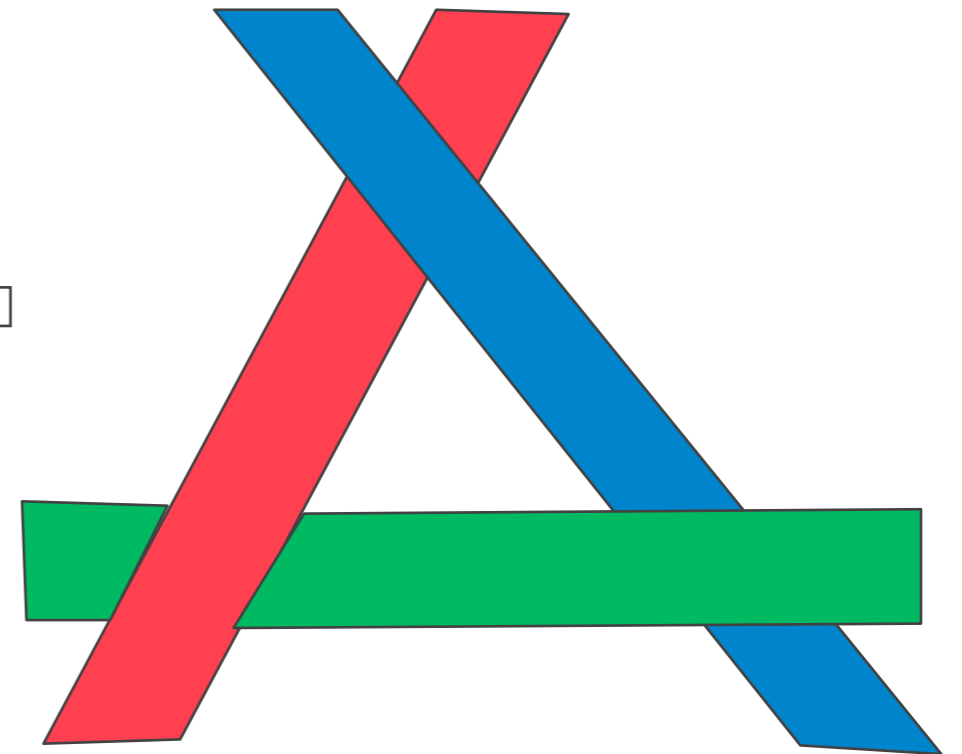
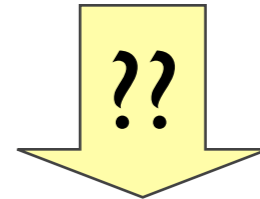


# Hidden Surface Removal

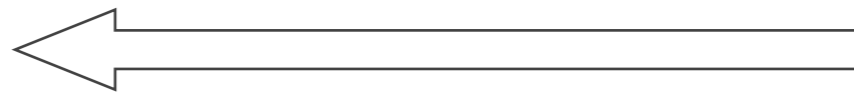
---



Painter's Algorithm  
From back to Front



**Area Sorting**

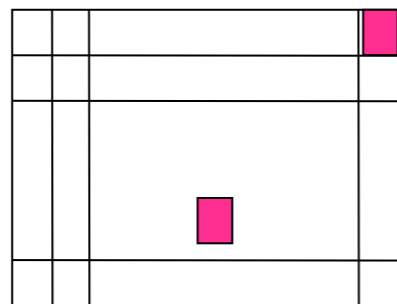


**Clipping**

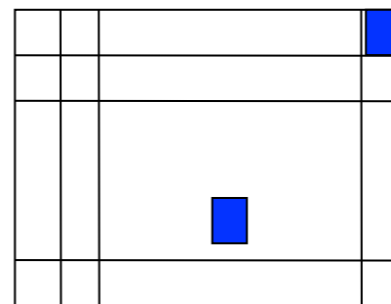
# Z-Buffer Algorithm

---

- Image precision algorithm
  - Apart from a frame buffer F in which **color** values are stored,
  - it also needs a z-buffer, of the same size as the frame buffer, to store **depth** (z) values



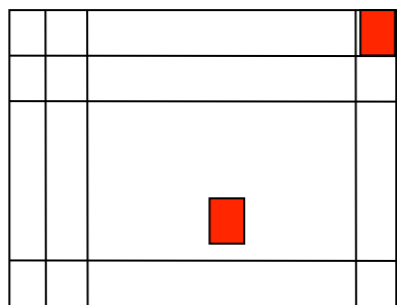
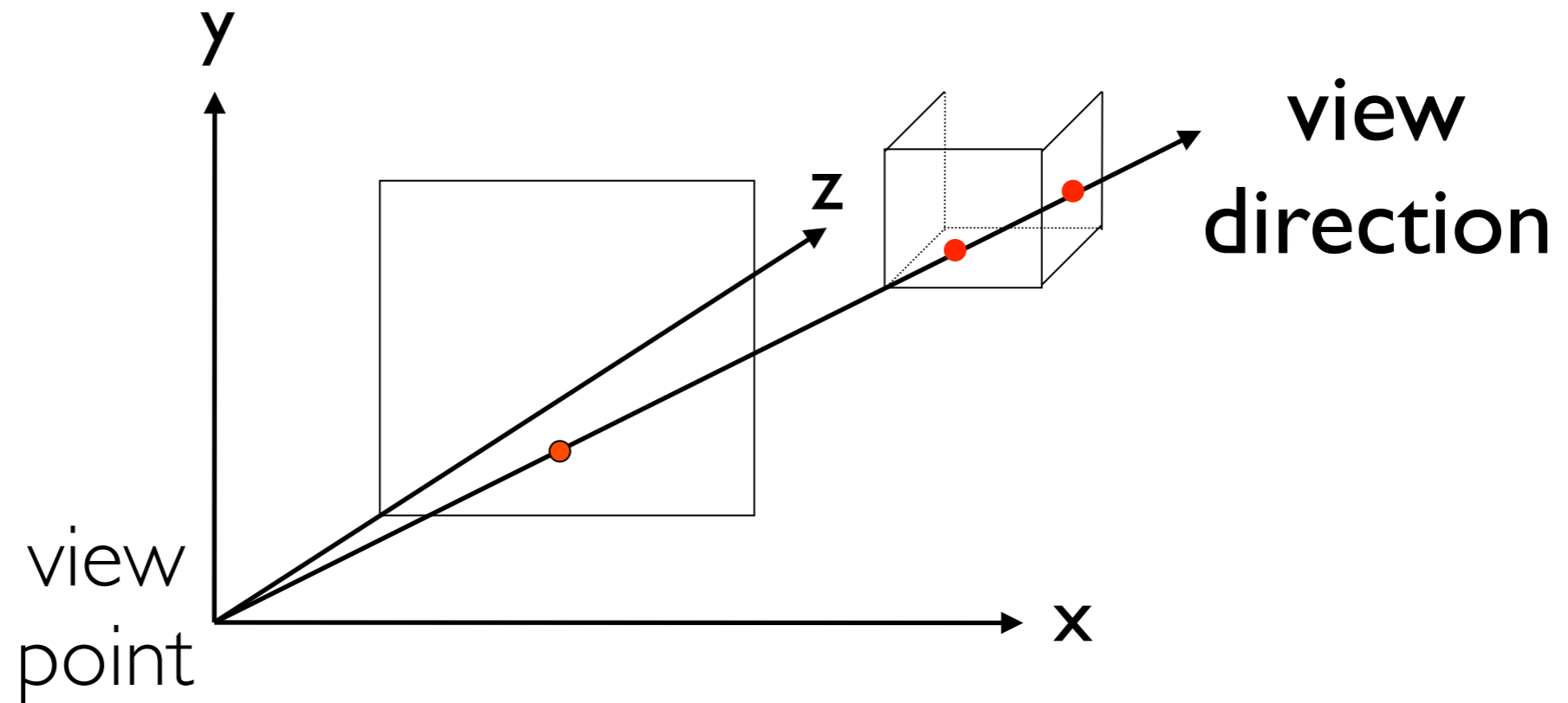
F-Buffer



