Multi-Viewpoint Panorama Construction With Wide-Baseline Images

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Abstract—We present a novel image stitching approach, which can produce visually plausible panoramic images with input taken from different viewpoints. Unlike previous methods, our approach allows wide baselines between images and non-planar scene structures. Instead of 3D reconstruction, we design a meshbased framework to optimize alignment and regularity in 2D. By solving a global objective function consisting of alignment and a set of prior constraints, we construct panoramic images, which are locally as perspective as possible and yet nearly orthogonal in the global view. We improve composition and achieve good performance on misaligned areas. Experimental results on challenging data demonstrate the effectiveness of the proposed method.

Index Terms—Image stitching, multi-view panorama, image alignment, wide-baseline images.

I. INTRODUCTION

W ITH the prevalence of smart phones, sharing photos has become popular. Since cameras generally have a limited field of view, panoramic shooting mode is provided, where the user can capture images under guidance to generate a panorama.

Panoramic stitching from a single viewpoint has been maturely studied. It is difficult however to generate reasonable results from a set of images under wide baselines. To produce

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This paper has supplementary downloadable material available at http://ieeexplore.ieee.org., provided by the author. The material includes a video that shows an example for Rapid Interactive Refinement. The user draws a line on one image, the stitching result will be updated instantly by incorporating this line preserving constraint into the energy function and solve the new solution. The total size of the video is 11.5 MB. Contact bao@cad.zju.edu.cn for further questions about this work.

Color versions of one or more of the figures in this paper are available online at http://ieeexplore.ieee.org.

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a large field-of-view image for a close object, the camera needs to be shifted to capture various regions, which causes trouble for general panorama construction. Images captured from multiple cameras raise similar challenges. All such applications require panorama techniques considering non-ignorable baselines among different cameras.

Many previous image stitching methods require simple camera rotation [1]–[3], or planar scene [4]. Violation of these assumptions may lead to severe problems. Recent methods [5]–[7] relaxed these constraints by dual-homography [5], or smoothly varying affine/homography [6], [7]. They work for images with moderate parallax, but are still problematic in the wide-baseline condition, as demonstrated in Figure 11.

In this paper, we propose a stitching approach for widebaseline images. Our main contribution is a mesh-based framework combining terms to optimize image alignment. A novel scale preserving term is introduced to make alignment nearly parallel to image plane but still allow local perspective correction. A new seam-cut model reduces visual artifacts caused by misalignment that is difficult to be handled by traditional seam-cutting algorithms [8], [9]. Figure 1 shows a challenging urban scene example where 14 images are captured in different positions. Our generated panorama is visually compelling.

II. RELATED WORK

A. 3D Reconstruction

Given the dense depth maps of a scene, the panoramic view can be generated by 3D modeling with texture mapping. However, multi-view stereo techniques [10]–[14] are constrained by a series of conditions including camera motion and Lambertian surface assumption. It is difficult to produce perfect 3D models in many cases, especially when there are only a few images. In the application of video stabilization where the baseline between source and target images is small, the reconstructed sparse 3D points may be enough for content-preserving warp [15], [16]. But this does not work that well for wide-baseline images with complex structure.

Agarwala *et al.* [4] constructed multi-viewpoint panoramas for approximately planar scenes. Structure-from-motion was used to recover camera poses and sparse 3D points. Then a dominant plane was selected manually so that the input images can be projected for stitching. In contrast, our method is an automatic approach without recovery of camera motion and 3D structures.

B. Mesh Optimization

Mesh optimization and manipulation perform well on image retargeting [17], [18], resizing [19]–[21], rectangling [22], and

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Fig. 1. Automatically constructed urban panorama with 14 wide-baseline images. (a) Input images. (b) The reconstructed panorama.

video stabilization [15], [16]. These methods use different global energy functions depending on their targets, and solve for the optimal mesh configuration. A similarity constraint was usually used for regularization, which however is not appropriate for perspective projection. For instance, parallel lines are not parallel under perspective transformation. Differently, our proposed straightness constraint does not involve the parallelism constraint and is more appropriate for perspective transformation.

C. Panoramic Mosaics

Panoramic image techniques [1], [3] work best for camera that undergoes only rotation. For other types of camera motion, misalignment artifacts could be introduced. Although seam optimization [8] and gradient domain fusion techniques [23] can be used, they do not solve the problem by nature. Recently, Gao *et al.* [5] proposed a dual-homography model to align overlapping images, where warping can be modeled as linear interpolation of two homographies. It is still insufficient for complex scenes.

Lin *et al.* [6] employed a smoothly varying affine model to stitch images with parallax. Zaragoza *et al.* [7] extended this method to general scenes with smoothly varying homographies. They use feature correspondence with adaptive weights to estimate locally coherent homographies. Both these methods assume that a global affine/homography can approximately represent image transformation and the local deviation is minor. This assumption is violated on wide-baseline images.

