



# Exploring the Sensitivity of Choropleths under Attribute Uncertainty

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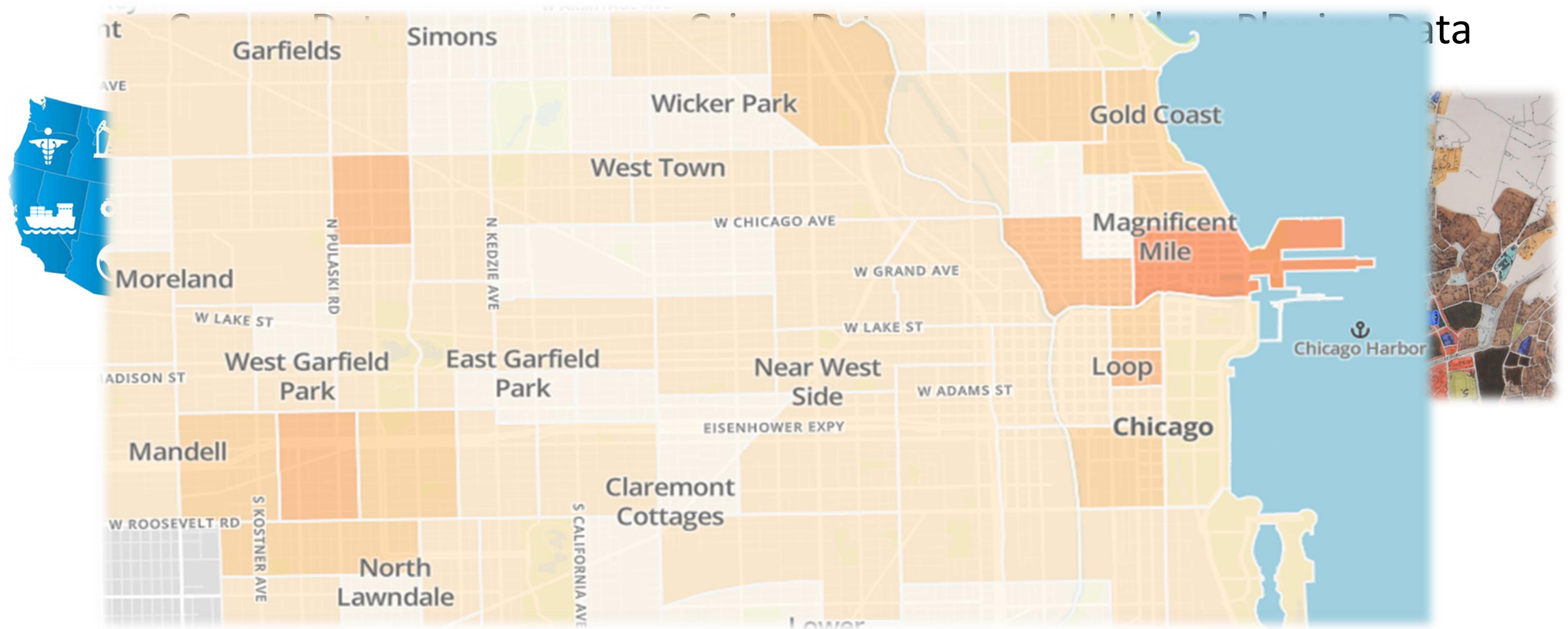
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3 The Department of Geography, Michigan State University

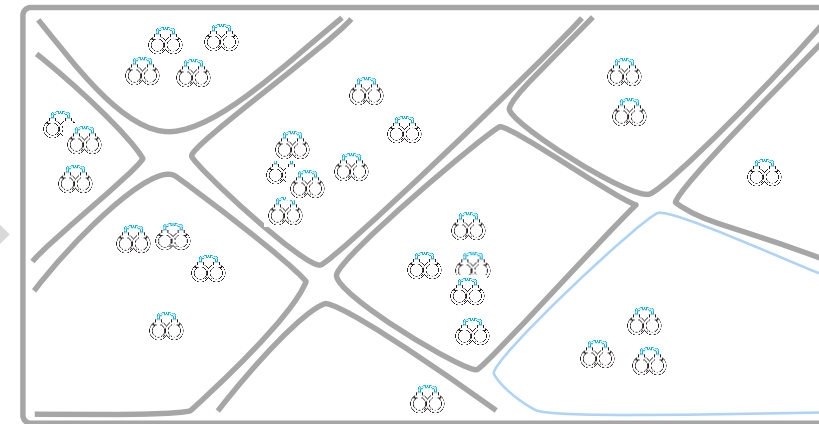


# Geospatial Analysis

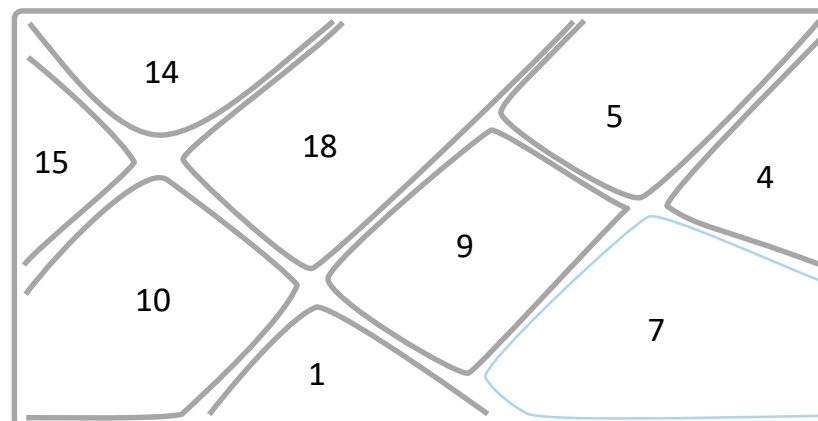


Choropleth map is one of the most common methods of visualizing spatially referenced data

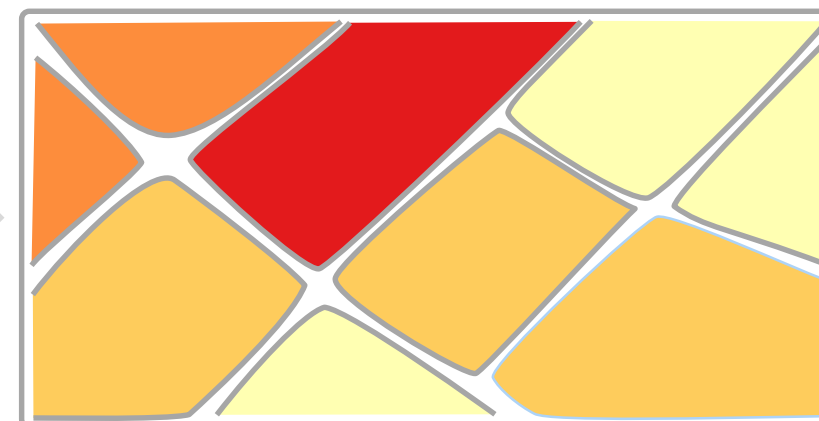
# Raw data

[illegible]