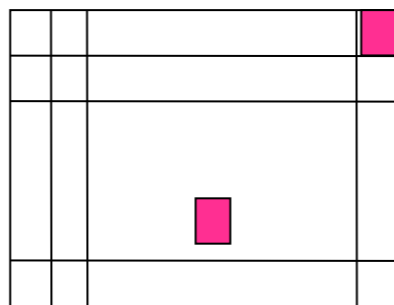
Z-Buffer

A.K.A. depth-buffer method

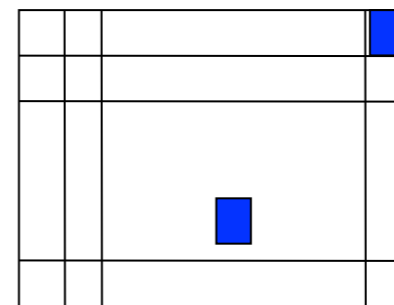
# Z-Buffer



Screen



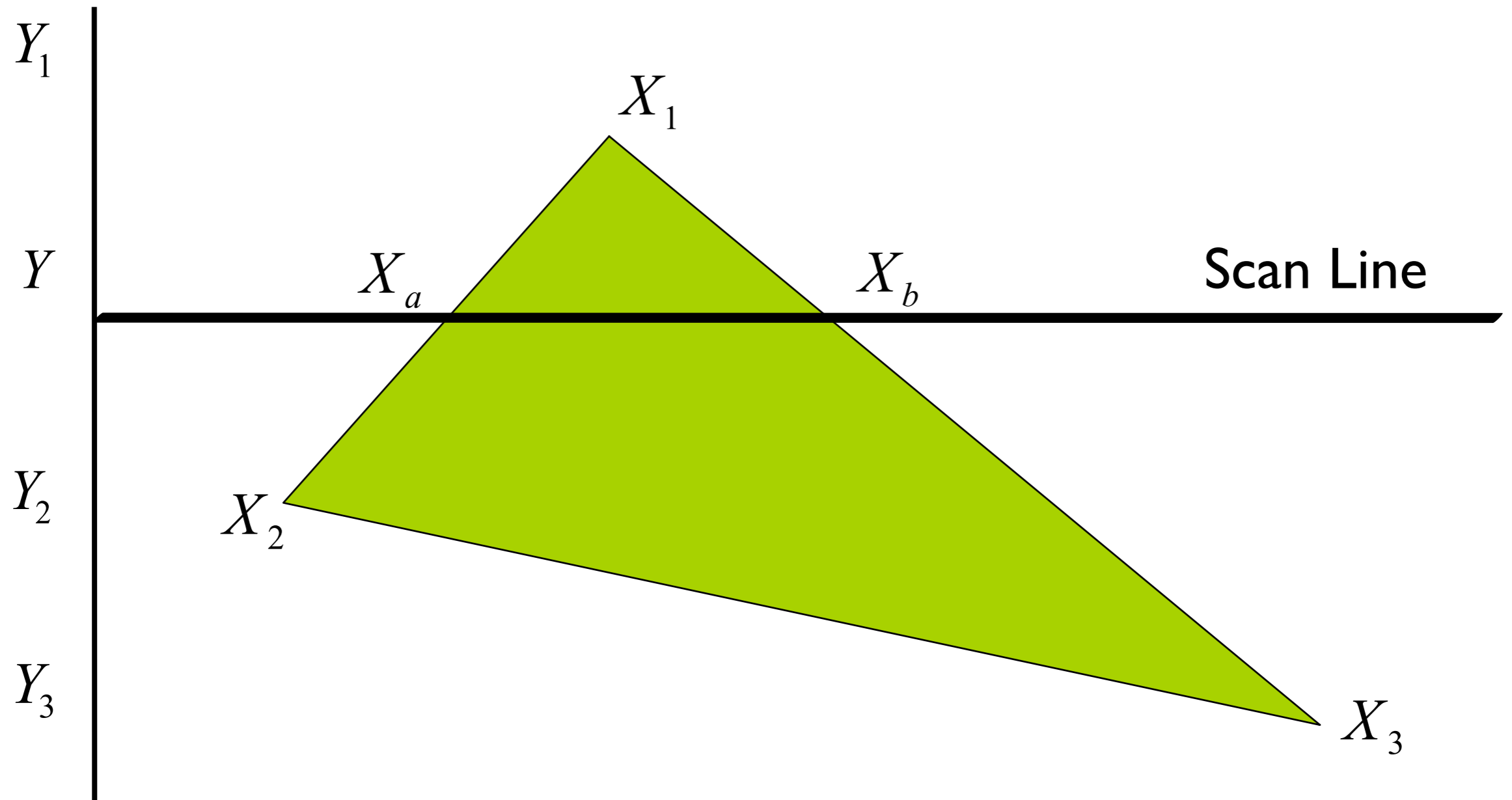
F-Buffer



Z-Buffer

# Polygon Scan Conversion

---

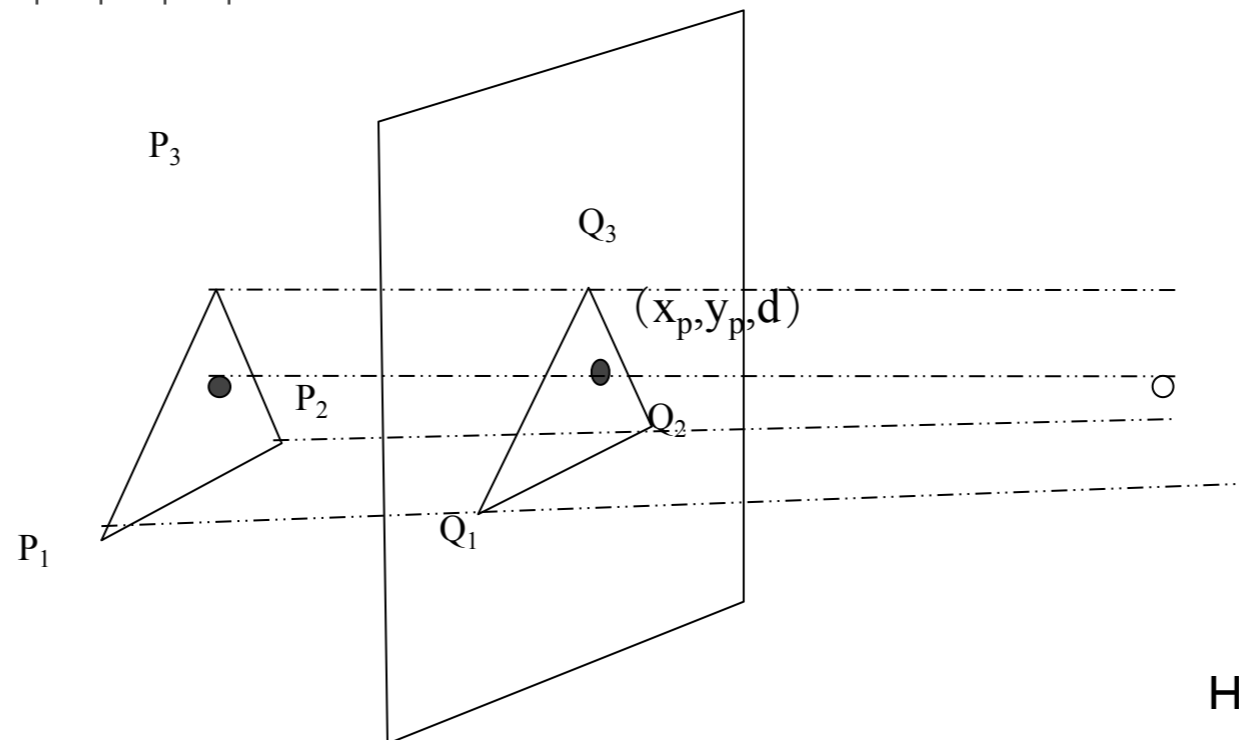
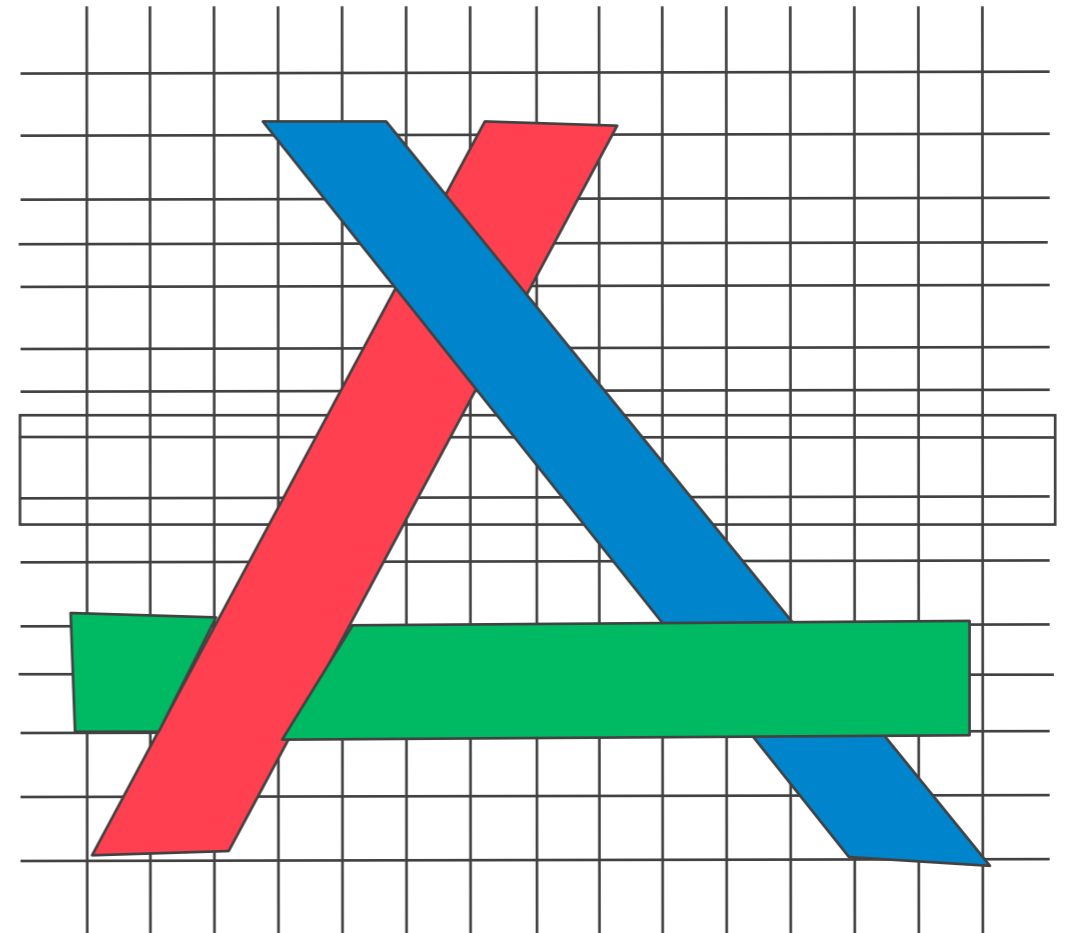
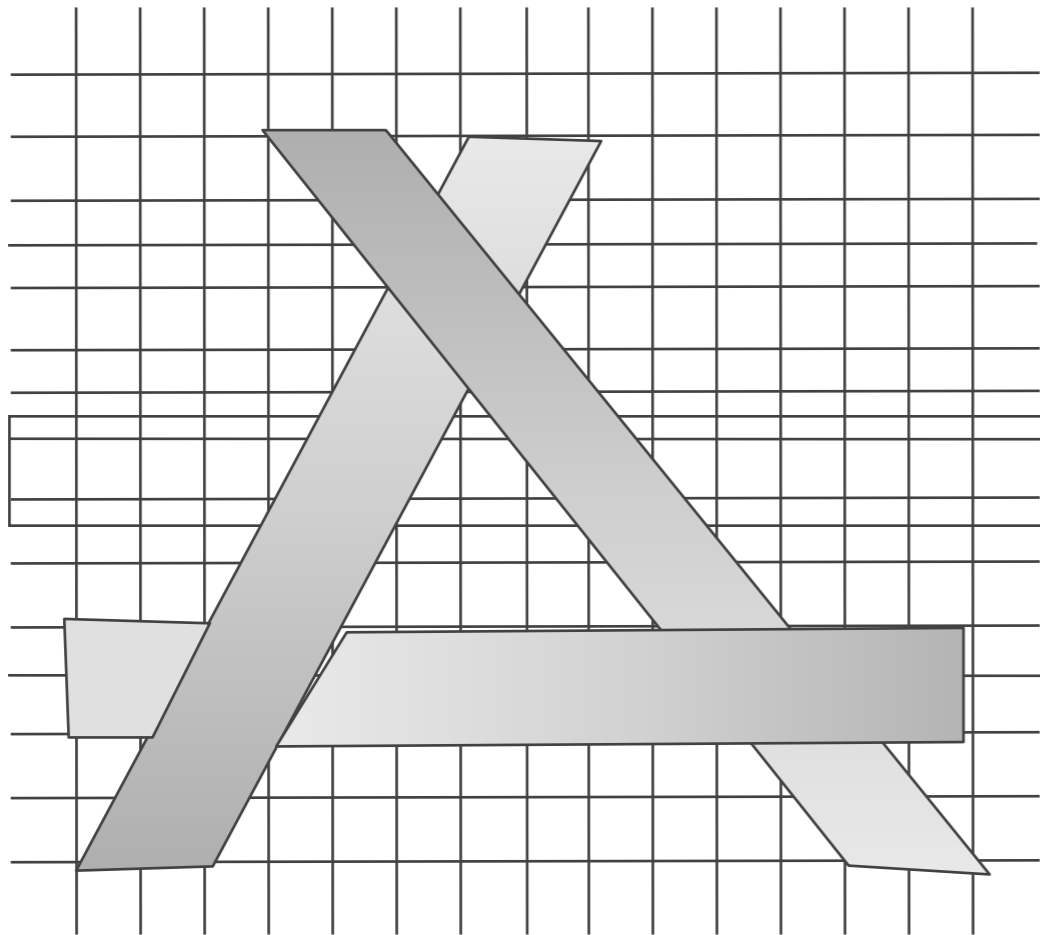


# Z-Buffer Pseudo-code

---

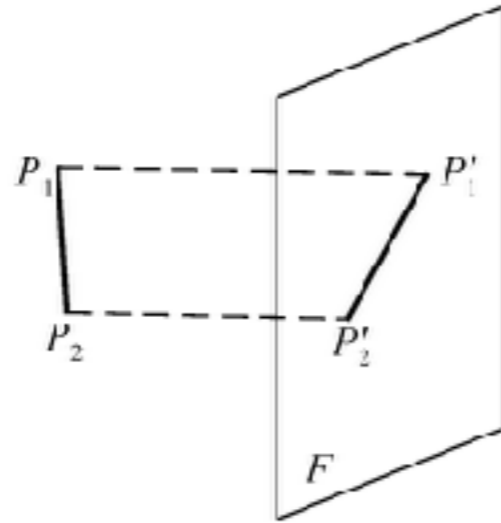
- for ( j=0; j<SCREEN\_HEIGHT; j++ )
  - for ( i=0; i<SCREEN\_WIDTH; i++ ) {
    - WriteToFrameBuffer(i, j, BackgroundColor);
    - WriteToZBuffer(i, j, MAX);
  - }
- for ( each polygon )
  - for ( each pixel in polygon's projection ) {
    - **z = polygon's z value at (i, j) ;**
    - if ( z < ReadFromZBuffer(i, j) ) {
      - WriteToFrameBuffer(i, j, polygon's color at (i, j));
      - WriteToZBuffer(i, j, z);
    - }
  - }