Different from the above methods, Zhang and Liu [24] focused on improving seam optimization. This method randomly picks subsets of correspondences and align only local parts of images. This process is repeated for optimizing seams to generate multiple candidate panoramas. The best panorama can be measured and chosen. Chang *et al.* [25] proposed combining the projective and similarity transformation to reduce distortion. This technique can be combined with that of [7]. But it still faces challenges in handling wide-baseline images. All above methods select one image as the reference, and warp other images to it, which may cause large perspective distortion when photographing a long scene.

D. Seamless Composition

Graph cuts algorithm [8] stitches images by optimizing a Markov random field (MRF). Agarwala *et al.* [4] proposed incorporating 3D information, while several other methods used a binary function depending on the visibility of pixels. The smoothness term penalizes color differences on the seams. In our wide-baseline cases, misaligned pixels may coincidentally have similar colors, which makes it difficult to detect bad seams via color. In order to address this problem, we combine alignment errors and colors in a new way.

III. FEATURE MATCHING WITH OUTLIERS REJECTION

Like many previous approaches [3], [7], we use SIFT [26] to find correspondences. For extremely challenging data, ASIFT [27] can be adopted to obtain more feature matches.

Estimating epipolar geometry with RANSAC [28] can reject mismatched correspondences. But outliers along the epipolar line are usually difficult to be eliminated, which may influence stitching. If the scene is planar, global homography estimation can also reject outliers. The method of [7] increases error threshold to accept feature correspondence from different planes. It works for small-baseline images. Our method is different–we use local homographies to robustly remove outliers, which works even in wide-baseline images.

For each feature point, we assume there is a plane in its local area, so that all neighbors are approximately on the same plane. For two arbitrary feature points, we regard them as neighbors if their distance is smaller than R. We use DLT [29] to fit a homography for all neighboring feature correspondences, and compute the residual error. If the error is less than a threshold γ , we mark it as an inlier. In our experiments, we generally set R = 50 and $\gamma = 5$.

The procedure is depicted in Algorithm 1. For image pair (I_i, I_j) , we first define the neighboring sets for each feature point in I_i and estimate the corresponding homographies. Each correspondence (p', q') is verified with several homographies since it can be included in different neighborhood sets. As long as it fits one homography, this correspondence will be recognized as an inlier. After enumerating all feature points in I_i , we obtain the inlier set S_1 for (I_i, I_j) . Then we swap I_i and I_j to get another inlier set S_2 by Algorithm 1. The final inlier set is $S_1 \cap S_2$.



6: if $|H(p') - q'|^2 < \gamma$ then 7: $S_{inlier} \leftarrow (p', q')$ 8: end if

- 8: en
- 9: end for
- 10: **end for**
- 11: return S_{inlier}
- 12: end procedure



Fig. 2. Outliers rejection comparison. (a) Matched features by SIFT. (b) Recognized inliers by RANSAC with global homography. (c) Recognized inliers by our approach.

As shown in Figure 1, the urban scene contains two major planes. With our local homography verification, outliers are rejected. Figure 2 gives a comparison with the methods using global and local homographies respectively. As shown in (b), traditional RANSAC with global homography eliminates many correspondences from the desktop. In contrast, our method preserves inliers in the same place. The stitching result is shown in Figure 3.

IV. ENERGY FUNCTION OF IMAGE STITCHING

After feature matching, we build regular mesh grids for all images, and index the control vertices from 1 to m. Then we put their coordinates into a 2m dimension vector

$$V = \begin{bmatrix} x_1 & y_1 & x_2 & y_2 & \dots & x_m & y_m \end{bmatrix}^{\top},$$

and optimize V to align corresponding feature points. Once V is solved for, the images are warped to a reference plane to generate desired panorama.

The energy function is defined as

$$E(V) = E_A(V) + \lambda_R E_R(V) + \lambda_S E_S(V) + E_X(V), \quad (1)$$



Fig. 3. Mesh based framework. (a) Regular mesh grids on input images. (b) Manipulating images via optimized mesh vertices. (c) Warping the images to a common plane.

where $E_A(V)$ is the alignment term, enforcing corresponding feature points to be warped to the same position. $E_R(V)$ is the regularization term, encouraging neighboring vertices to take similar transformation. $E_S(V)$ is the scale term, preventing large image scale change. λ_R and λ_S are the weights, which are usually set to 1 in our system. Optionally, $E_X(V)$ is an extra constraint used in cases of stronger regularization. The optimal vertex coordinates $V_{opt} = \arg \min_V E(V)$ are used to manipulate the images for generating a panorama.

In the example of Figure 3, the screen and desktop form two different planes, and our mesh-based model approximately fits two homographies as shown in (b). Compared to the single or dual homography representation, our multi-homography model has more degrees of freedom and can represent warping of a general smooth scene.

In addition, traditional image stitching methods [5]–[7] select one input image as the reference and warp other images towards it, which may cause perspective distortion for long sequences. Similar to [4], we project all images onto a common plane. The generated panorama is nearly orthogonal while the local perspective property is still preserved. In order to achieve this goal, we contribute a novel scale preservation term, which can constrain the image size to be nearly constant for ensuring this transformation. Our Laplacian regularization term also corrects local perspective distortion better than the similarity term used in [15], [20], and [22].