## Statistical data



## Choropleth Map



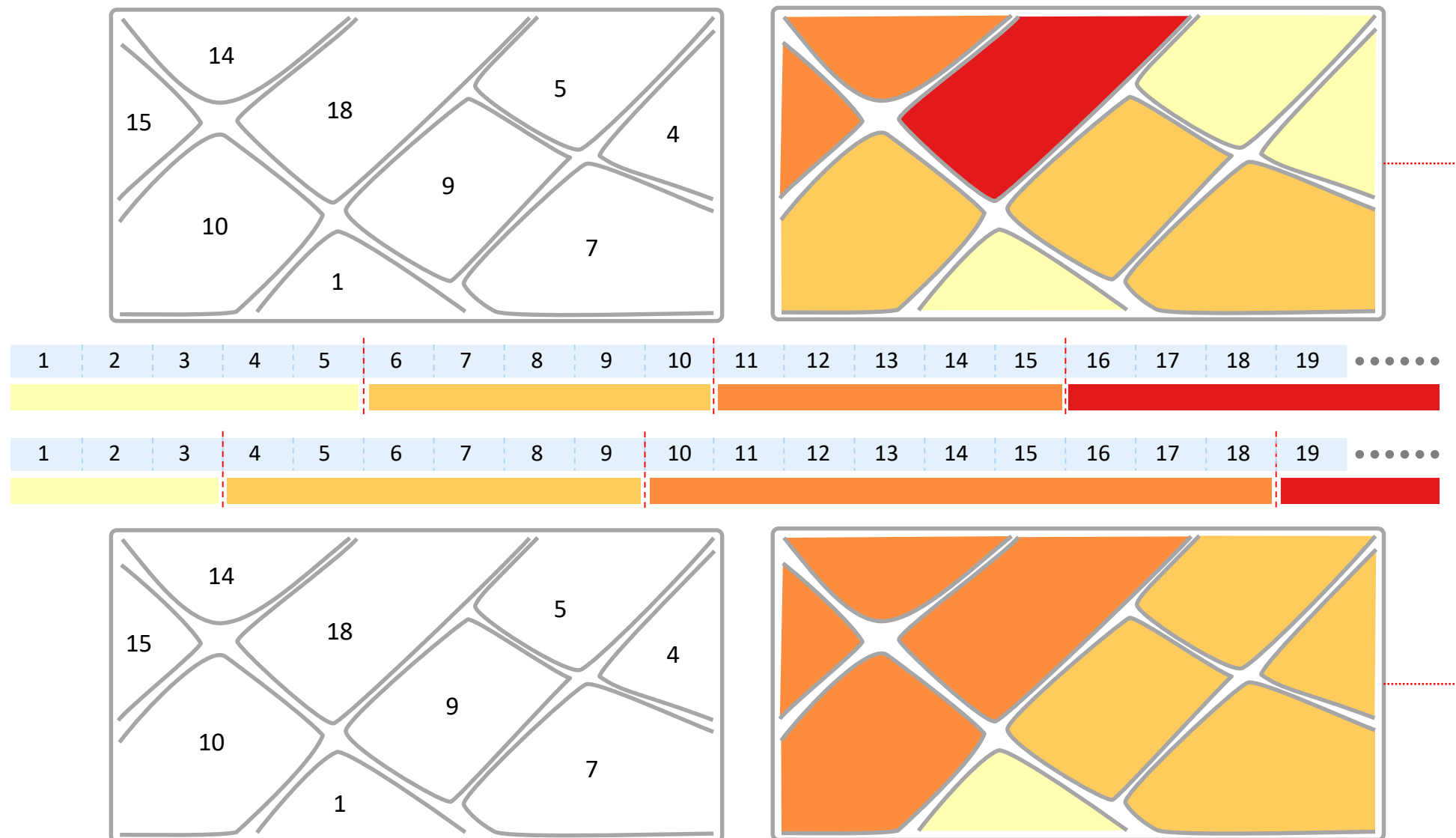
## histogram binning

0-5 6-10 11-15 16+

- Based on statistical data
- Regions are classified into several groups
- Region color is decided by a histogram binning of the measured variable

# Choropleth Maps – What happens under uncertainty?

The visual representation of the choropleth map is highly influenced by the class interval selection

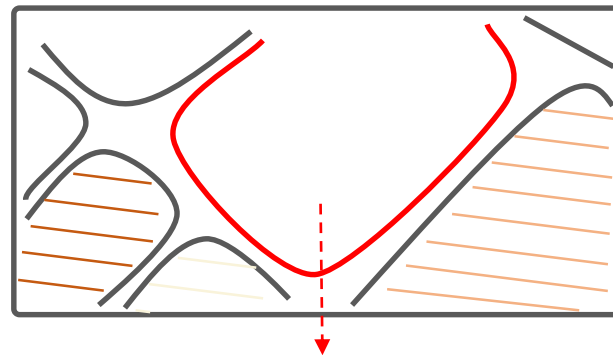


# Choropleth Maps – Data Uncertainty

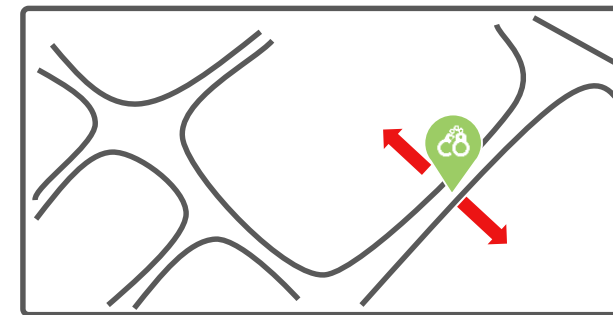
Many geographic datasets have an inherent level of uncertainty

 GPS traces    Twitter locations    American Community Survey<sup>1</sup>

In choropleth maps, we are mostly interested in attribute uncertainty



Around 10 Crimes



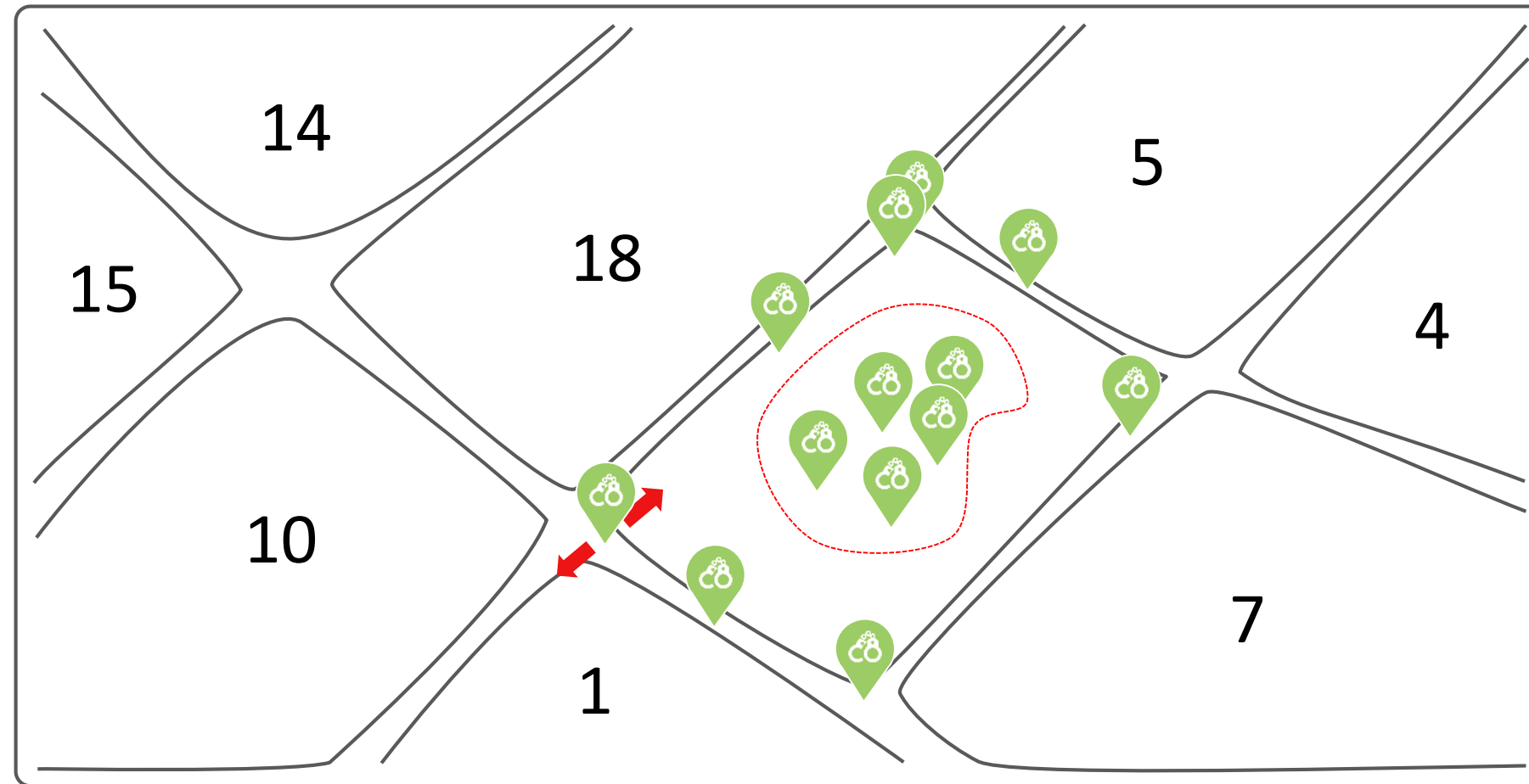
Ambiguous Location

- Arises from varying the spatial aggregation of data
- Often referred to as the modifiable areal unit problem (MAUP)<sup>2</sup>



