Homework 02

• Build a Solar System
  • requirement:
    • detailed computing steps
    • at least Earth, Moon and Sun
    • in OpenGL
  • bonus:
    • implemented demo
  • Deadline: 2014-10-24
Contents

• 2D viewing
• 3D viewing
2D Viewing

- The world is **infinite** (2D or 3D) but the screen is **finite**
- Depending on the details the user wishes to see, he limits his view by specifying a window in this world
By applying *appropriate transformations* we can map the world seen through the window on to the screen.
Windowing Concepts

• **Window** is a rectangular region in the 2D world specified by
  • a **center** \((x_{\text{Center}}, y_{\text{Center}})\) and
  • **size** \(\text{windowSize}\)

• Screen referred to as **Viewport** is a discrete matrix of pixels specified by
  • **size** \(\text{screenSize}\) (in pixels)
2D Viewing Transformation

• Mapping the 2D world seen in the window on to the viewport is 2D viewing transformation

• also called window to viewport transformation
Deriving 2D Viewing Transformation

\[ x - x_{\text{Center}} \]
\[ y - y_{\text{Center}} \]

\[
\begin{pmatrix}
(x - x_{\text{Center}}) \cdot \text{scaleFactor} \\
(y - y_{\text{Center}}) \cdot \text{scaleFactor}
\end{pmatrix}
\]

where, \( \text{scaleFactor} = \frac{\text{screenSize}}{\text{windowSize}} \)
• Given any point in the 2D world, the above transformations maps that point on to the screen.

\[
\frac{screenSize}{2} + \frac{(x - xCenter) \cdot scaleFactor}{2} - \frac{y - yCenter \cdot scaleFactor}{2}
\]
The Aspect Ratio

- In 2D viewing transformation the *aspect ratio* is maintained when the scaling is uniform.
- *scaleFactor* is same for both \(x\) and \(y\) directions.

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In the diagram:

- The 2D World represents the coordinate system where objects are originally defined.
- The Screen represents the display area on the screen.
- The \(x\) and \(y\) axes indicate the horizontal and vertical directions, respectively.
- The \(windowWidth\) and \(windowHeight\) represent the dimensions of the window.
- The \(screenWidth\) and \(screenHeight\) represent the dimensions of the screen.
- The ratio \(windowHeight / windowWidth\) represents the aspect ratio of the window.
- The ratio \(screenHeight / screenWidth\) represents the aspect ratio of the screen.

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Maintaining Aspect Ratio

\[
scaleFactor = \frac{screenHeight}{windowHeight}
\]

\[
scaleFactor = \frac{screenWidth}{windowWidth}
\]
OpenGL Commands

**gluOrtho2D( left, right, bottom, top )**

Creates a matrix for projecting 2D coordinates onto the screen and multiplies the current matrix by it.

**glViewport( x, y, width, height )**

Define a pixel rectangle into which the final image is mapped. 
(x, y) specifies the lower-left corner of the viewport. 
(width, height) specifies the size of the viewport rectangle.
void myReshape(GLsizei w,GLsizei h)
{
    glViewport(0,0,w,h);//设置视口
    glMatrixMode(GL_PROJECTION);//指明当前矩阵为GL_PROJECTION
    glLoadIdentity();//将当前矩阵置换为单位阵

    //定义二维正视投影矩阵
    if(w <= h)
        gluOrtho2D(-1.0,1.5,-1.5,1.5*(GLfloat)h/(GLfloat)w);
    else
        gluOrtho2D(-1.0,1.5*(GLfloat)w/(GLfloat)h,-1.5,1.5);
    glMatrixMode(GL_MODELVIEW);//指明当前矩阵为GL_MODELVIEW
}

Computer Graphics 2014, ZJU
void myDisplay(void)
{
    glClear(GL_COLOR_BUFFER_BIT); //刷新颜色buffer
    glShadeModel(GL_SMOOTH); //设置为光滑明暗模式
    glBegin(GL_TRIANGLES); //开始画三角形
        glColor3f(1.0,0.0,0.0); //设置第一个顶点为红色
        glVertex2f(-1.0,-1.0); //设置第一个顶点的坐标为(-1.0, -1.0)
        glColor3f(0.0,1.0,0.0); //设置第二个顶点为绿色
        glVertex2f(0.0,-1.0); //设置第二个顶点的坐标为(0.0, -1.0)
        glColor3f(0.0,0.0,1.0); //设置第三个顶点为蓝色
        glVertex2f(-0.5,1.0); //设置第三个顶点的坐标为(-0.5, 1.0)
    glEnd(); //三角形结束
    glFlush(); //强制OpenGL函数在有限时间内运行
}
2D Rendering-3
2D Rendering-3
User Interactions