# Z-buffer

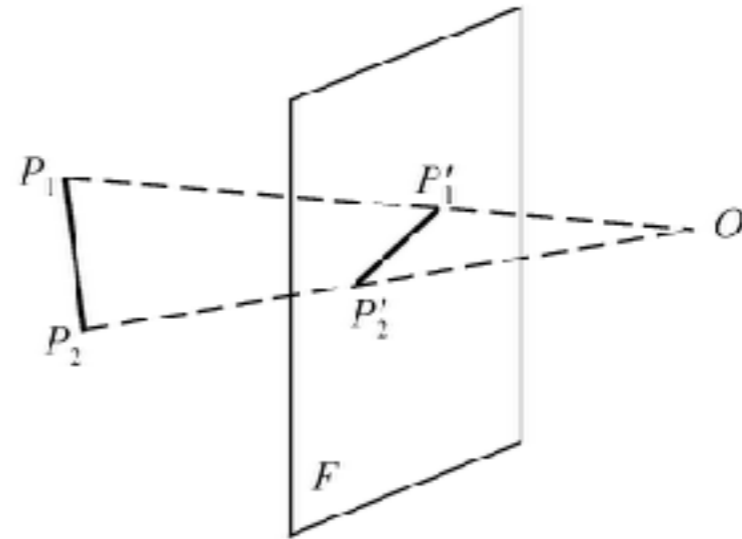


# Z-buffer

**Project:**



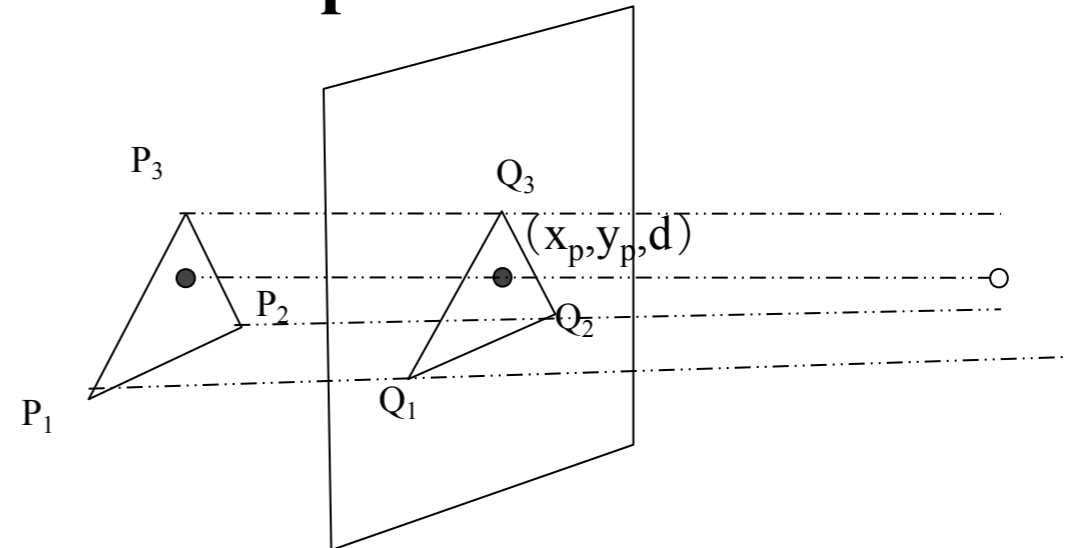
**Orthographic**



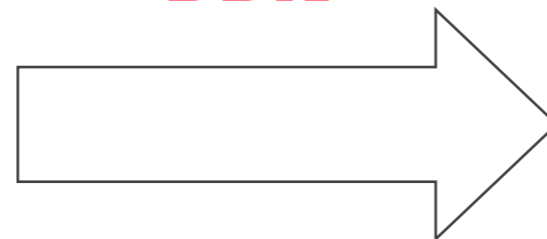
**Perspective**

**Calculate the z of the point**

$$Ax + By + Cz + D = 0$$



**DDA**

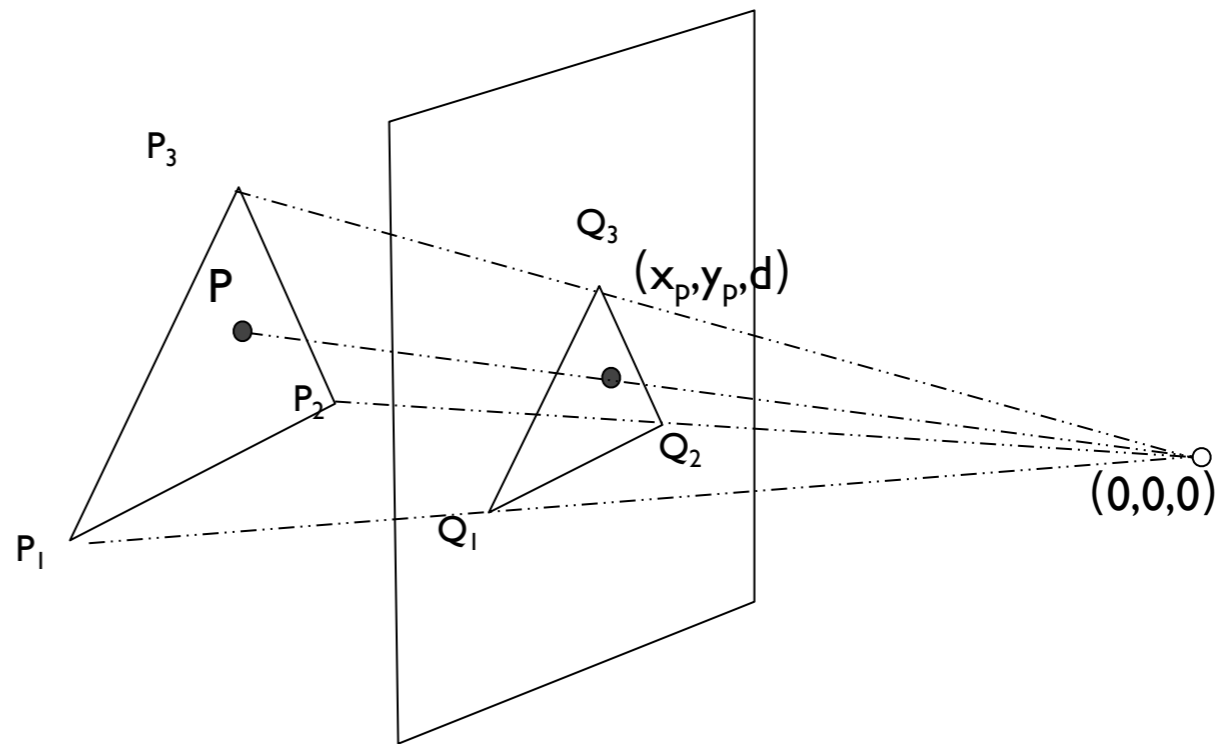
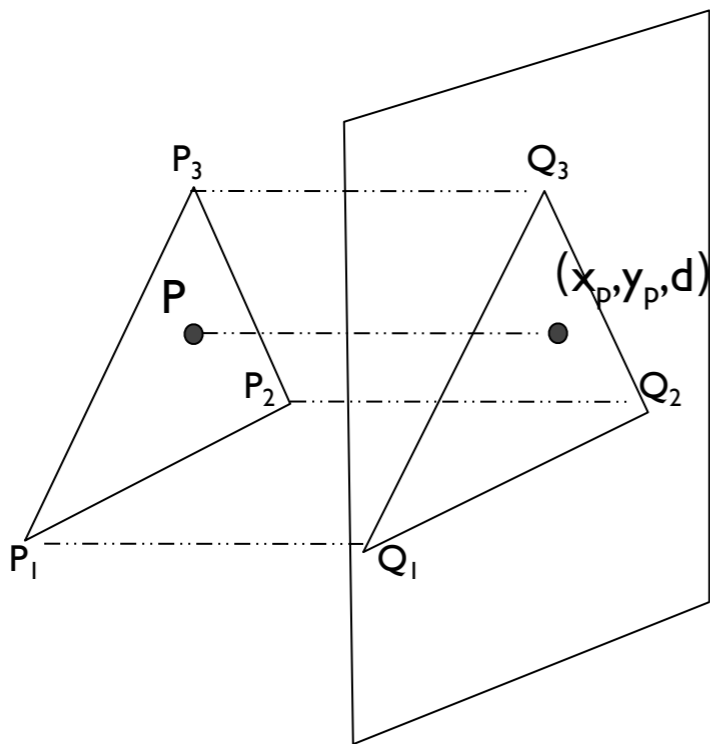