A. Feature Alignment

We represent each feature point as a weighted sum of their four enclosing control vertices, and minimize alignment errors



Fig. 4. Feature point interpolation. (a) Original mesh grid and a feature point p. (b) The warped vertices and feature point p^* .

of the warped points over all features. Similar to [16], we use bilinear interpolation to calculate weights on the original meshes, which is equivalent to the barycenter representation.

As illustrated in Figure 4, there is a feature point p inside the grid whose four vertices are denoted as v_1 , v_2 , v_3 , and v_4 . The interpolation weights are computed as

$$w_{1} = (v_{3x} - p_{x})(v_{3y} - p_{y}),$$

$$w_{2} = (p_{x} - v_{4x})(v_{4y} - p_{y}),$$

$$w_{3} = (p_{x} - v_{1x})(p_{y} - v_{1y}),$$

$$w_{4} = (v_{2x} - p_{x})(p_{y} - v_{2y}).$$
(2)

We assume that the interpolation weights are fixed after warping the grids (i.e., assuming affine transformation for each grid). As demonstrated in our supplementary document,¹ this assumption is reasonable in a typical panorama scenario especially when the mesh grid size is small. So we define the alignment term as

$$E_A(V) = \sum_{(p_i, p_j) \in C} \frac{1}{N_{p_i, p_j}} \|p_i^* - q_i^*\|^2$$

=
$$\sum_{(p_i, p_j) \in C} \frac{1}{N_{p_i, p_j}} \|W_i V - W_j V\|^2, \qquad (3)$$

where *C* is a set containing feature correspondences of all image pairs. p_i^* and q_i^* are warped positions of the two matched points, whose coordinates are weighted sums of the mesh vertices in *V*. W_i is a sparse $m \times 2$ weight matrix of p_i , formed as

where each column consists of 0 except the four positive values that sum to one. $W_i^{\top}V$ provides a 2D vector with x and y coordinates of p_i^* . N_{p_i,p_j} is the total number of feature points in the two cells containing p_i and p_j respectively. It is used to normalize the alignment error for different regions and prevent grids with rich features from dominating the alignment term. We note that even each grid performs affine transformation, the whole mesh grids can perform perspective alignment well as long as feature correspondences are accurate.

B. Regularization

The alignment term only affects grids with feature points. We need a regularization term to propagate transformation to other regions. In [15], [20], and [22], a similarity term is used to preserve the shape for each mesh grid. It however does not work well in our cases. For panoramic stitching, it is not reasonable to enforce similarity constraints, since perspective correction is generally necessary. With the local planar assumption, we prefer meshes that warp local neighboring regions with similar homographies.

As shown in Figure 6, for each vertex v, we estimate a local homography H with its four neighbors v_1 , v_2 , v_3 , v_4 and their warped positions v_1^* , v_2^* , v_3^* , v_4^* . Then we apply H on the vertex v to get the regular position v'. We minimize the Euclidean distance between v' and real position v^* .

Again, affine transformation was used to approximately constrain the coherence. So v' was replaced by Av where A is the affine transformation fitting warping of v_1, v_2, v_3, v_4 . With the linearity of affine transformation, we directly represent v'as a weighted sum of neighbors instead of solving for A. Since we divide the mesh grids evenly, the weights can be set as equal. Thus v' is simply the average of $v_1^*, v_2^*, v_3^*, v_4^*$, which leads a Laplacian operator on the mesh grids, i.e. $(v_1^* + v_2^* + v_3^* + v_4^*) - 4v' = 0$. Therefore, our regularization term is defined as

$$E_R(V) = \sum_{v} \|W_v V - \frac{1}{|N_v|} \sum_{v_i \in N_v} W_{v_i} V\|^2, \qquad (4)$$

where N_v is a 4-connected neighboring set of vertex v. For the vertices on the image boundary, we only use 2 horizontal or vertical neighbors. W_v and W_{v_i} are index matrices defined as

$$\begin{bmatrix} 0 & \dots & 1 & 0 & \dots & 0 \\ 0 & \dots & 0 & 1 & \dots & 0 \end{bmatrix},$$

which extracts x and y coordinates of v and v_i from V, respectively. As a result, $E_R(V)$ enforces neighboring vertices to favor similar affine transformation.

As shown in Figure 5, given two wide-baseline images, our approach can achieve better alignment than content-preserving warping [15], which preserves the shape of mesh grids. In order to measure the alignment quality, we average the warped images for a composite. The area with large alignment error is blurry. For fair comparison, we set the first image as the reference and warp the other one towards it. As shown in Figure 5(c), although the alignment result of [7] is reasonable, there are still misalignment and distortion artifacts due to the insufficient Gaussian smoothing weights.