# Choropleth Maps – What happens under uncertainty?

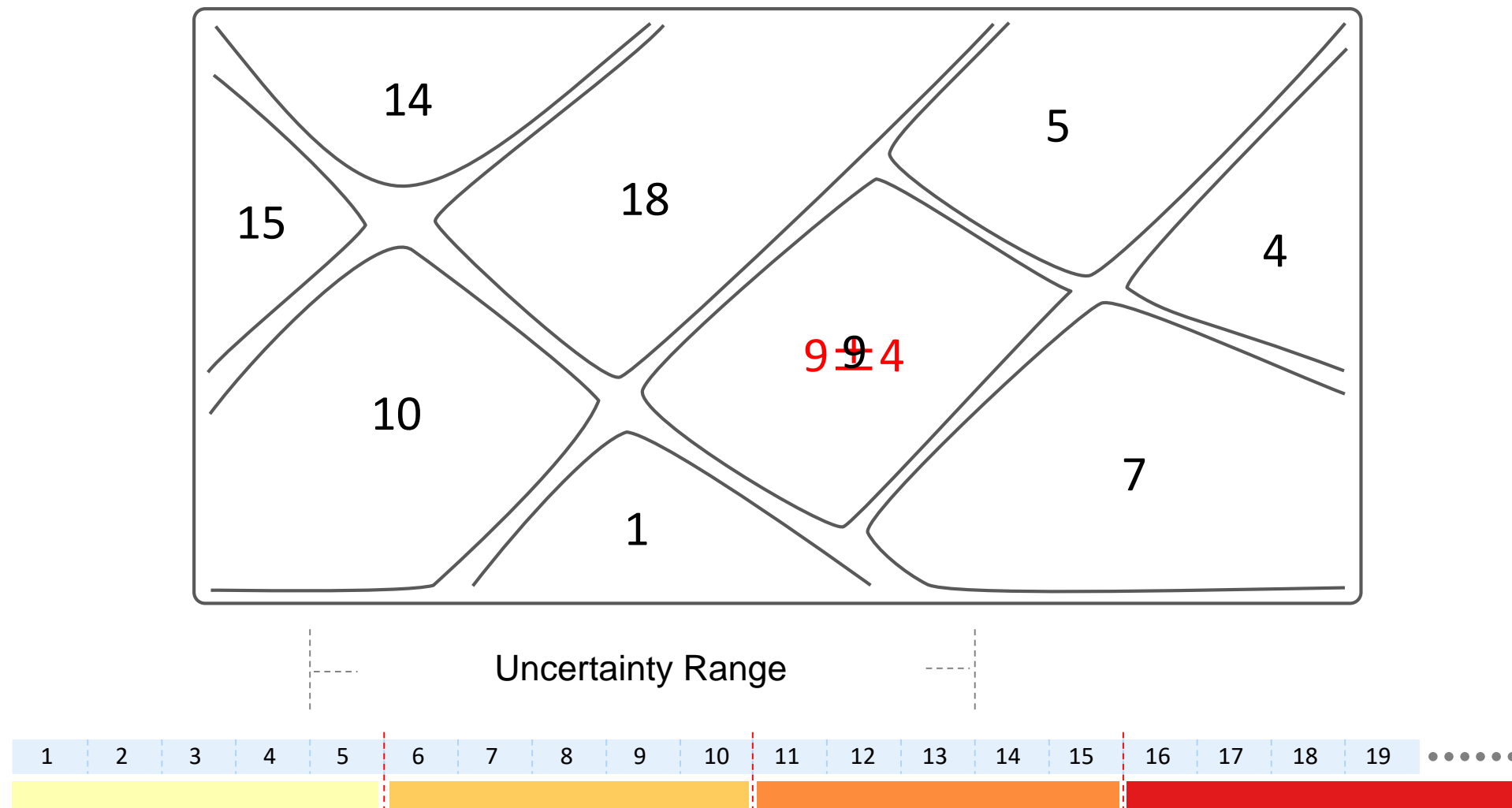
The visual representation of the choropleth map is highly influenced by the data uncertainty





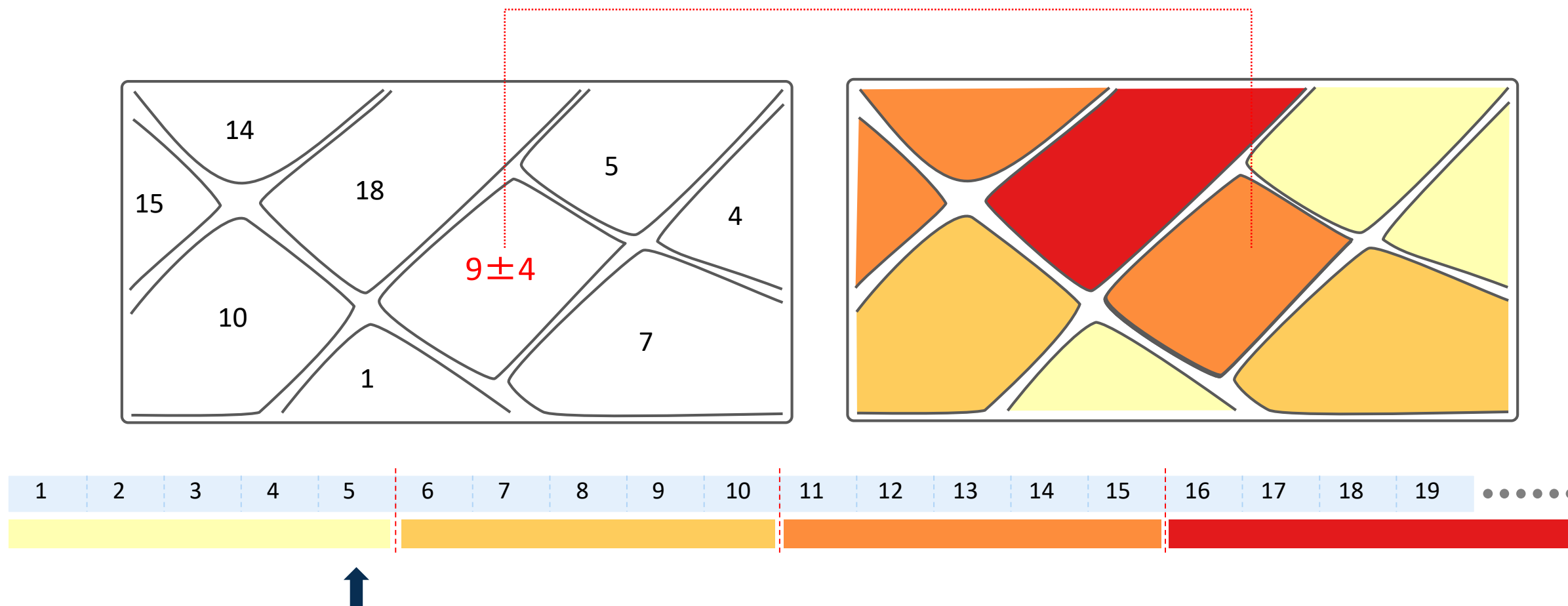
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# Choropleth Maps – What happens under uncertainty?