**x++, y++**

**z+??**

**Question: how?**





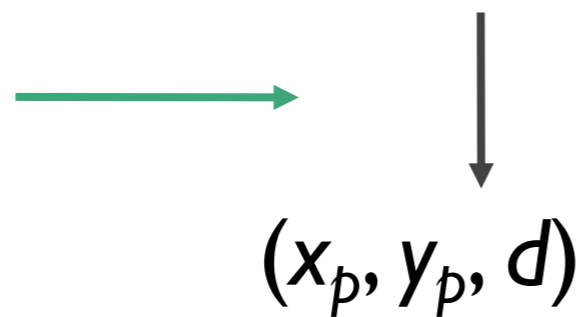
$$Ax + By + Cz + D = 0$$

$$(x, y, z) \rightarrow (x, y, d)$$

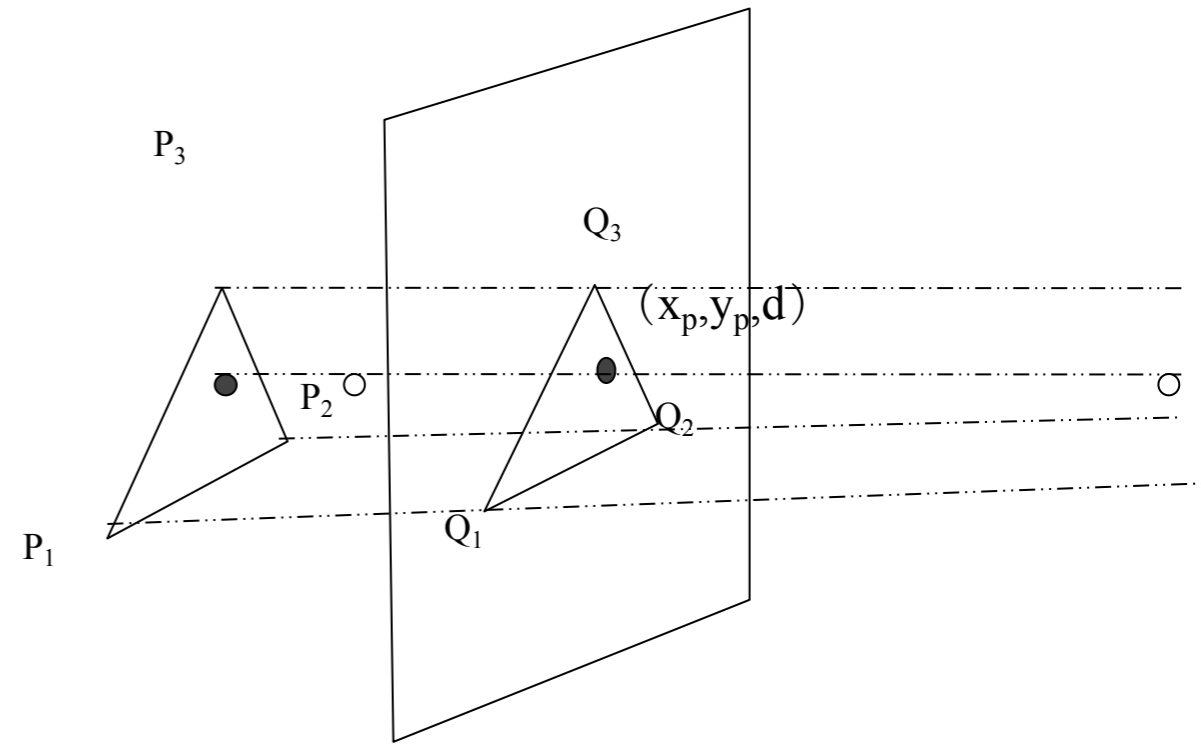
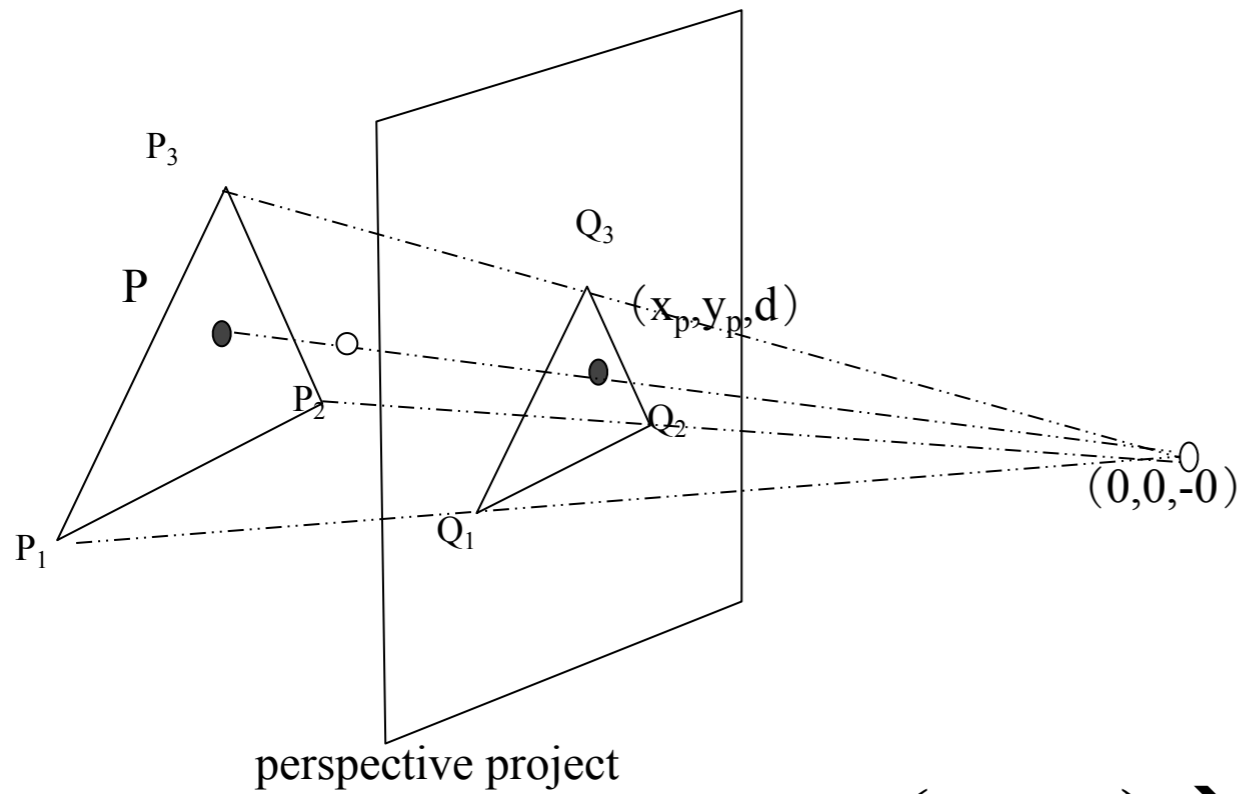
$$(x, y, z) \rightarrow (x_p, y_p, d)$$

$$(x, y, z) \rightarrow (x_p, y_p, z)$$

Orthographic  
project



$$\left\{ \begin{array}{l} \frac{x_p}{x} = \frac{d}{z} \\ \frac{y_p}{y} = \frac{d}{z} \end{array} \right.$$



$$(x,y,z) \rightarrow (x_p, y_p, z)$$

Perspective Transformation

Orthographic project



$$(x_p, y_p, d)$$

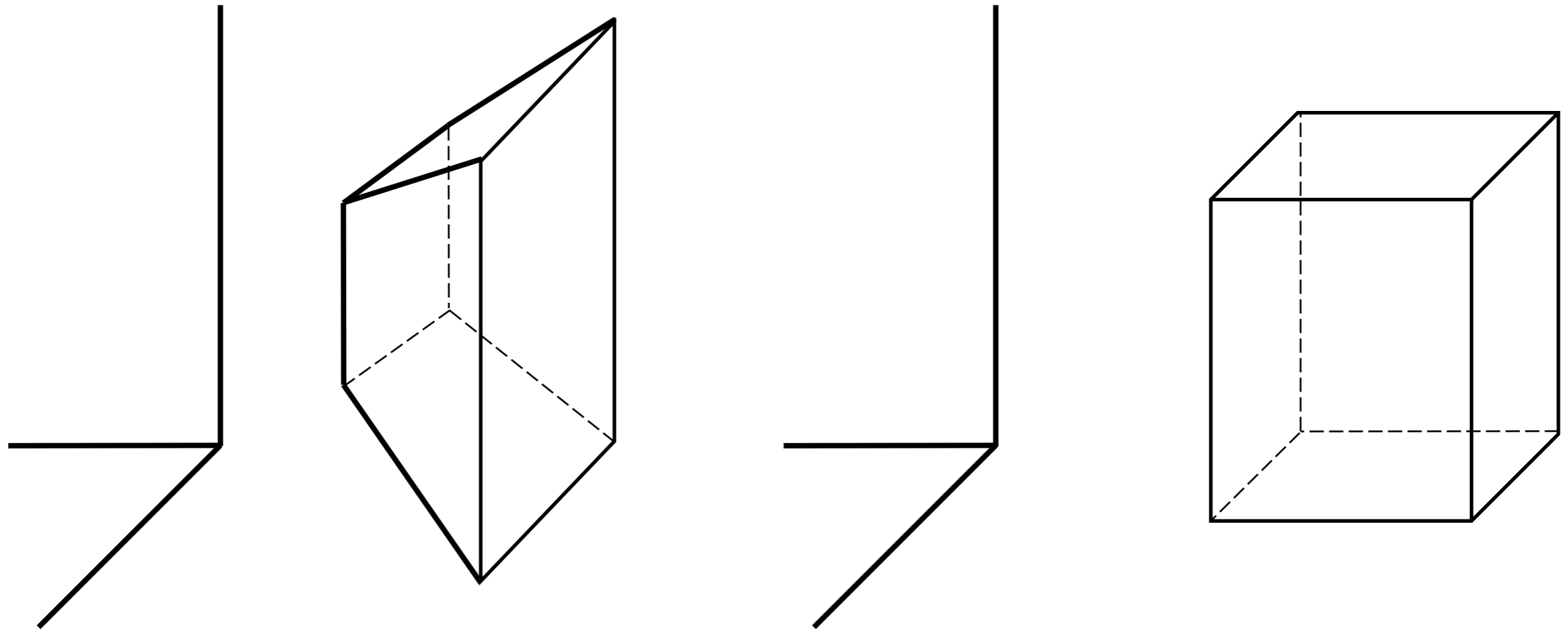
# Perspective Transformation...

---

- We need to apply a perspective transformation to the view volume and transform it into a rectangular parallel-piped one
- This makes the final 3D view volume of a perspective view the same as that of a parallel view, just before projection

# Perspective Transformation

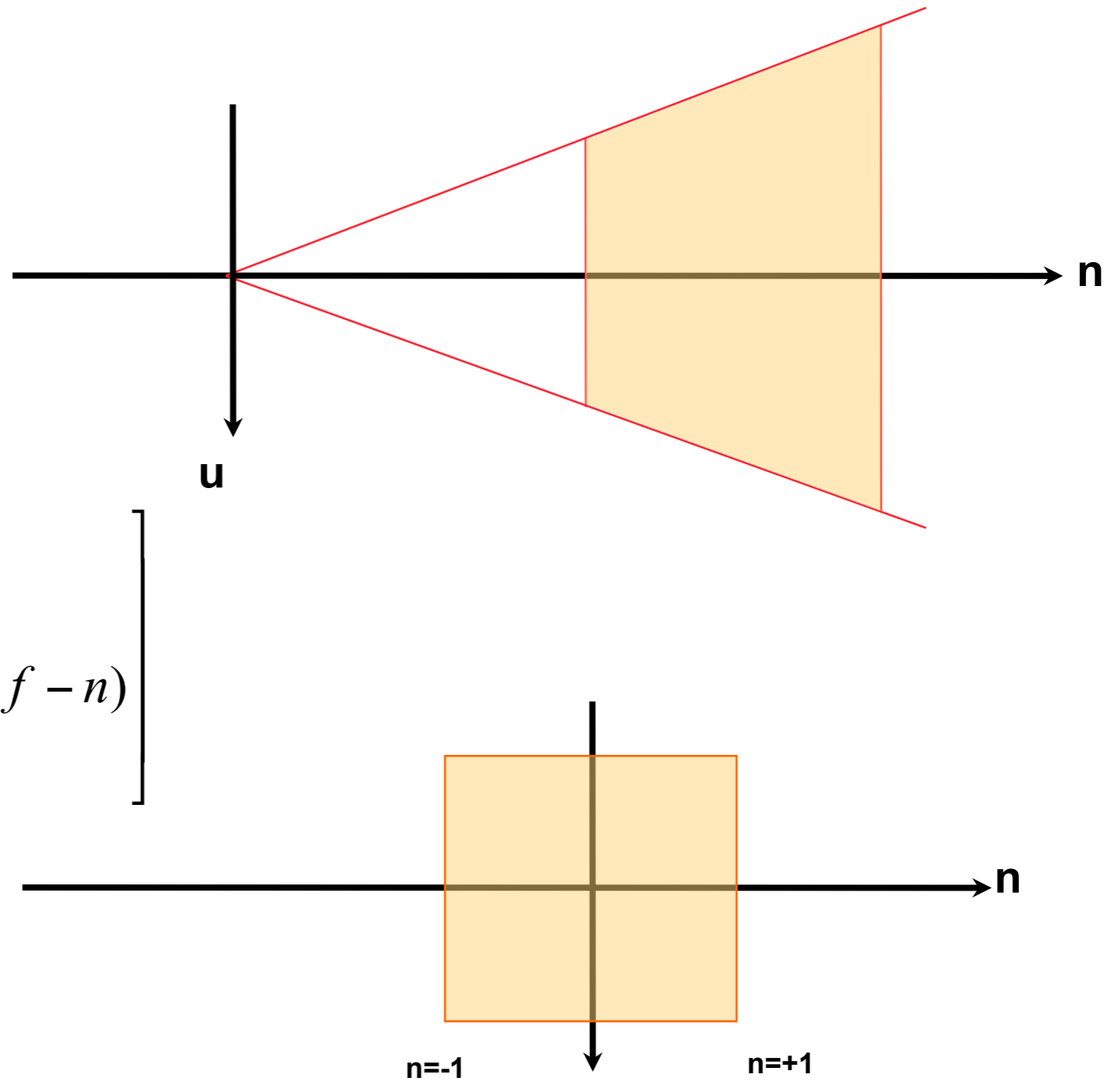
---



- A perspective transformation preserves relative depth, straight lines and planes