C. Scale Preservation

The alignment and regularization terms actually form a linear system as AV = 0, where V = 0 always satisfies this linear system. In order to avoid this degeneration problem, methods [5], [7] were proposed to select one image as the reference view. This strategy works if there are only a few images, as shown in Figure 5. With the increasing field-of-view, images far from the reference one may be significantly distorted in order to reduce the alignment error. Figure 7 shows

¹http://www.cad.zju.edu.cn/home/gfzhang/projects/panorama/pano-supple. pdf



Fig. 5. Panorama construction with 2 wide baseline images. (a) Input images. (b) The average of the stitched images by content-preserving warps [15]. (c) The average of the stitched images by APAP [7]. (d) The average of the stitched images by our approach.



Fig. 6. Regularization term. (a) Original vertices. (b) Warped vertices.



Fig. 7. Image stitching result by fixing the first image.

a stitching result with 14 images, where the first one is the reference. The right-most images are obviously scaled down.

To address this problem, the scale constraint should be applied to all images equally. The scale of an image can be measured by its four edges, since the inner area can be interpolated once the edge scales are decided. We estimate a scaling factor for each image according to the feature points. Specifically, for a matched image pair (I_i, I_j) , we build a convex polygon P_i on the feature points from I_i and find its corresponding polygon P_j on image I_j . Then the relative scaling factor γ_{ij} is defined using the ratio of polygon perimeters

$$\gamma_{ij}=\frac{e_{P_i}}{e_{P_j}},$$

where e_{P_i} and e_{P_j} are the perimeters of P_i and P_j respectively. We estimate the absolute scaling factor for each image by solving

$$\arg\min_{s} \sum_{(i,j)\in C_{I}} |\gamma_{ij}s_{j} - s_{i}|^{2}$$

s.t.
$$\sum_{i\in I} s_{i} = N_{I},$$

where N_I denotes the number of images and C_I is the set of matched image pairs. The obtained scaling factors agree with the relative ratios while the sum of all scales is preserved.

With the scaling factors, we add a constraint for each image. The scale preserving term is defined as

$$E_{S}(V) = \sum_{I_{i} \in I} ||S(I_{i}^{*}) - s_{i}S(I_{i})||^{2},$$

$$S(I_{i}) = \begin{bmatrix} ||B_{t}|| + ||B_{b}|| \\ ||B_{l}|| + ||B_{r}|| \end{bmatrix},$$
(5)

where I_i^* and I_i are the *i*-th warped and original images respectively. *S* is a scale measurement for images defined as a 2D vector. B_t , B_b , B_l and B_r are the top, bottom, left and right edges of image I_i and can be represented with vertices *V*. For example, the length of edge B_t is a nonlinear function of *V* as

$$||B_t|| = \sqrt{(W_{tl}V - W_{tr}V)^{\top}(W_{tl}V - W_{tr}V)},$$

where W_{tl} and W_{tr} are index matrices for the top-left and top-right vertices. $||B_t||$, $||B_l||$ and $||B_r||$ are similarly defined.

We define $S(I_i)$ as a 2D vector, because the vertical and horizontal edges should be considered independently, which is better than summing vertical and horizontal edges. If we constrain each image edge as a constant, the freedom degree would be too small to correct perspective distortion. In contrast, preserving vertical and horizontal scales independently can allow higher freedom to correct perspective distortion and simultaneously avoid unnatural distortion.

By constraining image sizes, images are favored when orthogonally projected to a reference plane. In addition, our feature alignment and regularization terms encourage perspective alignment. Our scale preserving term $E_S(V)$ not only constrains image sizes but also allows perspective correction in local regions. With all these terms, our method can construct good quality panoramas, as shown in Figure 8(a). Since $E_S(V)$ is nonlinear, we propose an iterative approach to optimize it, which will be described in Section V.



Fig. 8. Image stitching with different prior constraints. (a) Averaging result by solving $E(V) = \lambda_A E_A(V) + \lambda_R E_R(V) + \lambda_S E_S(V)$. (b) Averaging result by further incorporating the line preserving term. (c) Averaging result by further incorporating the orientation term.

D. Extra Constraints

Our mesh-based model allows for incorporating extra constraints conveniently. For special cases of urban scenes and closed-loop camera motion, we incorporate one or multiple of the following priors to achieve even better results.

a) Line preserving constraint: To further reduce distortion, we introduce a line preserving term, which prevents the line segments from bending. We use the method of [30] to automatically extract line segments, and denote the set of lines as L. For a line segment l in L, we evenly sample a few points $\{p_1, p_2, ..., p_n\}$ so that each grid contains at least one point. To make l straight, all segments on the line are with the same direction, leading to the energy function

$$E_{line}(V) = \lambda_{line} \sum_{l \in L} \sum_{i=1}^{n-1} ([a_l, b_l]_{\perp} \cdot (W_{p_i}V - W_{p_{i+1}}V)), \quad (6)$$

where $[a_l, b_l]_{\perp}$ is the orthogonal direction of l and the coordinates of p_i are formed by linear interpolation of enclosing vertices, as in Eq. (3). λ_{line} is a weight, usually set to 1 in our experiments. We update a_l and b_l iteratively during optimization. Figure 9 shows the detected line segments. Incorporating the line preserving term, the stitching result is improved as shown in Figure 8(b).

b) Orientation constraint: Urban scenes generally contain a few vanishing lines, which are either vertical or horizontal. While enforcing their straightness, we also constrain the orientation. After detecting line segments, we divide them into vertical and horizontal categories L_V and L_H (colored in green and yellow respectively in Figure 9).