Panning

Zoom In

Zoom Out
Modeling v.s. Viewing

• viewing transformations ≠ modeling transformations

  • *Modeling transformations* actually position the objects in the world,

• but viewing transformations are applied only to make a mapping from world to the screen

• *Viewing transformations* do not change the actual world in any fashion
Modeling Coordinates

Objects are usually defined in their own **local coordinate system** (instance transformation)
Modeling Coordinates

Objects are usually defined in their own local coordinate system (instance transformation)

Place (transform) these objects in a single scene,
Modeling Coordinates

Objects are usually defined in their own local coordinate system (instance transformation)

Place (transform) these objects in a single scene, in world coordinates
Modeling Coordinates

Objects are usually defined in their own local coordinate system (instance transformation)

Place (transform) these objects in a single scene, in world coordinates (modeling transformation)
Finally, we want to project these objects onto the screen
3D Viewing
3D Viewing

- To display a 3D world onto a 2D screen
  - Specification becomes complicated because there are many parameters to control
  - Additional task of reducing dimensions from 3D to 2D (projection)

- 3D viewing is analogous to taking a picture with a camera
The Pinhole Camera

The principle upon which all camera equipment works is traced to artist / inventor Leonardo da Vinci who showed that all that was needed to project an image was a small pinhole through which light could pass. The smaller the hole the sharper the image.

The basic camera, called a pinhole camera, existed in the early 17th Century. It took much longer for science to find a light sensitive material to record the image. It was not until 1826 when Joseph Niepce from France discovered that silver chloride (氯化银) could be used to make bitumen sensitive to light.

http://www.phy.ntnu.edu.tw/java/pinHole/pinhole.html

The world through a pinhole
Transformations and Camera Analogy

• **Modeling transformation**
  • Shaping, positioning and moving the objects in the world scene

• **Viewing transformation**
  • Positioning and pointing camera onto the scene, selecting the region of interest

• **Projection transformation**
  • Adjusting the distance of the eye

• **Viewport transformation**
  • Enlarging or reducing the physical photograph
Classical Viewing

Perspective Projection

PRP: Projection Reference Point = Eye position

Figures extracted from Angle's textbook
History of Perspective

"Perspective is the rein and rudder of painting"
Leonardo da Vinci
Early Perspective

Giotto di Bondone (1267–1337)

这位13世纪末、14世纪初的画家，为公认的西方绘画之父、文艺复兴的先驱。但以往因意大利官方难得愿意出借国宝外展，因此国人多不够熟悉这位西方美术史上的经典人物。

Not systematic -- lines do not converge to a single "vanishing" point
Vanishing Points

Brunelleschi

Invented systematic method of determining perspective projections in early 1400's

Brunelleschi's Peepshow (西洋镜)

VPL

VPR
Vanishing Points

Brunelleschi

Invented systematic method of determining perspective projections in early 1400's

Filippo Brunelleschi (1377-1446), early文艺复兴建筑先锋画家、雕刻家、建筑师、以及工程师。1420-36年间完成佛罗伦萨教堂的高耸圆顶, 发明了完成圆顶与穹窿顶塔的技术与工程。1415年重新发现线性透视法，使空间变得逼真

Brunelleschi's Peepshow (西洋镜)
Single Vanishing Point

RAPHAEL: School of Athens
Perspective Projection

- Characterized by diminution of size
- The farther the object, the smaller the image
- Foreshortening depends on distance from viewer
- Can’t be used for measurements
- Vanishing points
Engineering Viewing