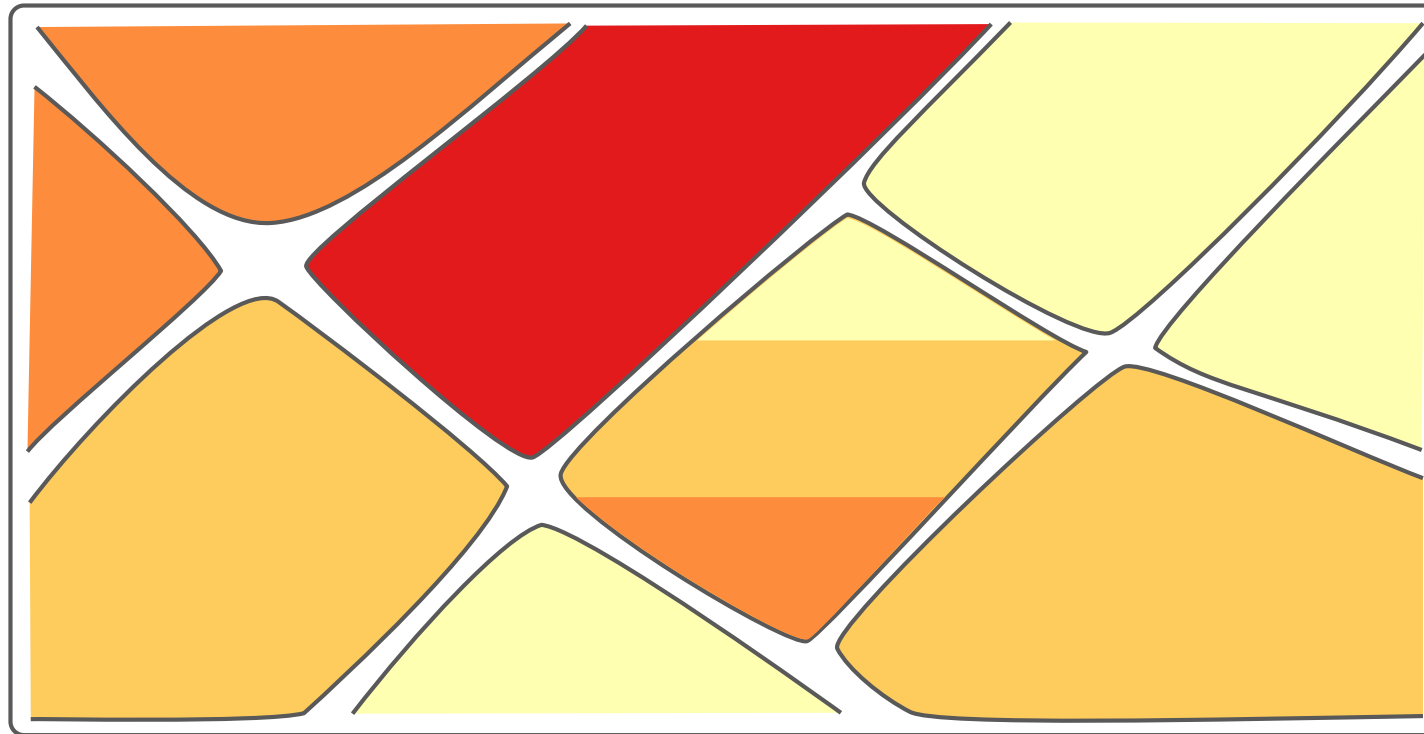
The visual representation of the choropleth map is highly influenced by the data uncertainty



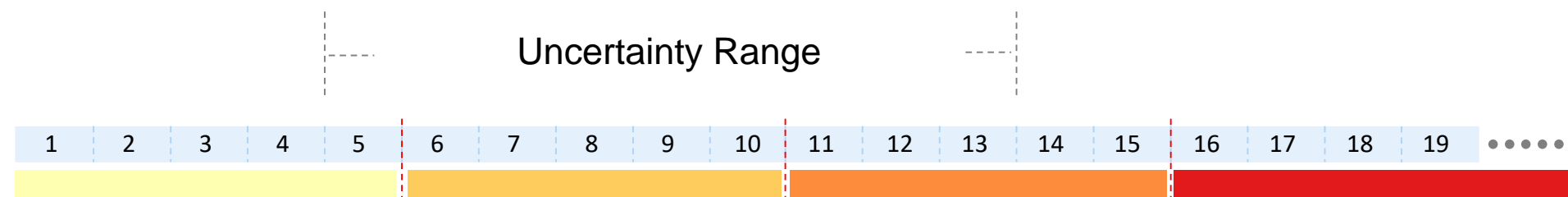


# Choropleth Maps – What happens under uncertainty?

What should the map look like?