Fig. 9. Detected line segments.

We use RANSAC [28] to estimate vanishing points and eliminate outliers. The lines joining at the same vanishing point correspond to either horizontal or vertical lines. By assuming images are taken horizontally, we recognize lines with small angles as horizontal lines. Denoting p and qas two end points of such a line segment, they should have the same x or y coordinates. The orientation term is defined as

$$E_O(V) = \lambda_O (\sum_{l \in L_V} |(W_{p_x} - W_{q_x})V|^2 + \sum_{l \in L_H} |(W_{p_y} - W_{q_y})V|^2), \quad (7)$$

where W_{p_x} and W_{p_y} are the interpolation weight vectors of p in x and y coordinates respectively. λ_O is a weight with value 1 in our experiments. Mesh V warps p to position $(W_{p_x}V, W_{p_y}V)$. Figure 8(c) shows the result with the orientation term.

c) Loop closure constraint: For capturing a full panoramic view, the camera needs to rotate 360° so that the first image has overlapping content with the last one. However, the alignment term cannot be applied directly to the tail images because the feature points of the first and last images are aligned with an unknown offset.

In practice we align edges instead of points, so that the unknown offset can be eliminated. We define the loop closure term as

$$E_{loop}(V) = \lambda_L \sum_{(e_i, e_j) \in C_e} \|e_i - e_j\|^2,$$
(8)

where C_e is a set of corresponding edges matched between the first and last images. $e_i = p_i - q_i = (W_{p_i} - W_{q_i})V$ and $e_j = p_j - q_j = (W_{p_j} - W_{q_j})V$. p_i and q_i are the two ends of edge e_i . W_{p_i} and W_{q_i} are the weight matrices of p_i and q_i respectively. λ_L is a weight, set to 1000 to enforce the hard constraint if there is a loop closure.

If we connect each point pair in the *n*-point set, there are n^2 edges. For reducing the complexity, we randomly shuffle feature points and connect the neighboring ones. Figure 14 shows an example for generating a 360° panoramic image. With the loop closure constraint, the left and right most images become consistent, so that they can be aligned well if we project them onto a cylinder.

V. OPTIMIZATION

Since the energy function defined in (1) is not quadratic, we propose an iterative approach to optimize it. Specifically, only the scale and line preservation terms (i.e. E_S and E_{line}) are non-quadratic. We replace these terms by their linear approximation in each step, and then update the result iteratively.

A. Linear Approximation

As defined in Eq. (5), E_S is non-linear because the scale function *S* needs to compute the length of edges. In each iteration, we denote the direction of B_t as a normalized vector B_t^* , and assume that B_t^* does not change much in the next iteration. The length then can be approximated as $||B_t|| = B_t^{*\top} B_t$, leading to

$$E_{S1}(V) = \sum_{I_i \in I} (|B_t^{*\top} B_t + B_b^{*\top} B_b - 2s_i W|^2 + |B_l^{*\top} B_l + B_r^{*\top} B_r - 2s_i H|^2),$$

where W and H are the original width and height of the image, corresponding to the two components from $S(I_i)$ in Eq. (5).

Since we assume that the edge direction does not change much, we regularize it by introducing

$$E_{S2}(V) = \sum_{i \in I} (|B_{l}^{\prime \top} B_{l}|^{2} + |B_{b}^{\prime \top} B_{b}|^{2} + |B_{l}^{\prime \top} B_{l}|^{2} + |B_{l}^{\prime \top} B_{l}|^{2} + |B_{r}^{\prime \top} B_{r}|^{2}),$$

where B'_t , B'_b , B'_l , and B'_r are orthogonally normalized vectors of B^*_t , B^*_b , B^*_l , and B^*_r respectively. E_{S2} penalizes rotation of edges and enforces smooth update.

During each iteration, (5) is replaced by

$$E'_{S}(V) = E_{S1}(V) + \lambda E_{S2}(V),$$

where λ is a weight trading off the robustness and convergence speed. We found that setting λ to $0.1 \sim 0.5$ worked well in our experiments and the function converged quickly and stably (generally fewer than 10 iterations).

Similarly, the line preserving term E_{line} is not quadratic because the direction vector $[a_l, b_l]$ is unknown. We linearly approximate it by assuming that the lines change smoothly. In each iteration, we estimate the direction based on the current solution. By fixing a_l and b_l in Eq. (6), E_{line} becomes a quadratic function for us to optimize and update iteratively.

B. Efficient Optimization

With the above linear approximation, we optimize Eq. (1) efficiently. In each iteration, we solve a linear system of

$$\begin{bmatrix} A_A \\ A_R \\ A_S \\ A_X \end{bmatrix} V = \begin{bmatrix} 0 \\ 0 \\ b_S \\ b_X \end{bmatrix},$$

where A_A , A_R , A_S , A_X and 0, 0, b_S , b_X are Jacobian matrices and residual errors of the alignment, regularization, scale preserving, and extra terms respectively.