# Perspective Transformation

$$\mathbf{M}_P = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & (f+n)/(f-n) & -2f*n/(f-n) \\ 0 & 0 & 1 & 0 \end{bmatrix}$$



# A-buffer

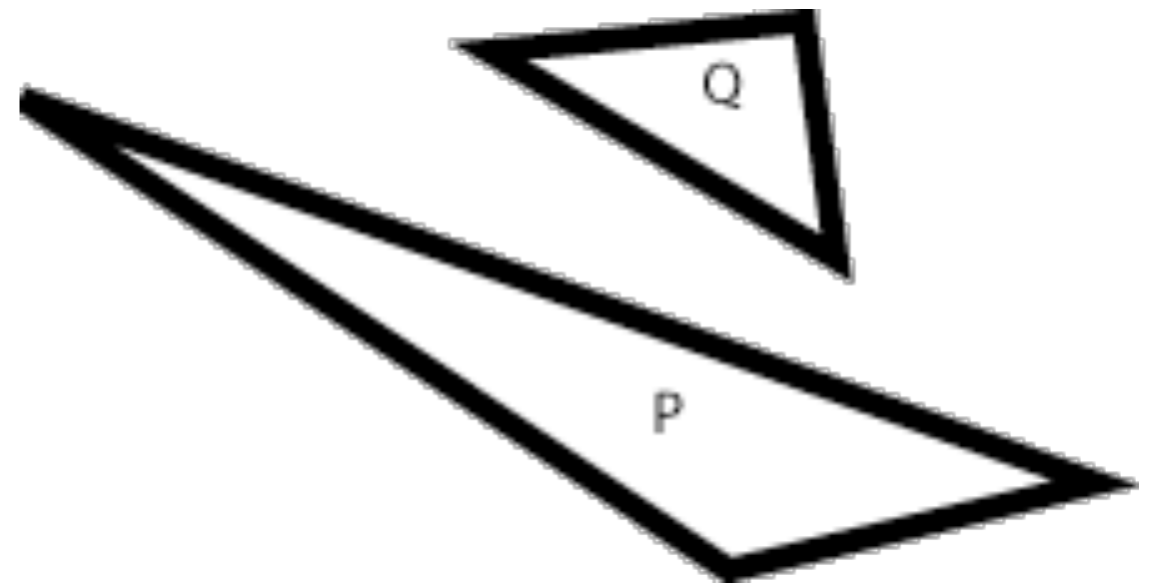
---

- Accumulation buffer
  - used in Lucasfilm REYES
  - not only store depth but also other data
  - support transparent surfaces

# Depth-sorting

---

- space-image space hybrid method
  - space or image space:
    - sort surface by depth
  - image space:
    - do scan conversion from deepest surfaces



# Binary Space Partitioning Trees

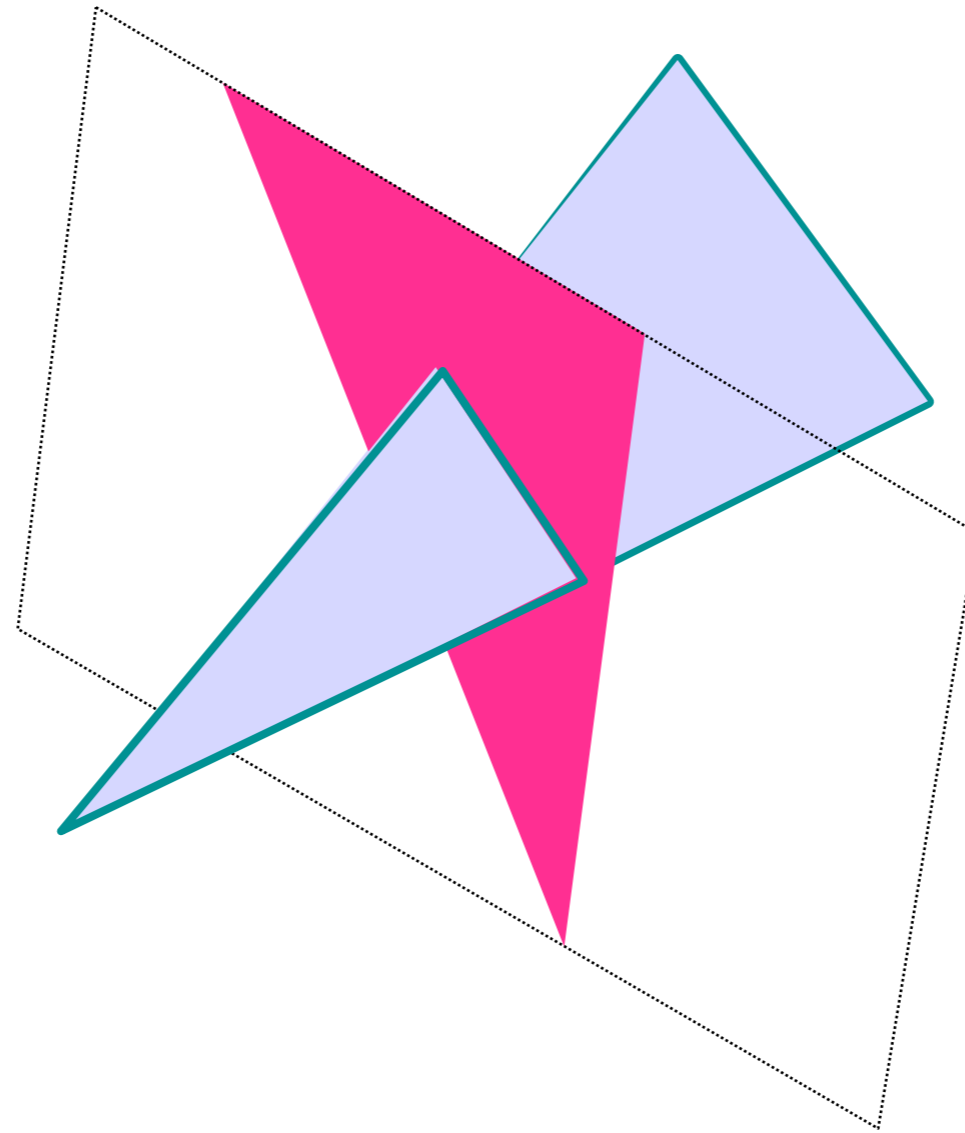
---

- BSP Tree
  - Very efficient for a static group of 3D polygons as seen from an arbitrary viewpoint
  - Correct order for Painter's algorithm is determined by a suitable traversal of the binary tree of polygons



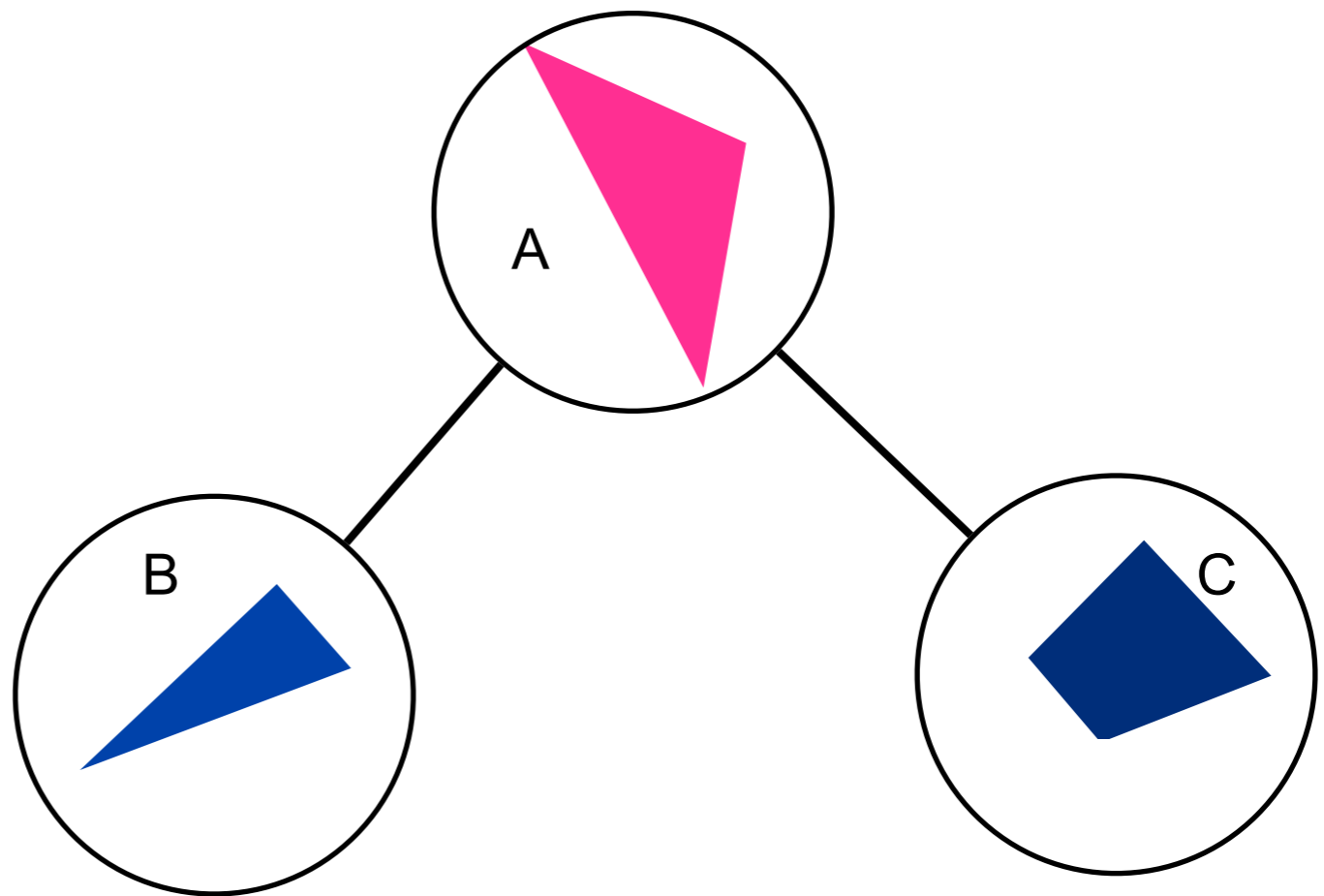
# BSP Tree

---



# BSP Tree

---



# BSP Tree

---

## Draw BSP Tree

```
function draw(bsptree tree, point eye)
```

```
if tree.empty then
```

```
    return
```

```
if  $f_{\text{tree.root}}(\textit{eye}) < 0$ 
```

```
    draw (tree.right)
```

```
    rasterize(tree.root)
```