- Visual appearance
- Spatial autocorrelation
- Relationships between variables

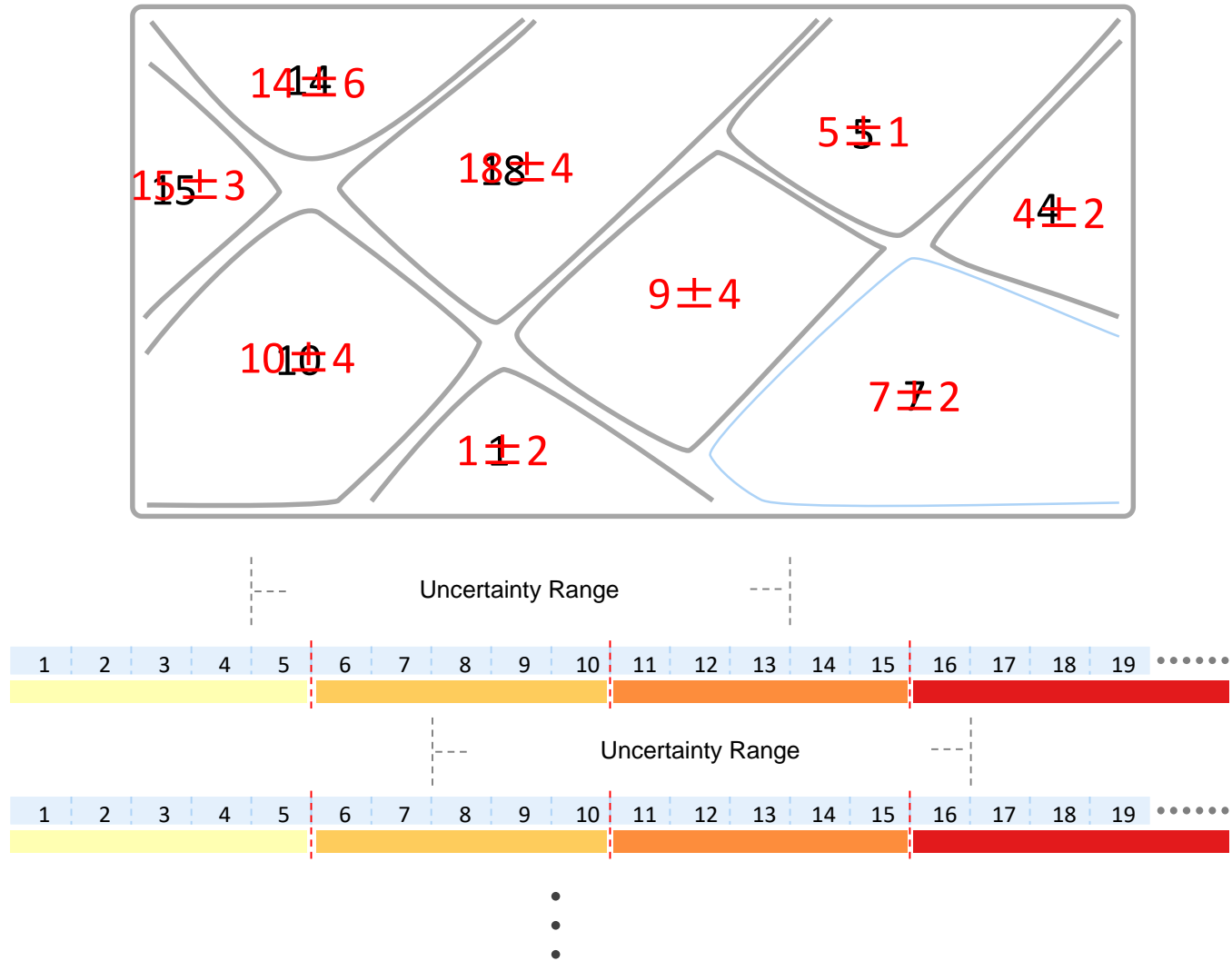


# Choropleth Maps – What happens if...?

The issue of uncertainty becomes even more complex in analyses implementing

Univariate context

Multivariate Classification

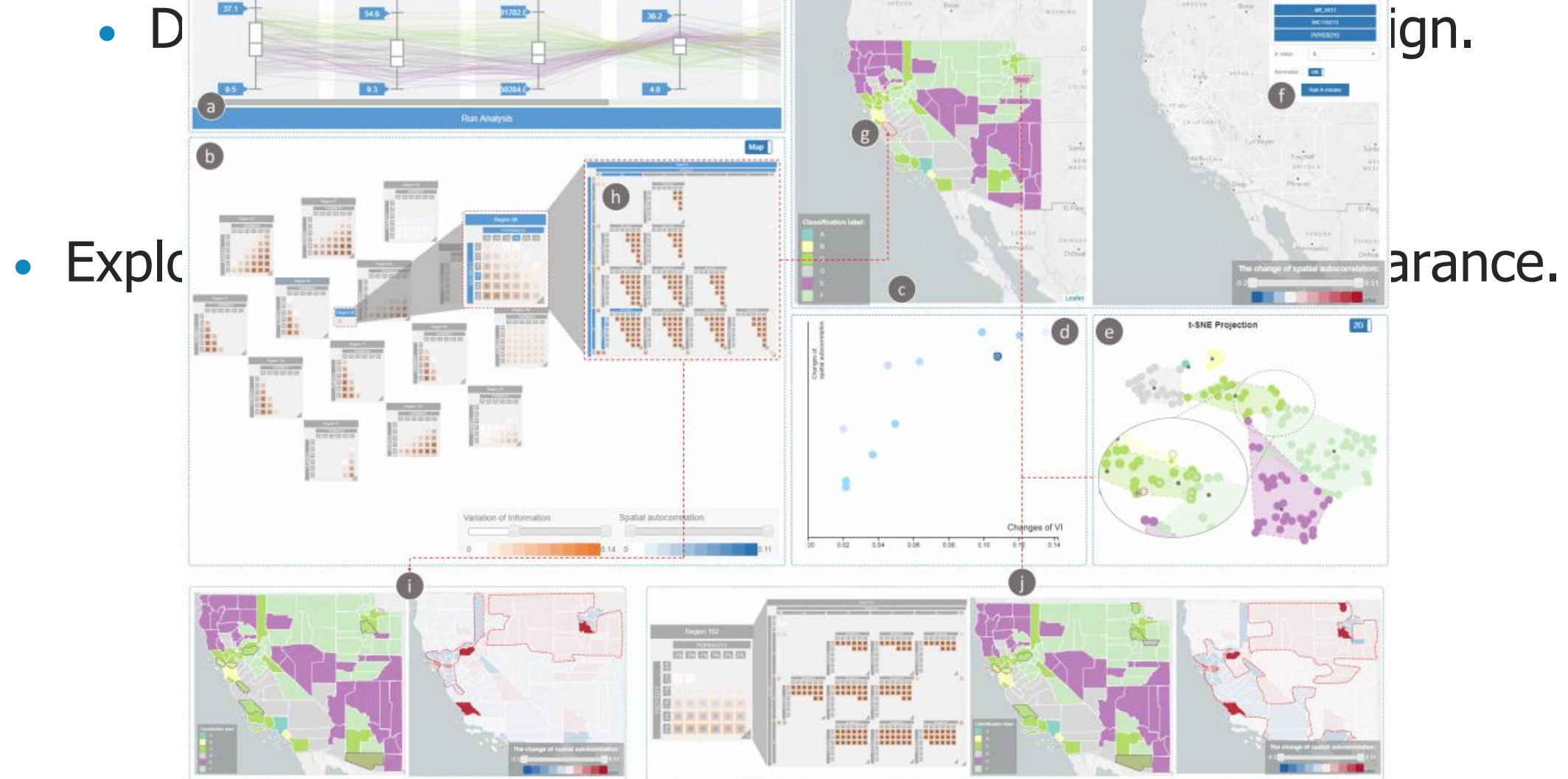


Variable name	Description
PST045214	Population, 2014 estimate
PST040210	Population, 2010 (April 1) estimates base
PST120214	Population, percent change - April 1, 2010 to July 1, 2014
POP010210	Population, 2010
AGE135214	Persons under 5 years, percent, 2014
AGE295214	Persons under 18 years, percent, 2014
AGE775214	Persons 65 years and over, percent, 2014
EDU635213	High school graduate or higher, percent of persons age 25+, 2009-2013
EDU685213	Bachelor's degree or higher, percent of persons age 25+, 2009-2013
VET605213	Veterans, 2009-2013
LFE305213	Mean travel time to work (minutes), workers age 16+, 2009-2013
HSG010214	Housing units, 2014
HSG445213	Homeownership rate, 2009-2013
HSG096213	Housing units in multi-unit structures, percent, 2009-2013
HSG495213	Median value of owner-occupied housing units, 2009-2013
HSD410213	Households, 2009-2013

- It has been widely applied in various domains over various geographical areas
  - Regional ecosystems<sup>2</sup>
  - Demographic maps<sup>1</sup>