The left side of the equation is a $n \times 2m$ matrix with n much larger than 2m, since we have much more constraints than the number of vertices (m). We convert the stacked matrices into the summation format

$$(A_{A}^{T}A_{A} + \dots + A_{X}^{T}A_{X})V = A_{S}^{T}b_{S} + A_{X}^{T}b_{X},$$
(9)

reducing the matrix size to $2m \times 2m$. Since these matrices are rather sparse, we utilize the sparsity to significantly reduce the computational complexity.

Except for the scale and line preserving terms, other terms are all quadratic, thus their Jacobian matrices and residual errors are constant. We update A_S , b_S , A_{line} , and b_{line} in each iteration. For the "Urban1" example with 14 images, it takes 2.30 seconds to initialize the matrix and 0.21 second to update the matrix in each iteration. The whole optimization takes 15.4 seconds in total with three iterations. We use Cholesky decomposition to analytically solve the linear system. If we use conjugate gradient algorithm to iteratively update the solution in each iteration, the optimization speed could be even quicker.

C. Rapid Interactive Refinement

Since our term update and optimization are rather efficient, our system provides a line-drawing tool to allow the user to correct residual image distortion and improve alignment interactively. With line preserving constraints, solution is updated quickly by solving Eq. (9). The updating time is generally $1 \sim 5$ seconds. Please see our supplementary video² for real-time interactions and fast refinement.

VI. SEAMLESS COMPOSITION

After solving Eq. (1), we warp input images to a common coordinate system. For overlapping regions, a simple average may cause blurring. Graph cuts has been used in [8] to find seams between images so that pixels on the two sides of the seam are consistent.

In previous approaches, color difference is commonly used as reference. In our wide-baseline cases, alignment errors can be large and the misaligned pixels might have similar colors. We propose combining the alignment error and color difference to generate a better condition.

A. Alignment Score

Given a pair of overlapping images I_i and I_j , we measure alignment errors for all matched feature points and map them to [0, 1] through Gaussian of

$$s_{p,q} = \exp(-\frac{\|\Psi_i(p) - \Psi_j(q)\|^2}{\sigma_1^2})$$

where (p, q) is a pair of corresponding feature points from I_i and I_j respectively. Ψ_i and Ψ_j are the warping functions corresponding to I_i and I_j , respectively. σ_1 is set to 0.003D where D denotes image diagonal length. For features with the alignment error larger than 0.01D, we assume they are not reliable and ignore them in following process.

With the feature alignment scores, we produce a dense score map on I_i . The contribution of feature p to pixel x depends on distance from p to x as

$$w_{p,x} = \exp(-\frac{\|p-x\|^2}{\sigma_2^2}).$$

²http://www.cad.zju.edu.cn/home/gfzhang/projects/panorama/pano-video. wmv σ_2 should be related to the alignment score, since a well aligned feature point propagates better than those with larger alignment errors. For rotational camera motion or a locally planar scene, pixels surrounding the feature points are very likely to be also good. In our experiments, we generally set σ_2 to $0.4D \cdot s_{p,q}$.

We define the alignment score map for image I_i as

$$S_{I_i}(x) = \frac{\sum_p w_{p,x}^2 s_{p,q}}{\sum_p w_{p,x}}.$$

Finally we repeat the same process on I_j to generate S_{I_j} , warp the score maps according to the optimized mesh, and average them as the final map as

$$S_{align} = \frac{1}{2} (\Psi_i(S_{I_i}) + \Psi_j(S_{I_j})).$$
(10)

B. Color Score

We also use the color difference as the measure of consistency. A Gaussian function is adopted to smooth the energy. The color distance is normalized as

$$S_{color}(x) = \exp(-\frac{|\Psi(I_i)(x) - \Psi(I_j)(x) - \mu|^2}{\sigma^2}), \quad (11)$$

where $\Psi(I_i)$ and $\Psi(I_j)$ are the warped images. μ and σ are the mean and standard deviation of the L2 distance, which are estimated with the overlapping region.

With the Gaussian function, misaligned pixels with large color difference do not provide absurdly large costs. With increasing color distances, the color score moves close to 0. Misaligned pixels are thus assigned with small scores, no matter how different the colors are.

Conditions such as lighting and exposure affect the global luminance of images. With normalization factors μ and σ , they can be corrected to an extend. The global color difference can be finally resolved by gradient domain fusion [23].

C. Graph-Cuts Optimization

We combine the alignment score (10) and color score (11), and convert them to a function

$$E_{(i,j)}(x) = \max(0, \min(1.5 - S_{align} - S_{color}, 1)). \quad (12)$$

Since $S_{align} \in [0, 1]$ and $S_{color} \in [0, 1]$, the value of $-S_{align} - S_{color}$ is in the range of [-2, 0]. We adopt the formula in (12) to truncate the value and only choose the medium range [0, 1.0], which can avoid the influence of extreme cases. Now $E_{(i,j)}(x)$ describes the consistency of image pair (I_i, I_j) at pixel x. Given a seam connecting I_i and I_j , the total consistency is defined as the accumulated $E_{(i,j)}(x)$ over the seam pixels. For the special case i = j, we define $E_{(i,j)}(x) = 0$.