Parallel Projection

Object

Projection Plane

DOP: Direction of Projection = Eye position at infinity

Figures extracted from Angle's textbook
Taxonomy of Projections

Planar Projection

Parallel projection

Oblique
  - Cavalier
  - Cabinet

Orthographic
  - Axonometric

Perspective projection

1pt 2pt 3pt

Multiview Orthographic

Isometric  Dimetric  Trimetric

Figures extracted from Angle's textbook
Orthographic Projection 正交投影

DOP is perpendicular to the view plane

DOP is the same for all points

Figures extracted from Angle's textbook
Multiview Parallel Projection
多角度平行投影

Faces are parallel to the projection plane

Figures extracted from Angle's textbook
Axonometric Projections 轴侧投影

- DOP orthogonal to the projection plane, but...
  ...orient projection plane with respect to the object
- Parallel lines remain parallel, and receding lines are equally foreshortened by some factor.

Projection type depends on angles made by projector with the three principal axes.

Figures extracted from Angle's textbook
Reference

Foreshortening

Object size $s$ is foreshortened to $l$

$$l = s \cos \theta = s(u \cdot n)$$
mechanical drawing

isometric

trimetric
Oblique Projections

斜平行投影

• Most general parallel views
• Projectors make an arbitrary angle with the projection plane
• Angles in planes parallel to the projection plane are preserved
• Back of view camera
Oblique Projections

Cavalier
Angle between projectors and projection plane is 45°. Perpendicular faces are projected at full scale

Cabinet
Angle between projectors and projection plane is 63.4°. Perpendicular faces are projected at 50% scale

Figures extracted from Angle's textbook
Perspective Viewing

Type of perspective depends on the number of principal axes cut by the projectors.

3-point

2-point

1-point

Figures extracted from Angle's textbook
View Specification

Specify

Focus point or reference point, typically on the object

(view reference point)

direction of viewing

(viewDirection)

picture’s up-direction (upVector)

All the specifications are in world coordinates
View Reference Coordinate System

World coordinates

\[ \vec{n} = -\text{viewDirection} \]
\[ \vec{u} = \text{upVector} \times \vec{n} \]
\[ \vec{v} = \vec{n} \times \vec{u} \]
View Up Vector

- `upVector` decides the orientation of the view window on the view reference plane
Once the view reference coordinate system is defined, the next step is to project the 3D world on to the view reference plane.
Simplest Camera position

- Projecting on to an arbitrary view plane looks tedious

- One of the simplest camera positions is one where \textit{vrp} coincides with the \textit{world origin} and \textit{u,v,n} matches \textit{x,y,z}

- Projection could be as simple as ignoring the \textit{z-coordinate}
World to Viewing coordinate Transformation

• The world could be transformed so that the view reference coordinate system coincides with the world coordinate system

• Such a transformation is called world to viewing coordinate transformation

• The transformation matrix is also called view orientation matrix
Deriving View Orientation Matrix

- The **view orientation matrix** transforms a point from **world** coordinates to **view coordinates**

\[
\begin{bmatrix}
    u_x & u_y & u_z & -u \cdot vrp \\
    v_x & v_y & v_z & -v \cdot vrp \\
    n_x & n_y & n_z & -n \cdot vrp \\
    0   & 0   & 0   & 1
\end{bmatrix}
\]
Deriving View Orientation Matrix

- The view orientation matrix transforms a point from world coordinates to view coordinates.
Perspective Projection

• The points are transformed to the view plane along lines that converge to a point called
  • projection reference point (prp) or
  • center of projection (cop)

• prp is specified in terms of the viewing coordinate system
Transformation Matrix for Perspective Projection

- \( \text{prp} \) is usually specified as perpendicular distance \( d \) behind the view plane

\[
\begin{bmatrix}
1 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 \\
0 & 0 & 0 & 0 \\
0 & 0 & 1/d & 1
\end{bmatrix}
\]
View Window

- **View window** is a rectangle in the view plane specified in terms of view coordinates.