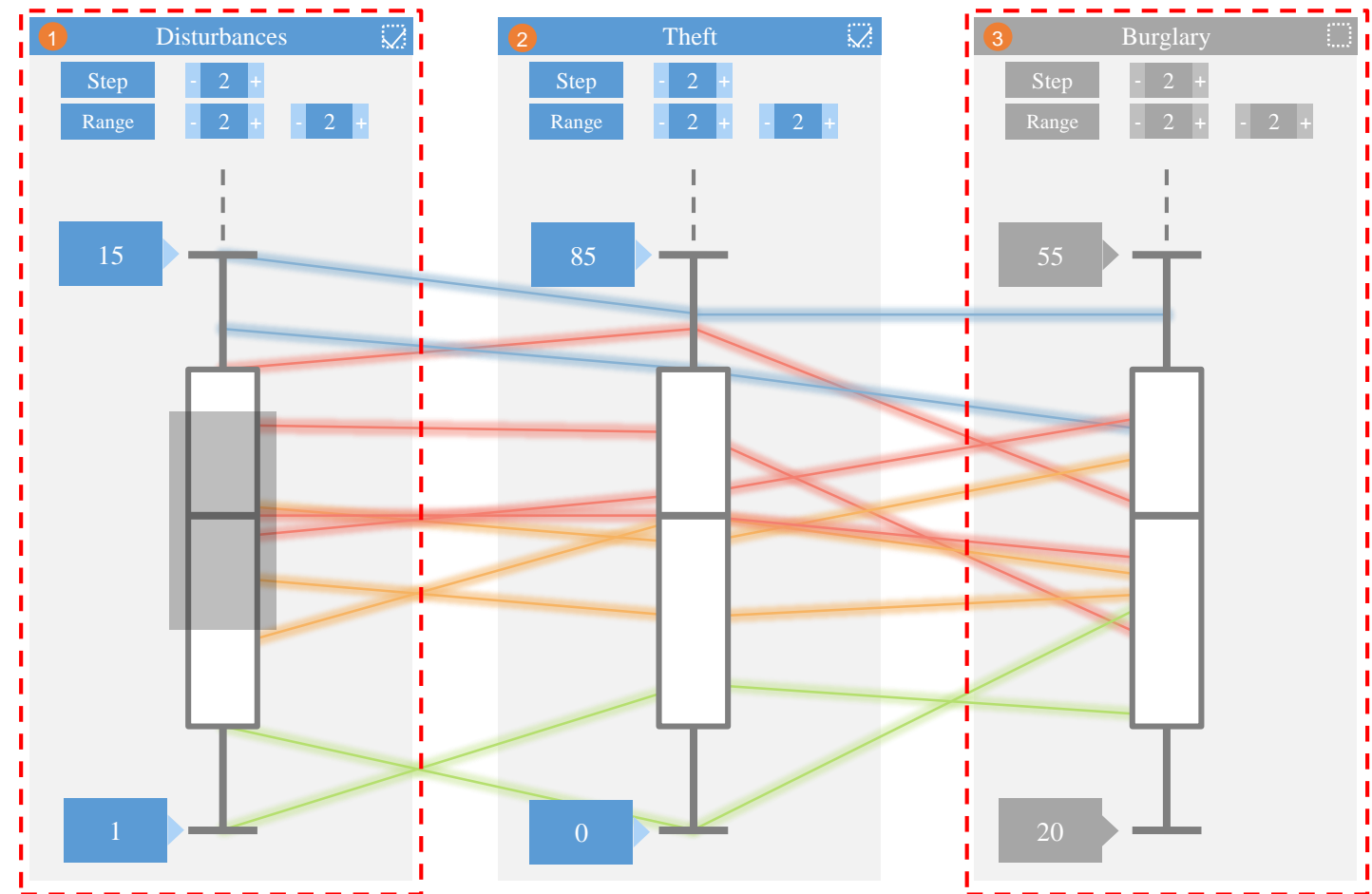
# Challenges



# Specification of uncertainty of an attribute

Using a preferred clustering algorithm and Setting the uncertainty range

1. Show the distribution of the attribute's
2. Specify a range the value to change in
3. Specify the step the value to change in



# Quantify the impact of data uncertainty

For each spatial unit, we simulate a classification across a range of uncertainty



- How many **labels will change** in the map if a measurement is uncertain
- How much **spatial autocorrelation** changes under the range of uncertainty

# Quantify the impact of data uncertainty

- How many labels will change in the map if a measurement is uncertain
  - How much **spatial autocorrelation** changes under the range of uncertainty
- 
- Join Count statistics<sup>1</sup>
  - Geary's C<sup>2</sup>
  - Getis-Ord General G<sup>3</sup>
  - Moran's I<sup>4</sup> is defined as

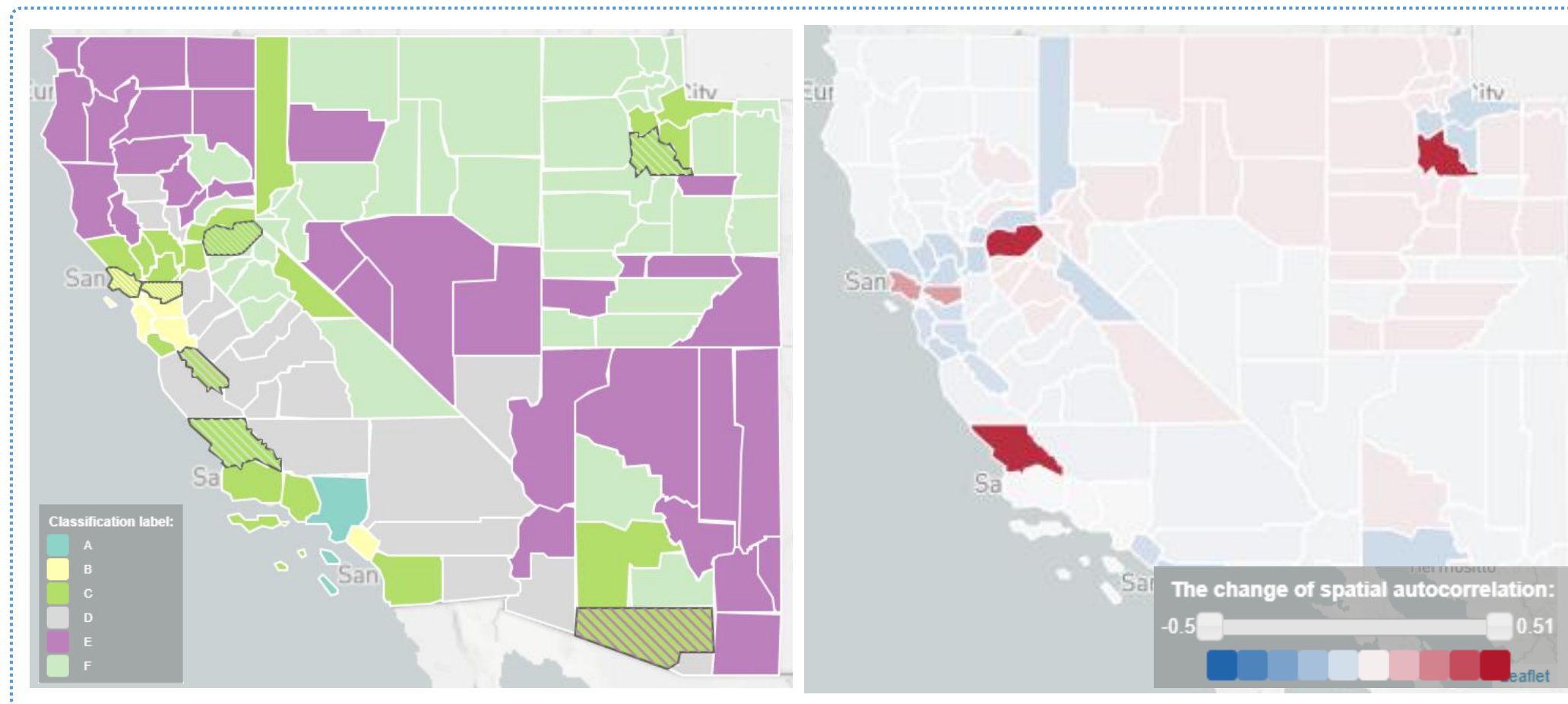
$$I = \frac{N}{\sum_i \sum_j w_{ij}} \frac{\sum_i \sum_j w_{ij} (x_i - \bar{X})(x_j - \bar{X})}{\sum_i (x_i - \bar{X})^2},$$