Similar to previous methods, we optimize the function via graph cuts [31] as

$$E_{cut}(p,L) = \sum_{p} E_{d}(p,L_{p}) + \lambda_{s} \sum_{(p,q)\in N} E_{s}(p,q,L_{p},L_{q}),$$
(13)



Fig. 10. Seamless Composition. (a) Graph cuts result with the traditional smoothness term only incorporating color difference. (b) Our result. (c) Our final result with gradient domain fusion.

where E_d is the data term defined by the availability of pixels, E_s is the smoothness term preferring well aligned regions, and N is the set of neighboring pixels. λ_s is a smoothness weight set to 256 in our experiments.

The data term E_d is defined as

$$E_d(p, L_p) = \begin{cases} 0, & x \in \hat{I}_{L_p} \\ \eta, & otherwise \end{cases}$$

where \hat{I}_{L_p} is a warped mask of the image with index L_p . If a pixel is available in the warped L_p -th image, its cost is 0, otherwise it is set to a very large penalty η to avoid being labeled with L_p .

The smoothness term E_s is defined as the sum of consistency scores on the neighboring pixels:

$$E_s(p,q,L_p,L_q) = E_{(L_p,L_q)}(p) + E_{(L_p,L_q)}(q).$$

The final labeling problem is solved by minimizing the energy. We use graph cuts [31] to efficiently solve it, and then apply gradient domain fusion [23].

As shown in Figure 10 (a), the blue pot is misaligned due to the lack of reliable features. Due to similar color, traditional seam-cutting method [9] splits this area. With our new energy function, such a seam causes a large cost and thus is prohibited. The result shown in (b) demonstrates the effectiveness of our method.

VII. EXPERIMENTS

To evaluate the performance, we conducted experiments on several challenging wide-baseline image datasets, including urban image datasets, indoor image datasets, wide-angle image datasets. If there is no special mention, our results are generated automatically without user interactions.

The timing statistics are shown in Table I with implementation on a desktop PC with an Intel i5 CPU@3.30GHz and a GeForce GTX 760 display card. We generally use



Fig. 11. Image stitching with "Urban2" dataset including 8 wide-baseline images. (a) Input images. (b) Panorama generated by AutoStitch. (c) Panorama generated by APAP. (d) Panorama generated by our approach.

Datasets	Urban1	Urban2	Globe	Campus	Desktop
	Fig. 1	Fig. 11		Fig. 14	Fig. 10
Image Number	14	8	24	15	6
SIFT Matching	2.1s	1.7s	5.6s	4.0s	1.2s
Image Stitching	15.4s	5.2s	62.0s	48.3s	5.1s
Average Blending	0.95s	0.4s	1.61s	0.87s	0.18s
GC Optimization	79.3s	19.4s	215.3s	79.7s	16.6s
GD Fusion	59.3s	33.7s	76.3s	51.4s	18.3s
APAP	176.1s	65.4s	503.4s	-	155.7s
AutoStitch	$\sim 6s$	$\sim 5s$	$\sim 12s$	$\sim 8s$	$\sim 3s$

TABLE I The Running Time on Our Datasets

SiftGPU [32] to perform feature matching with outlier rejection, which takes $1 \sim 6$ seconds in our datasets. For widebaseline urban image datasets, we also use ASIFT [27] to obtain more matches, which takes several minutes additionally. Other modules of our system are implemented without GPU acceleration. For each image, it takes about 0.2 second to extract line segments if line preserving constraint is used. Our stitching optimization is also very efficient, which is an order of magnitude faster than APAP [7]. For seamless composition, our graph-cuts optimization takes 79.3 seconds, and gradient domain fusion takes 59.3 seconds for "Urban1" example in Figure 1. Both APAP and AutoStitch³ [3] use simple blending techniques without global optimization, where the composition time is close to that of our average blending operation listed in Table I.

A. Results on Urban Image Datasets

Figure 11 shows an urban scene example with 8 widebaseline images, where the building and street form two dominant planes. AutoStitch does not find many correspondences under the perspective assumption. APAP [7] constructs a complete panorama, but suffers from distortion due to the lack of prior constraints. The same correspondences are used for APAP and our approaches for fair comparison. Our mesh-based model generates a dualhomography panorama, as shown in (d). All methods cannot handle strong occlusions. Figure 1 shows another example with the input of 14 images. The results of AutoStitch and APAP are contained in the supplementary document.

We also test our approach using the long sequences from [4]. Figure 12 gives a comparison, where (a) and (b) show the average images of the stitched images using the method of [4] and ours respectively. Compared to [4], our method does not require 3D information and can work with much sparser images. We choose only 13 images from the 107 images and achieve comparable result. Like that of [4], for this example, we use view selection strokes to guide composition. We do not apply other manual work, such as inpainting.