- Specify **center** \((cx, cy)\), **width** and **height**

- \(prp\) lies on the axis passing through the center of the view window and parallel to the n-axis
Perspective Viewing

1. Apply the view orientation transformation

2. Apply translation, such that the center of the view window coincide with the origin

3. Apply the perspective projection matrix to project the 3D world onto the view plane
4. Apply 2D viewing transformations to map the view window (centered at the origin) on to the screen
Parallel Viewing

1. Apply the world to view transformation

2. Apply the parallel projection matrix to project the 3D world onto the view plane

\[
\begin{bmatrix}
1 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 \\
0 & 0 & 0 & 0 \\
0 & 0 & 0 & 1
\end{bmatrix}
\times
\begin{bmatrix}
u_x & u_y & u_z & -r \\
v_x & v_y & v_z & -r \\
n_x & n_y & n_z & -r \\
0 & 0 & 0 & 1
\end{bmatrix}
\]

3. Apply 2D viewing transformations to map the view window on to the screen
View Volume & Clipping

- For *perspective projection* the **view volume** is a semi infinite pyramid with apex at *prp* and edges passing through the corners of the *view window*.

- For efficiency, view volume is made finite by specifying the front and back clipping plane specified as distance from the *view plane*. 
• For parallel projection the view volume is an infinite parallelepiped with sides parallel to the direction of projection

• View volume is made finite by specifying the front and back clipping plane specified as distance from the view plane

• Clipping is done in 3D by clipping the world against the front clip plane, back clip plane and the four side planes
The Complete View Specification

• Specification in world coordinates
  position of viewing \((v_{rp})\), direction of viewing\((-n)\),
  up direction for viewing \((u_{pVector})\)

• Specification in view coordinates
  view window : center \((cx, cy)\), \textit{width} and \textit{height},
  \textit{prp} : distance from the view plane,
  front clipping plane : distance from view plane
  back clipping plane : distance from view plane
OpenGL Parallel View

glOrtho(left, right, bottom, top, near, far);
OpenGL Perspective

\[ \text{glFrustum(left, right, bottom, top, near, far);} \]

\[ \text{glMatrixMode(GL_PROJECTION);} \]

\[ \text{glLoadIdentity( );} \]

\[ \text{glFrustum(left, right, bottom, top, near, far);} \]
OpenGL Perspective

`gluPerspective(fovy, aspect, near, far);`

FOV is the angle between the top and bottom planes
gluPerspective(fovy, aspect, near, far)

{
  GLdouble m[4][4];
  double sine, cotangent, deltaZ;
  double radians = fovy / 2 * __glPi / 180;

  deltaZ = zFar - zNear;
  sine = sin(radians);
  if ((deltaZ == 0) || (sine == 0) || (aspect == 0)) {
    return;
  }

  cotangent = COS(radians) / sine;

  gluMakeIdentityd(&m[0][0]);
  m[0][0] = cotangent / aspect;
  m[1][1] = cotangent;
  m[2][2] = -(zFar + zNear) / deltaZ;
  m[2][3] = -1;
  m[3][2] = -2 * zNear * zFar / deltaZ;
  m[3][3] = 0;
  glMultMatrixd(&m[0][0]);
}
A More Intuitive Approach Offered by GLU

\texttt{gluLookAt(eyex, eyey, eyez, atx, aty, atz, upx, upy, upz);}

eyex, eyey, eyez specify the position of the eye point and are mapped to the origin.

atx, aty, atz specify a point being looked at, which will be rendered in center of view port. It is mapped to the -z axis.

upx, upy, upz specify components of the camera up vector.
```c
gluLookAt
{
    float forward[3], side[3], up[3];
    GLfloat m[4][4];
    forward[0] = centerx - eyex;
    forward[1] = centery - eyey;
    forward[2] = centerz - eyez;
    up[0] = upx;
    up[1] = upy;
    up[2] = upz;
    normalize(forward);
    /* Side = forward x up */
    cross(forward, up, side);
    normalize(side);
    /* Recompute up as: up = side x forward */
    cross(side, forward, up);
    __gluMakeIdentityf(&m[0][0]);
    m[0][0] = side[0];
    m[1][0] = side[1];
    m[2][0] = side[2];
    m[0][1] = up[0];
    m[1][1] = up[1];
    m[2][1] = up[2];
    m[0][2] = -forward[0];
    m[1][2] = -forward[1];
    m[2][2] = -forward[2];
    glMultMatrixf(&m[0][0]);
    glTranslated(-eyex, -eyey, -eyez);
}
```
Homework 03

- How to stitch 2x2 iPad screen (2048 x 1536) together to create a larger OpenGL viewport (4K)

- requirement:
  - detailed computing steps

- bonus:
  - implemented demo