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Dual-Choropleth Map





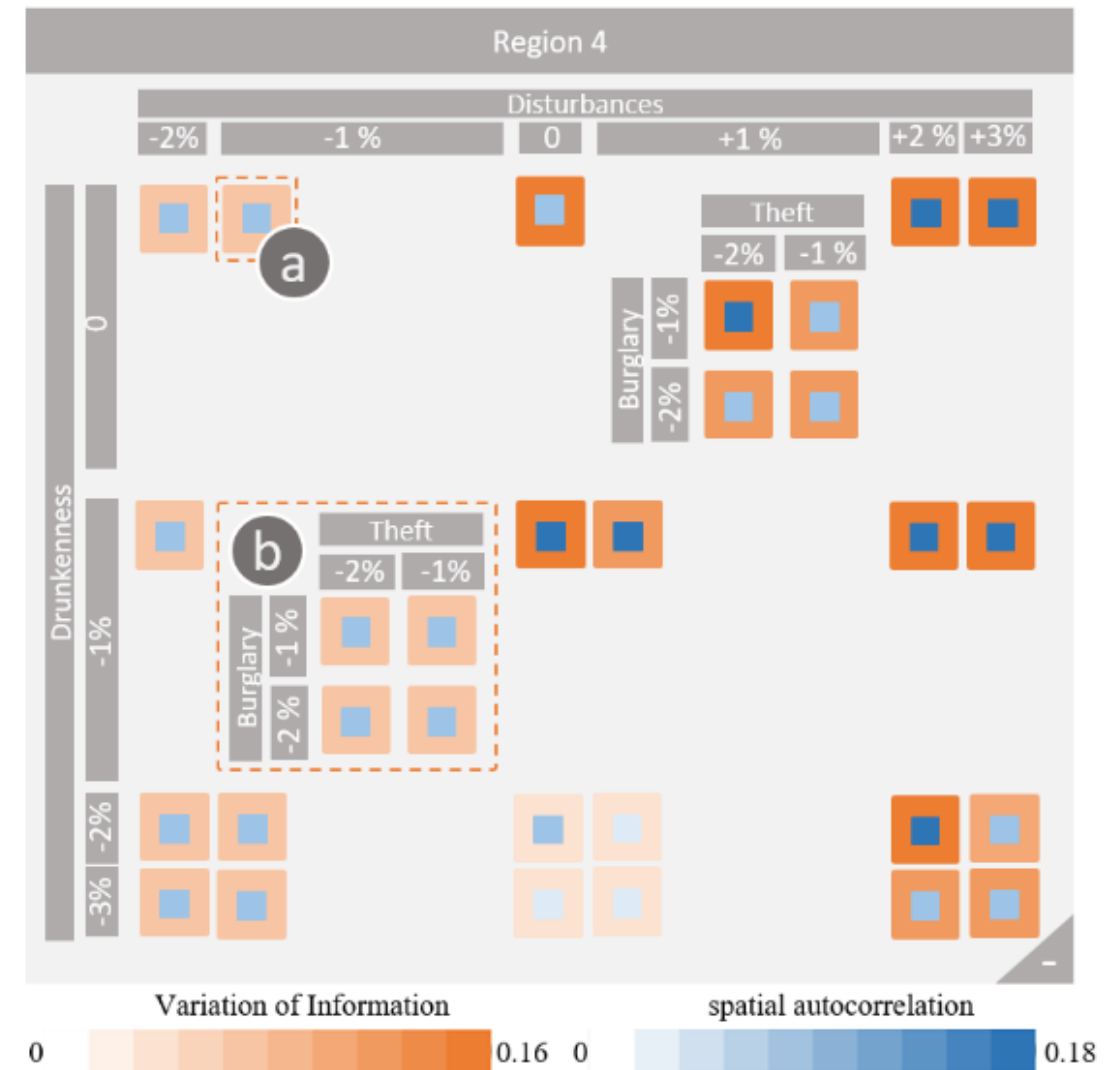
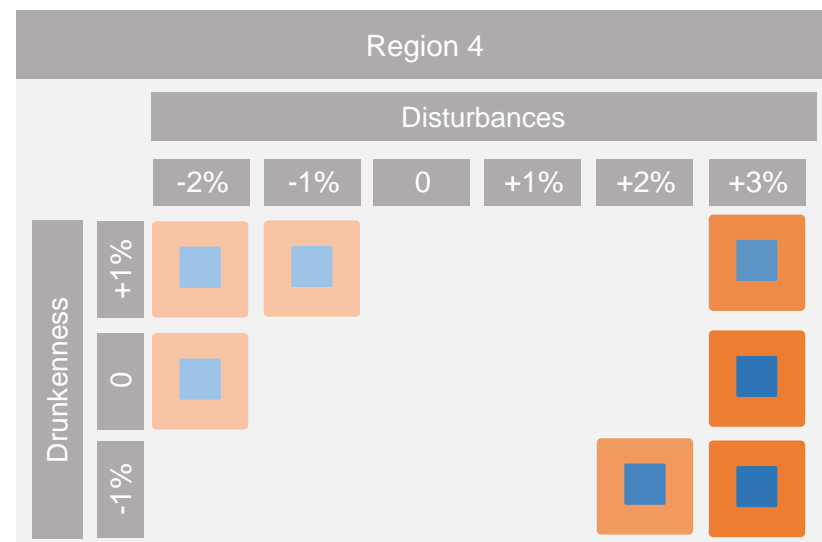
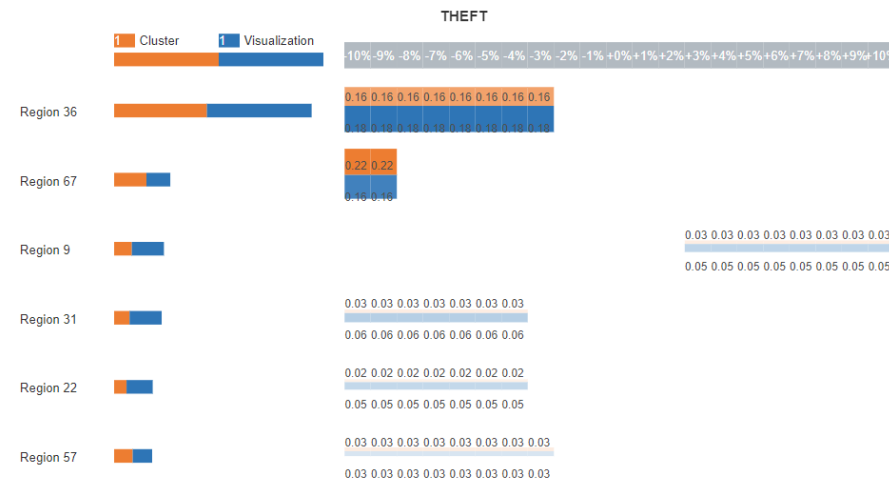
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## Single Attribute Impact Profile -- Impact River



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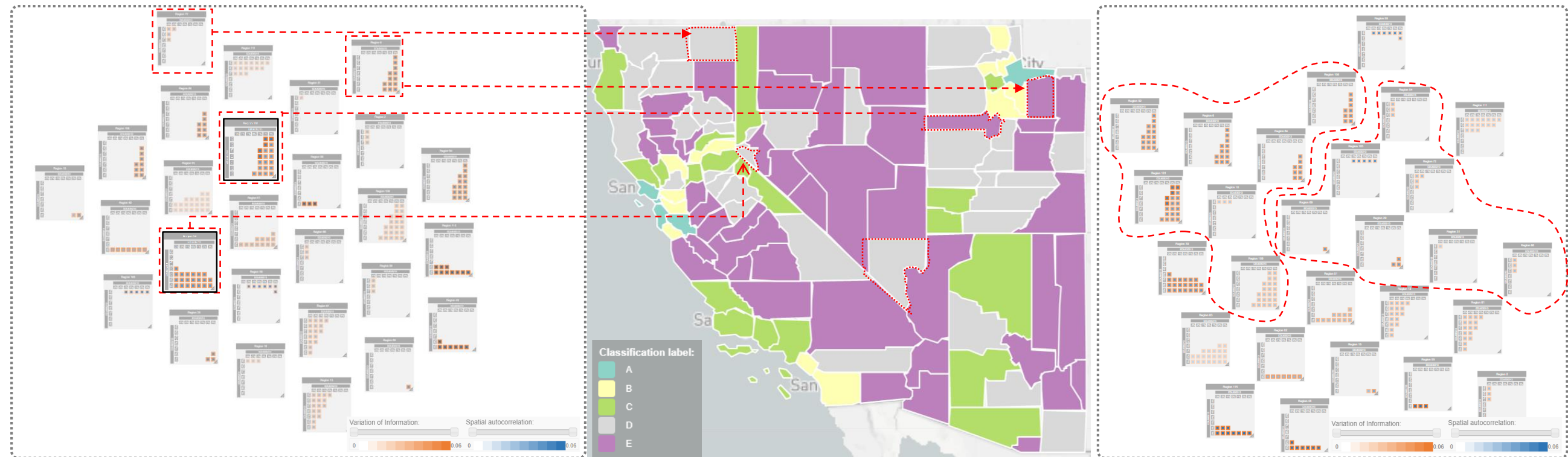
## Impact Matrix – Multi-Attribute Impact Profile