B. Results of Wide-Angle and Loop-Closing Images

With adaptive homographies, our method can handle images with significant radial distortion. For the example shown in Figure 13, we capture 3 images by GoPro Hero3 camera.



Fig. 12. Long scene example. (a) Average of 107 stitched images by the method of [4]. (b) Average of 13 stitched images by our approach. (c) Final result of [4]. (d) Our final result.



Fig. 13. Image stitching with radial distortion. (a) Three images captured with GoPro Hereo3. (b) The stitching result by AutoStitch. (c) The average of the stitched images by APAP. (d) The average of the stitched images by our method.

Due to radial distortion, AutoStitch and APAP do not work well as shown in Figures 13 (b) and (c). Our stitching result contains less ghost artifacts.

Figure 14 shows a 360° panorama example. The input images are also with significant radial distortion. With the loop closure term in Eq. (8), the left and right most images become more consistent with each other. They are aligned when projecting onto a cylindrical surface. We note the smoothly-varying transformation assumption makes the right most highlight not aligned very well.

Besides panoramic mosaics, our approach can also be applied to texture unfolding for simple objects. The supplementary document shows an example.

C. Application for Selfie

In selfies, panoramic stitching is also useful. Since the camera is close to the face, the introduced parallax can be rather large. Figure 15 shows an example, where AutoStitch causes misalignment. APAP performs better with the multi-homography model. Our r is with the decent quality.

D. Quantitative Evaluation

We follow the method of [7] to evaluate results quantitatively. For pairwise stitching, we quantify the alignment error of the estimated warp $f : R^2 \rightarrow R^2$ by the root



Fig. 14. 360° panoramic mosaic with radial distorted images. (a) The stitching result by AutoStitch. (b) Highlights. (c) The average of the stitched images by our method without seamless composition. (d) Our final result with seamless composition.



Fig. 15. Selfie example. (a) Selfies. (b) The stitching result by AutoStitch. (c) The average of the stitched images by APAP. (d) The average of the stitched images by our approach. (e) Our final result with seamless composition.

mean squared error (RMSE) of corresponding feature points $\{x_i, x_i'\}_{i=1}^N$, where $RMSE(f) = \sqrt{\frac{1}{N}\sum_{i=1}^N ||f(x_i) - x_i'||^2}$. We randomly partition all feature matches into "training" and

"testing" sets with equal sizes. We use the training set to optimize the warp, and evaluate RMSE on both sets.

We also compare pixel-wise difference quantitatively. Following [7], [33], we define a pixel x as an outlier if there is

TABLE II Average RMSE (TR: Training Set Error, TE: Testing Set Error)

TR	TE	%outliers
1.26	1.82	2.86
0.84	1.72	2.63
0.78	0.90	8.12
0.24	0.71	7.02
1.43	3.57	25.64
1.08	3.33	24.29
0.43	0.62	9.30
0.31	0.63	9.95
0.88	1.04	12.42
0.41	0.94	12.94
1.10	1.47	15.44
0.45	1.26	15.39
0.79	0.90	11.44
0.24	0.81	11.04
	TR 1.26 0.84 0.78 0.24 1.43 1.08 0.43 0.31 0.88 0.41 1.10 0.45 0.79 0.24	$\begin{array}{c c c c c c c c c c c c c c c c c c c $

no similar pixel (intensity difference less than 10 gray levels) within the 4-pixel radius of the warped point. The percentage of outliers in the overlapped area is calculated similarly. For each datum, we repeat this process 20 iterations, and use the average of the results. In each iteration we use the same feature matches on both methods. For our wide-baseline image pairs shown in our supplementary document, since the number of the matched features is already small, we use all matches and evaluate the whole RMSE and outlier percentage.

For fair comparison, we select the first frame as reference, same as that in [7]. In this case, most prior constraints are unnecessary. So we only use feature alignment and regularization terms to construct the energy function, i.e. $E(V) = E_A(V) + \lambda_R E_R(V)$.

Table II shows the average RMSE (in pixels) and outlier percentage on different image pairs. "railtracks", "conssite", and "garden" are from [7]. "apartment", "carpark" and "temple" are from [5]. "chess" is from [6]. For APAP, we use the implementation provided by the authors. In most image pairs, our method yields lower errors.

VIII. DISCUSSION AND CONCLUSIONS

We have presented a new image stitching approach for wide-baseline images. With the flexibility of a mesh-based model, our method can accommodate moderate deviation from the planar structures. By combining feature alignment, regularization, scale preservation and other extra constraints, a reasonable multi-viewpoint panorama is accomplished without explicit 3D reconstruction.

Our approach still has limitations. If a straight line spans across multiple images, our method can only preserve the local straightness in each image. This problem can be addressed either by performing line matching or manually specifying feature match along the lines if the corresponding matches are not automatically found.

In addition, if the input images are with significant occlusion – one region appears in one image but is occluded in others – the occluded parts may not be aligned correctly, such as the highlighted red circle region in Figure 11(d). This problem can be alleviated with user interaction and seam cut. Our future work will be using the multi-homography model

to support the discontinuity representation around occlusion boundaries, which may require accurate segmentation.

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