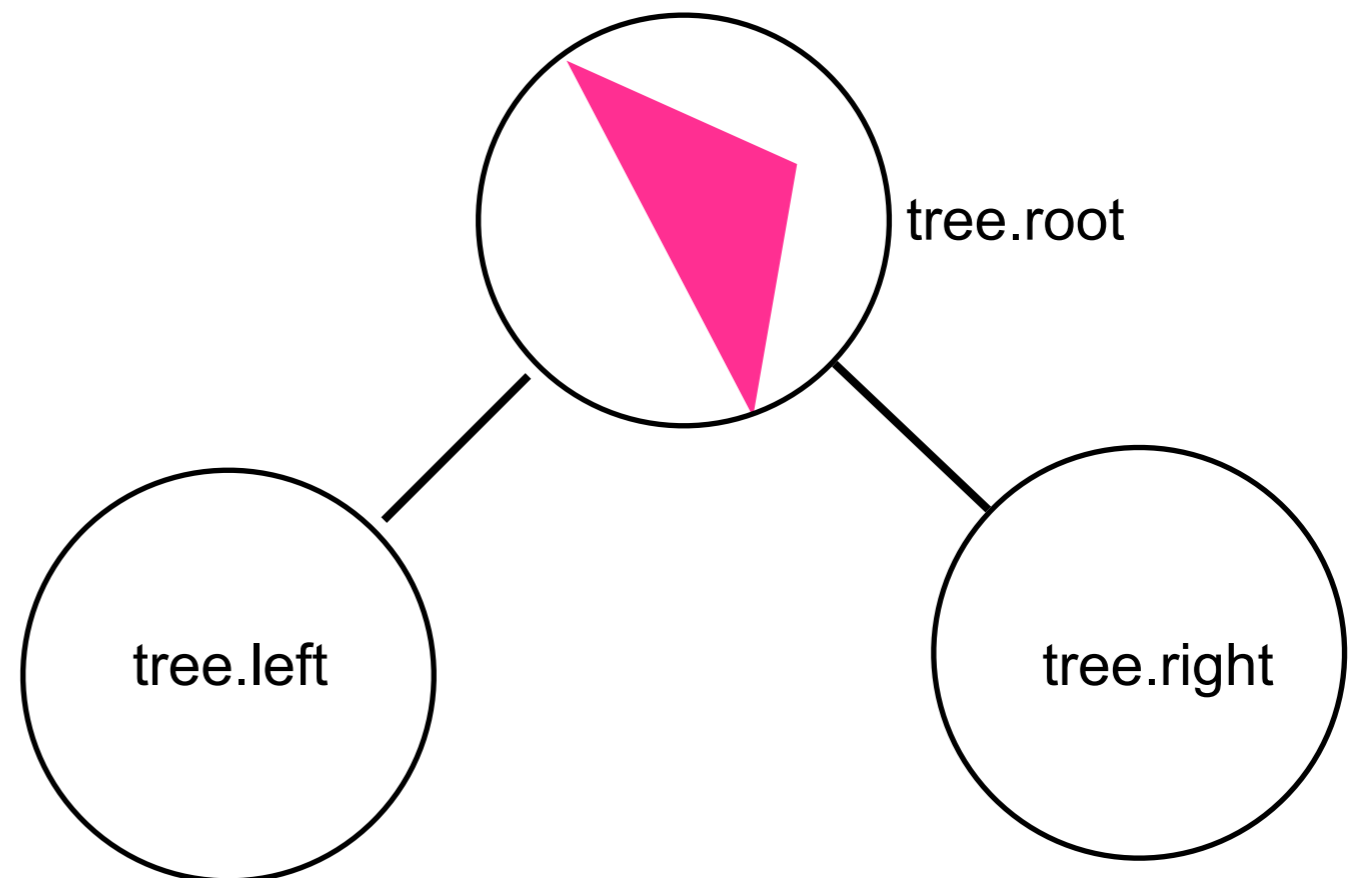
```
    draw(tree.left)
```

```
else
```

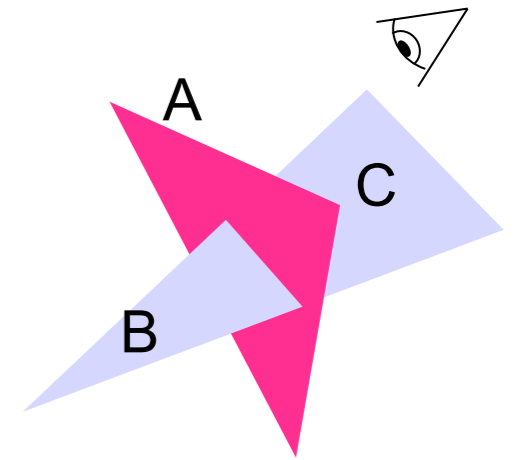
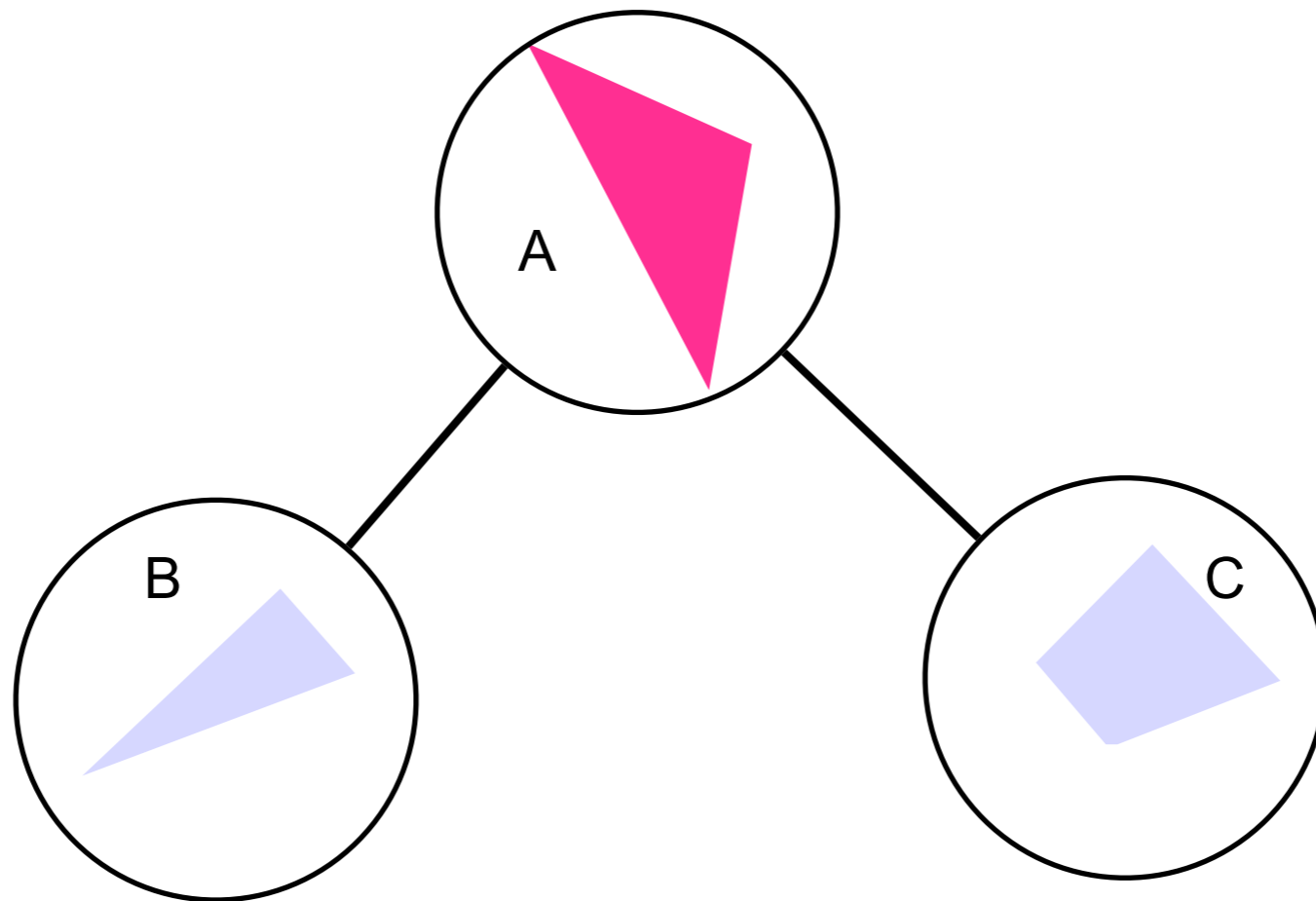
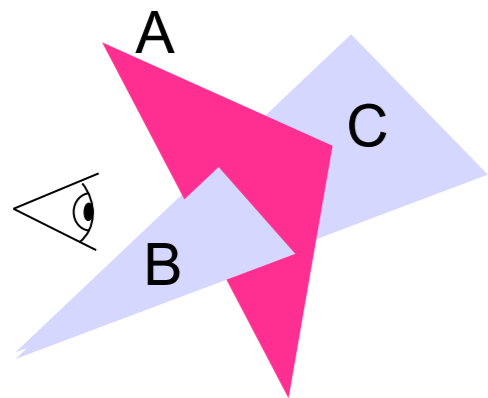
```
    draw (tree.left)
```

```
    rasterize(tree.root)
```

```
    draw(tree.right)
```



# BSP Tree



rasterize(C)  
rasterize(A)  
rasterize(B)

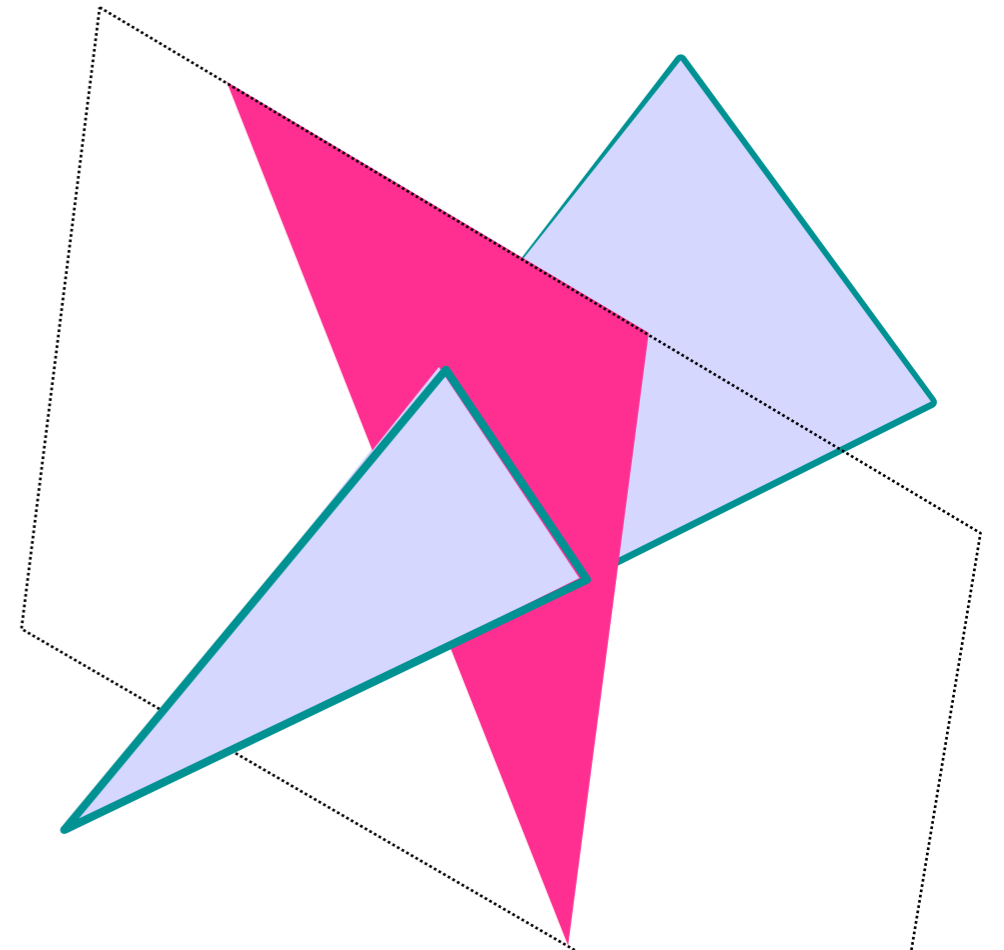
rasterize(B)  
rasterize(A)  
rasterize(C)