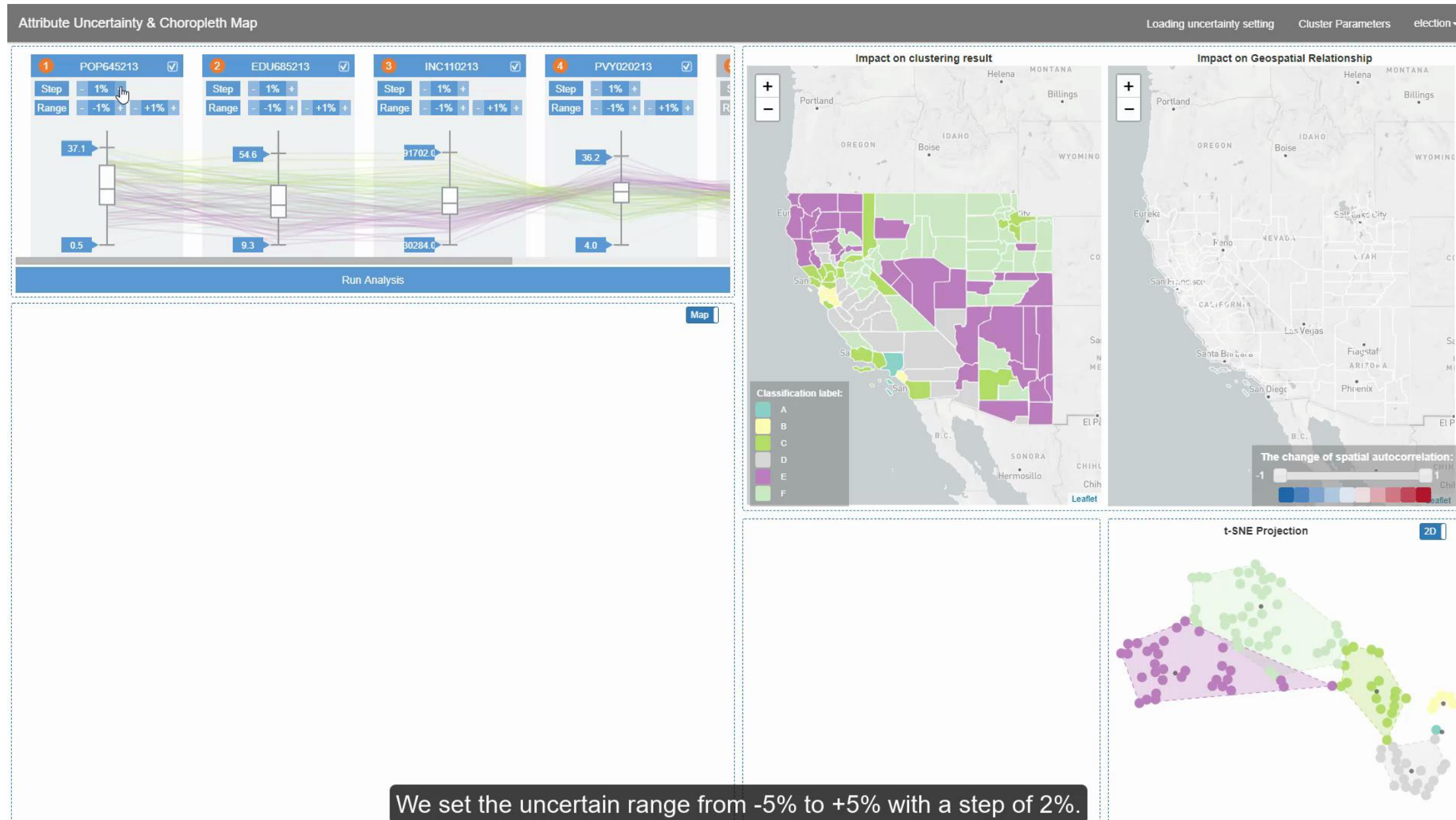
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Impact Matrix – Multi-Attribute Impact Profile

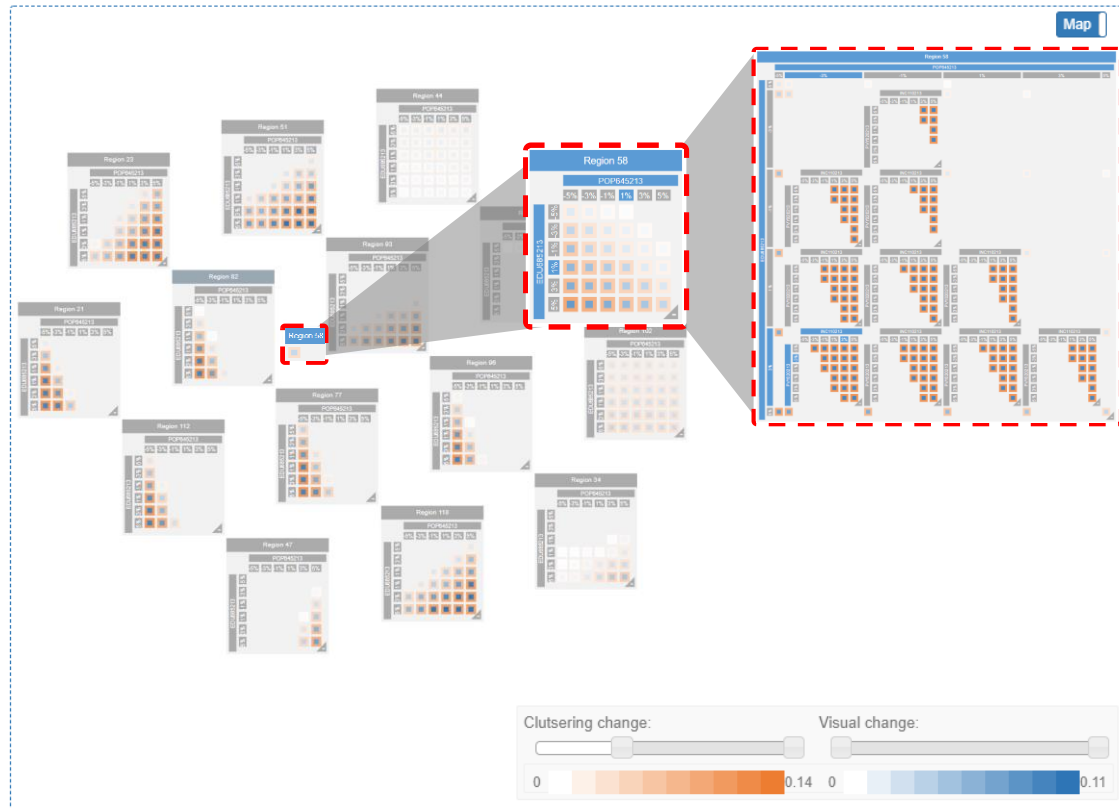
Map-Based and PCA-Based Layouts



# Case study



# Future Work



- To deal with the increased data dimension and the number of spatial units
  - increased **computational** cost
  - **inconvenient** to show the entire matrix by clicking the rectangles one by one.
- Some findings and discoveries might also be related to the **clustering algorithm**.
- To consider cascading effects when **multiple units change simultaneously**.



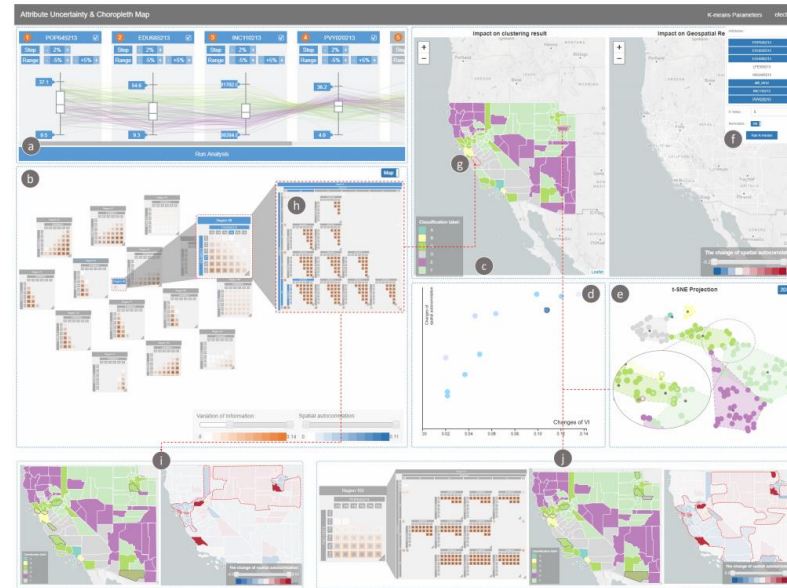
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System available at : <https://github.com/VADERASU/Choropleths-Attribute-Uncertainty>

Thank you!

Q&A



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The Department of Geography, Michigan State University

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