# BSP Tree

---

- Code works for any view
- Tree can be pre-computed
- Requires evaluation of

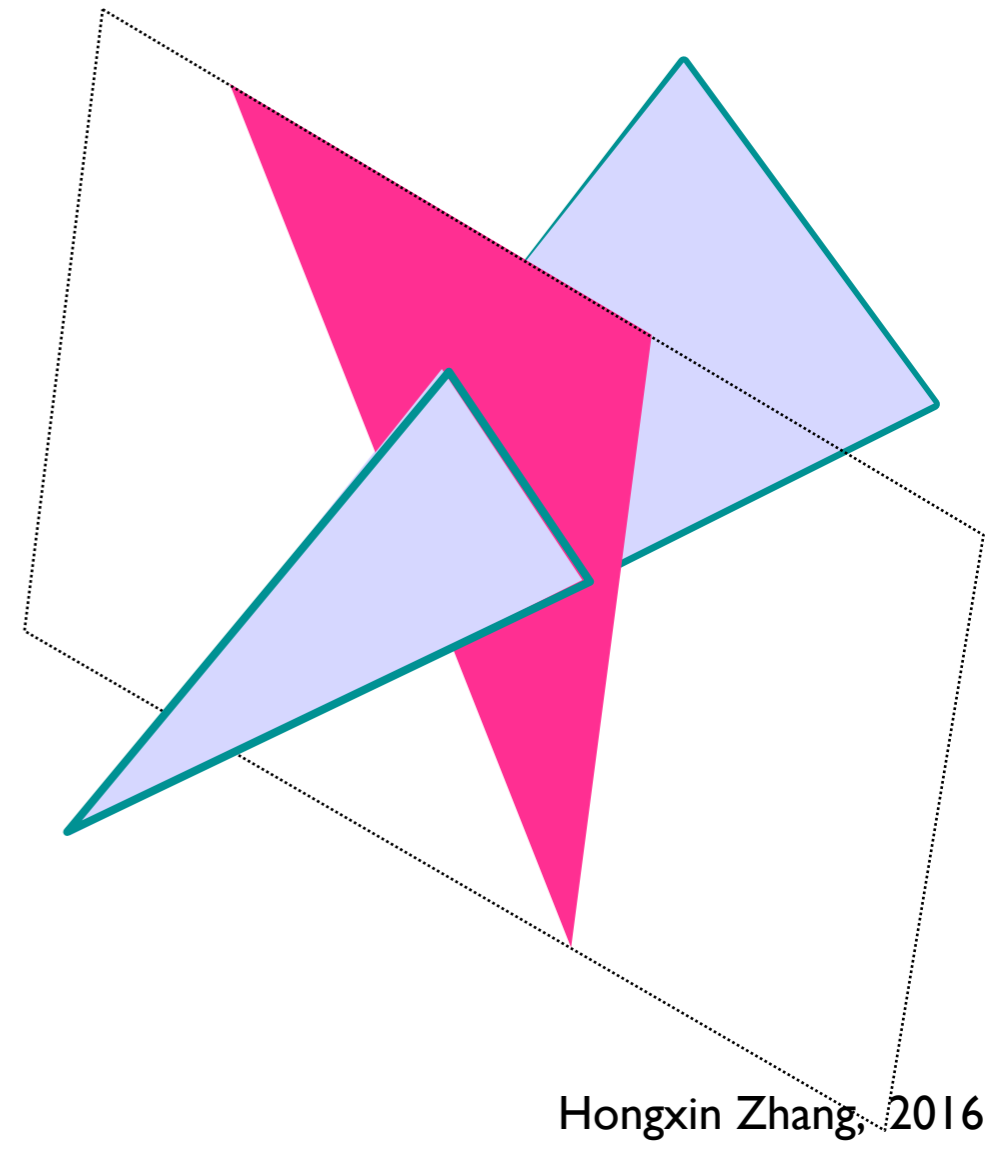
$f_{plane\ of\ the\ triangle}(eye)$



# BSP Tree Construction

---

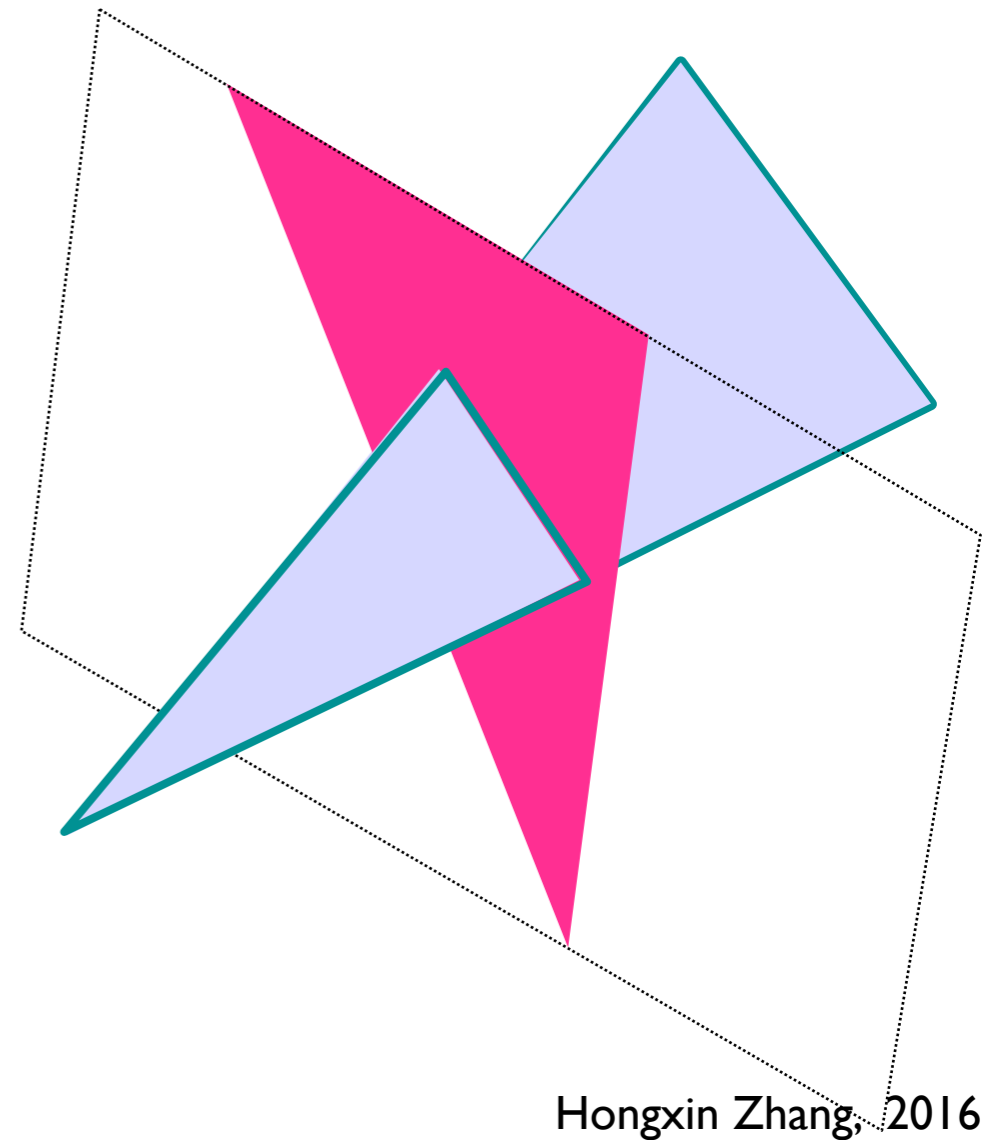
- The binary tree is constructed using the following principle:
  - For each polygon, we can divide the set of other polygons into two groups
  - One group contains those lying in front of the plane of the given polygon
  - The other group contains those in the back
  - The polygons intersecting the plane of the given polygon are split by that plane



# BSP Tree

---

- Split Triangle:  
How to?



# Summary: BSP Trees

---

- Pros:

  - Simple, elegant scheme

  - Only writes to frame-buffer (i.e., painters algorithm)

    - Thus very popular for video games (but getting less so)

- Cons:

  - Computationally intense preprocess stage restricts algorithm to static scenes

  - Worst-case time to construct tree:  $O(n^3)$

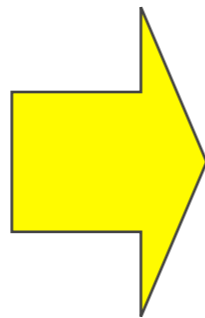
  - Splitting increases polygon count

    - Again,  $O(n^3)$  worst case



---

**Computational  
expensive of  
clipping**



Z-buffer

Scan-line

Warnock:

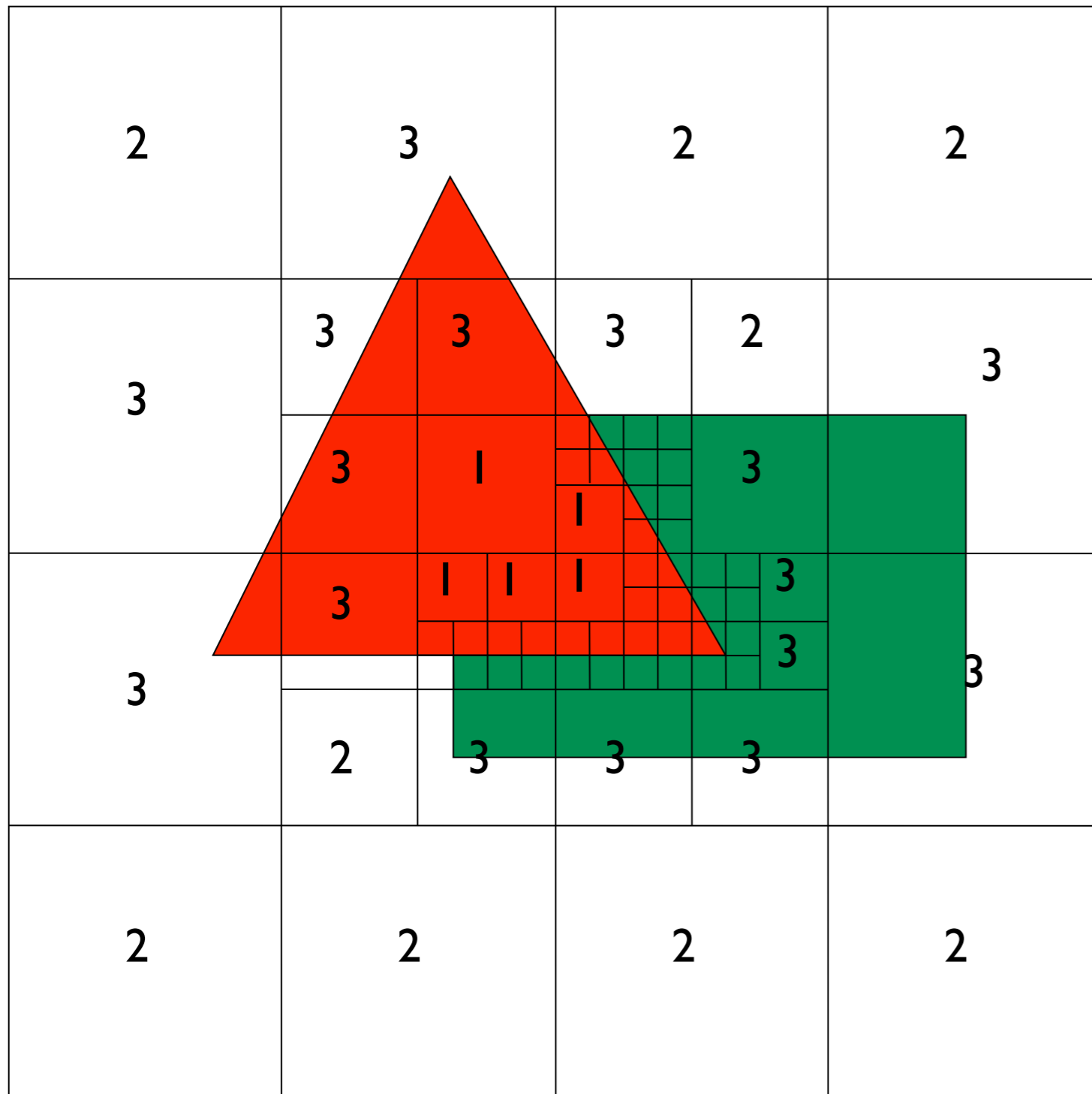
A divide and conquer

# Warnock's Area Subdivision (Image Precision)

---

- Start with whole image
- If one of the easy cases is satisfied, draw what's in front
  - front polygon covers the whole window or
  - there is at most one polygon in the window.
- Otherwise, subdivide region into 4 windows and recurse
- If region is single pixel, choose surface with smallest depth
  
- Advantages:
  - No over-rendering
  - Anti-aliases well - just recurse deeper to get sub-pixel information
- Disadvantage:
  - Tests are quite complex and slow

# Warnock's Algorithm



- Regions labeled with case used to classify them:

One polygon in front

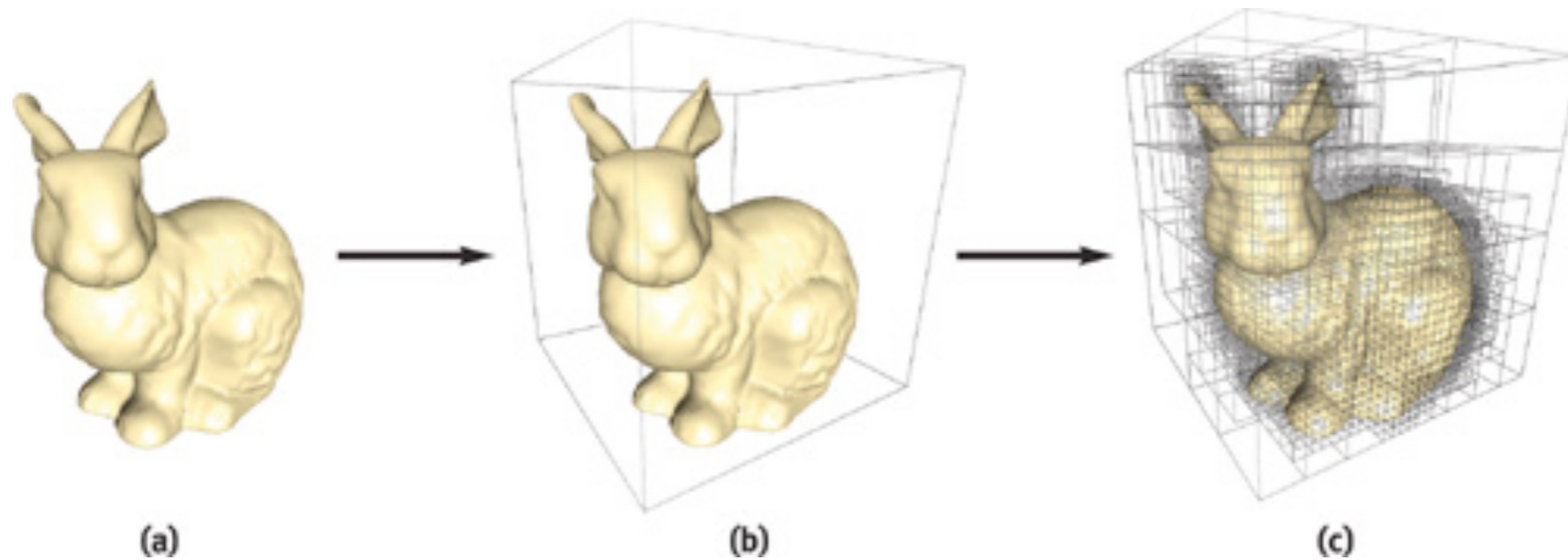
Empty

One polygon inside, surrounding or intersecting

- Small regions not labeled

# Octree

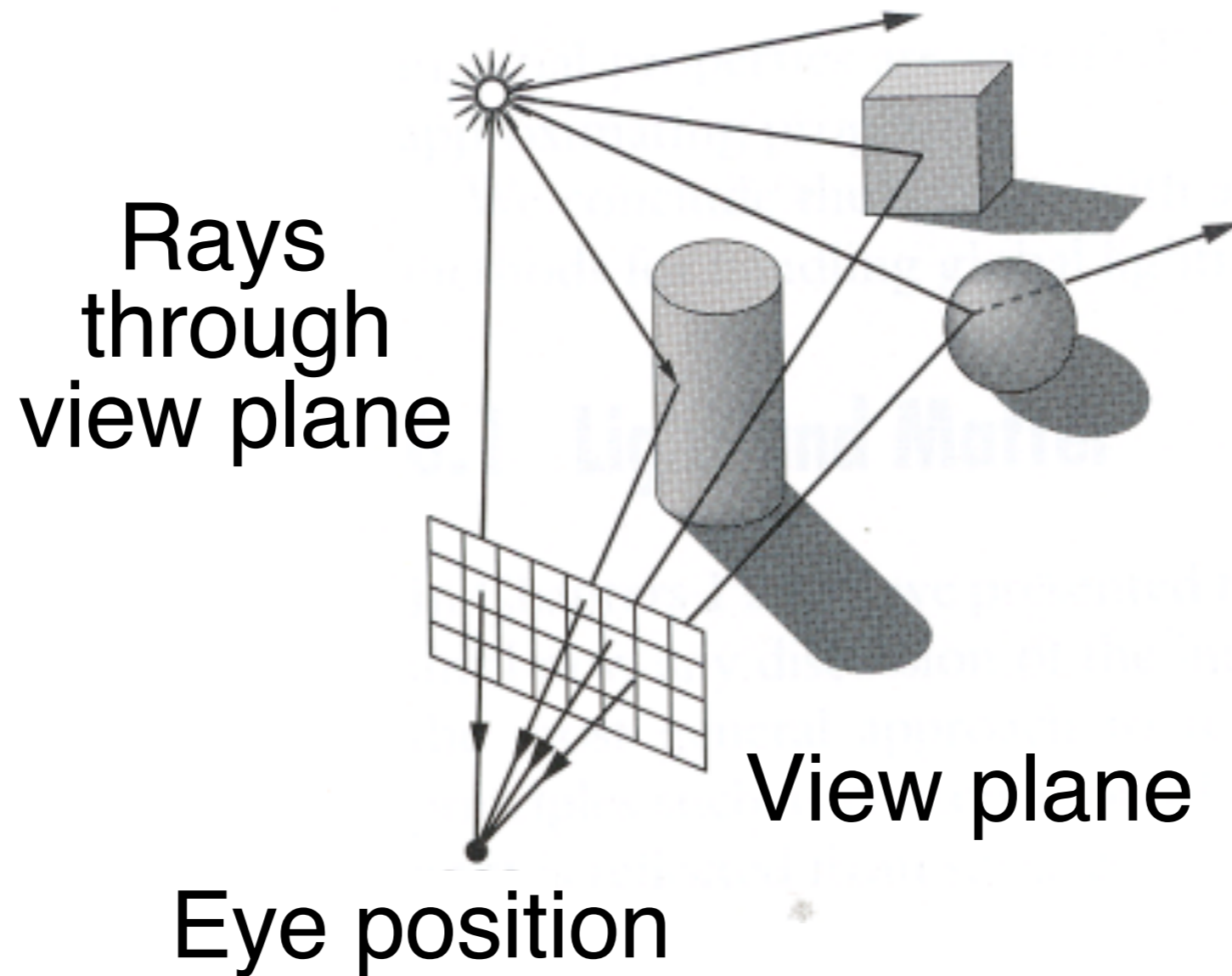
---



[http://en.wikipedia.org/wiki/View\\_frustum\\_culling](http://en.wikipedia.org/wiki/View_frustum_culling)

# Ray casting

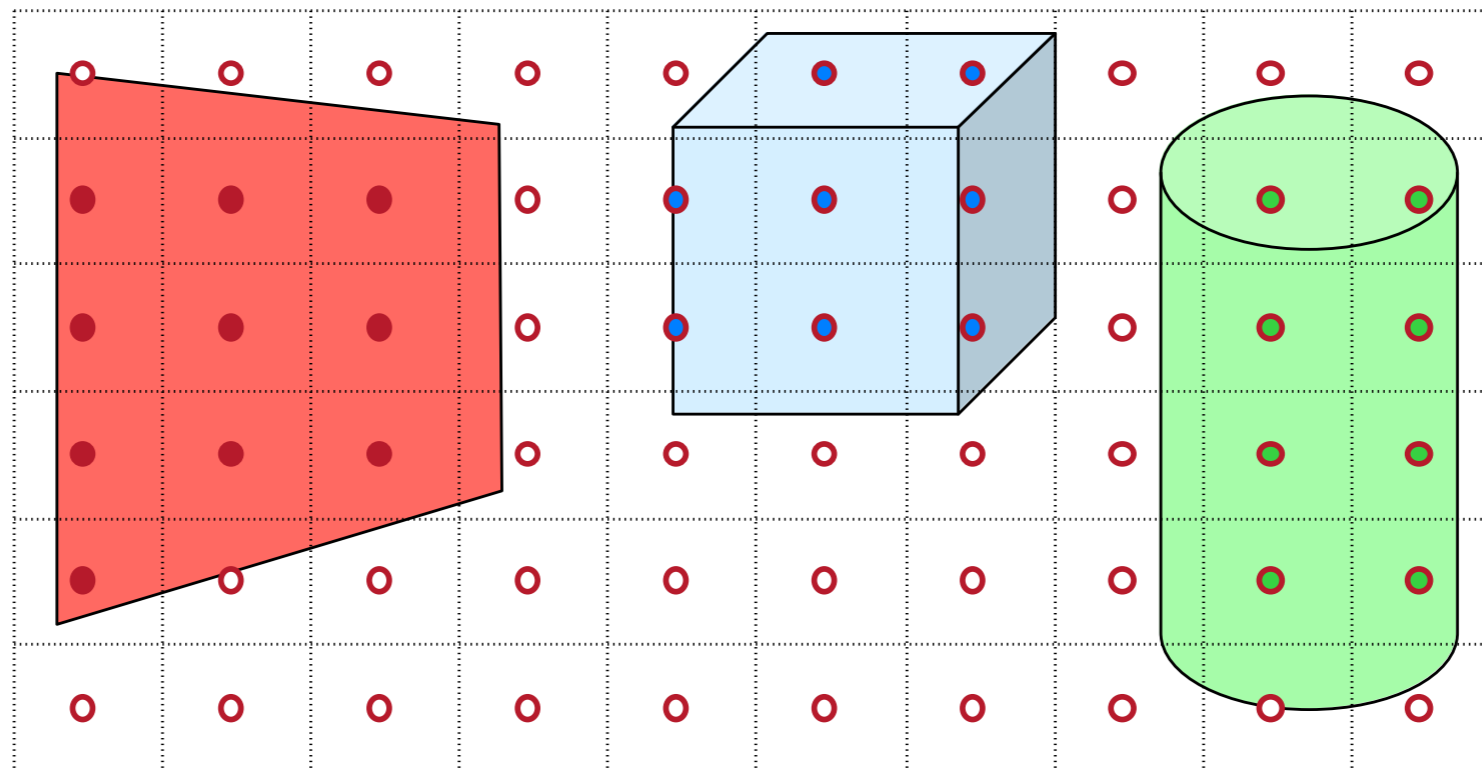
---



# Ray Casting

---

- For each sample ...
  - Construct ray from eye position through view plane
  - Find first surface intersected by ray through pixel
  - Compute color sample based on surface radiance



**Thank You**